

Exam Seat No. \_\_\_\_\_

# THAKUR COLLEGE OF SCIENCE & COMMERCE

NAAC  
Accredited  
with Grade "A"  
(3<sup>rd</sup> Cycle)



ISO  
9001 : 2015  
Certified

## Degree College Computer Journal CERTIFICATE

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This is to certify that the work entered in this journal  
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who has worked for the year 2019 in the Computer  
Laboratory.

*Amit*  
Teacher In-Charge

Date : 27.2.19

Head of Department

*Examiner*

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## Practical 1:

## → R Software:

1. R is a software for statistical analysis and data computing.
2. It is an effective data handling software and outcome storage is possible.
3. It is capable of graphical display.
4. It is a free software.

(Q) Solve the following:-

$$\textcircled{1} \quad 4 + 6 + 8 / 12 - 5$$

$$> 4 + 6 + 8 / 12 - 5$$

$$> 9$$

$$\textcircled{2} \quad 2^2 + 1 - 31 \quad 4 + \sqrt{45}$$

$$> 2^2 + 1 - 31 + \sqrt{45}$$

$$> 13.7082$$

$$\textcircled{3} \quad 5^3 + 7 \times 5 \times 8 + 467.5$$

$$\rightarrow 5^3 + 7 \times 5 \times 8 + 467.5$$

$$\rightarrow 414.2$$

$$\textcircled{4} \quad \text{round off } (46.77 + 9 \times 8)$$

$$> \text{round } (46.77 + 9 \times 8)$$

$$> 79$$

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(Q2) Solve:-

- (i)  $> C(2, 3, 5, 7) * 2 \rightarrow [1] 4, 6, 10, 14$   
(ii)  $> C(2, 3, 5, 7) + C(2, 3) \rightarrow [1] 4, 9, 10, 21$   
(iii)  $> C(2, 3, 5, 7) * C(2, 3, 6, 2) \rightarrow [1] 4, 9, 30, 14$   
(iv)  $> C(1, 6, 2, 3) * C(-2, -3, -4, -1) \rightarrow [1] -2, -18, -8, -3$   
(v)  $> C(2, 3, 5, 7) *^1 2 \rightarrow [1] 4, 9, 25, 49$   
(vi)  $> C(4, 6, 8, 9, 4, 5) *^1 C(1, 2, 3) \rightarrow [1] 4, 36, 512, 9, 16, 125$   
(vii)  $> C(6, 2, 7, 5) / C(4, 5) \rightarrow [1] 1.80, 0.40, 1.75, 1.00$

(Q3) Solve:-

$$\begin{aligned} (1) &> x = 20 \\ &> y = 80 \\ &> z = 2 \\ &> x^2 + y^2 + z \\ &[1] 27402 \end{aligned}$$

$$\begin{aligned} (2) &\sqrt{x^2 + y} \\ &> 894t(x^2 + y) \\ &[1] 20.73644 \end{aligned}$$

$$\begin{aligned} (3) &x^2 + y^2 \\ &x^2 + y^2 z \\ &[1] 1300 \end{aligned}$$

$$\begin{matrix} x & [1] & [2] & [3] \\ [1,] & 4 & -2 & 6 \\ [2,] & 7 & 0 & 7 \\ [3,] & 9 & -5 & 3 \end{matrix}$$

(Q4) Solve :-

$$(1) \begin{bmatrix} 1 & 6 \\ 2 & 6 \\ 8 & 7 \\ 4 & 8 \end{bmatrix}$$

> x ← matrix(x(nrow=4, ncol=2, data = c(1:8)))

> x [1] [2]

$$[1,] 1 \leftarrow$$

$$[2,] 2 \leftarrow 6$$

$$[3,] 3 \leftarrow 7$$

$$[4,] 4 \leftarrow 8$$

$$(2) x = \begin{bmatrix} 9 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}, y = \begin{bmatrix} 10 & -6 & 1 \\ 12 & -4 & 9 \\ 16 & -6 & 8 \end{bmatrix}$$

> x = matrix(nrow=3, ncol=3, data = c(4, 7, 9, -2, 0, 1))

> y = matrix(nrow=3, ncol=3, data = c(10, 12, 15, -6, 4, 7, 9, 6))

Points as follows  
Data :-  
47,  
> m = C(g9v  
> length(m)  
> a - cut  
> b - table  
> c - transform  
> c

1  
2  
3  
4  
5  
6  
7  
8

029

Q) Points of marks of computer Science students are  
as follows:-

Data :- 59, 20, 35, 24, 46, 56, 55, 45, 27, 22,  
47, 58, 54, 40, 50, 32, 36, 29, 35, 39

> n = l (given data)

> length (n) > [2] 20 > breaks = seq (20, 60, 5)

> a = cut (n, breaks, right = FALSE)

> b = table (a)

> c = transform (b)

> c

	x	freq
1	[20, 25)	3
2	[25, 30)	2
3	[30, 35)	1
4	[35, 40)	4
5	[40, 45)	1
6	[45, 50)	3
7	[50, 55)	2
8	[55, 60)	4

Q 18  
Ex 2.9

Q50

(1) > prob = c(0.1, 0.2, -0.5, 0.4, 0.3) 0.5)

> sum(prob)

[1] 1.0

(2) > p = c(0.2, 0.2, 0.3, 0.2, 0.2)

> sum(p)

[1] 1.0

(3) p = c(0.2, 0.2, 0.35, 0.15, 0.1)

> sum(p)

[1] 1.0

## Practical 2:

## Probability Distribution.

(i) Check whether the followings are pmf or not

(i)  $x \ P(x)$

0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

(ii)  $x \ P(x)$

1	0.2
2	0.2
3	0.3
4	0.2
5	0.2

(iii)  $x \ P(x)$

10	0.2
20	0.2
30	0.35
40	0.15
50	0.1

(iii) I satisfies both the conditions.

This is a pmf.

i)  $P(2) = -0.5$

cannot be a probability mif. since pmf is ( $> 0$ ) for all  $x$ .

ii) It cannot be a probability mass fn. as summation pmf = 1.

Q8Q:

(2) (i) Find cdf. for the following pmf & stage the graph.

(i)	$x$	10	20	30	40	50
	$P(x)$	0.2	0.2	0.35	0.15	0.1

(ii)	$x$	1	2	3	4	5	6
	$P(x)$	0.15	0.25	0.1	0.2	0.2	0.1

$$(i) > P(X) = 0 \quad x \leq 10$$

$$= 0.2 \quad 10 \leq x \leq 20$$

$$= 0.45 \quad 20 \leq x \leq 30$$

$$= 0.75 \quad 30 \leq x \leq 40$$

$$= 0.95 \quad 40 \leq x \leq 50$$

$$= 1.0 \quad x \geq 50$$

$$> p = c(0.2, 0.2, 0.35, 0.16, 0.1)$$

[1] 1

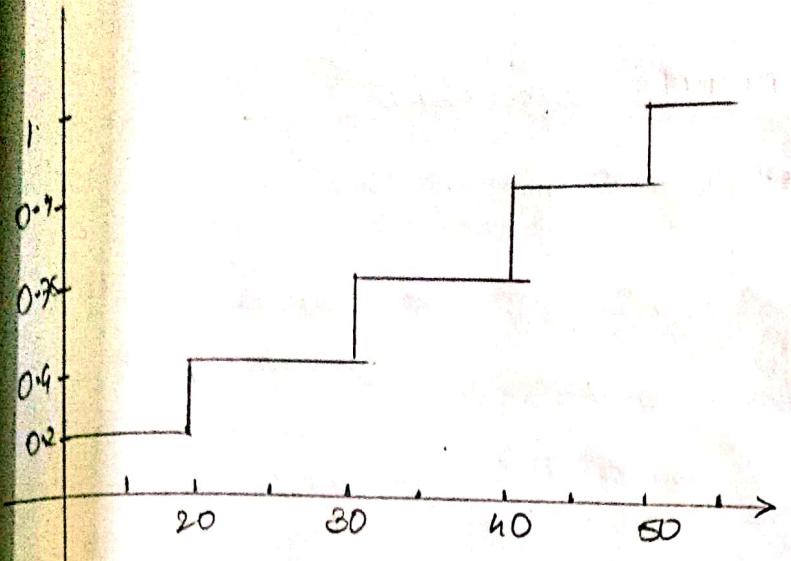
> cumsum(p)

$$[1] 0.20 \quad 0.4 \quad 0.75 \quad 0.9 \quad 1.00$$

$$> pi = c(20, 30, 40, 50)$$

> plot(pi, cumsum(p), "s")

031



(ii)  $P(x) = \begin{cases} 0.15 & x < 1 \\ 0.25 & 1 \leq x < 2 \\ 0.1 & 2 \leq x < 3 \\ 0.2 & 3 \leq x < 4 \\ 0.2 & 4 \leq x < 5 \\ 0.1 & 5 \leq x < 6 \end{cases}$

> p = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)

> sum(p)

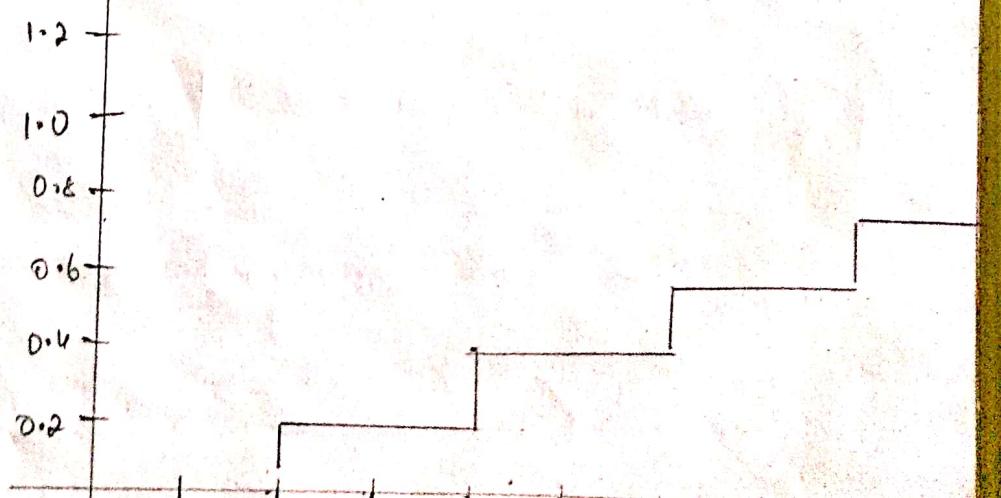
[1] 1

> cumsum(p)

[1] 0.15 0.40 0.5 0.7 0.9 1.0

> pi = (1, 2, 3, 4, 5, 6)

> plot(pi, cumsum(p), "s")



180

(iii) Check whether following is pdf or not:

$$f(u) = 3 - 2u$$

$$0 \leq u \leq 1$$

$$f(u) = 3u^2$$

$$0 < u < 1$$

$$(i) f(u) = 3 - 2u \quad 0 \leq u \leq 1$$

$$\int_0^1 (3 - 2u) du$$

$$= \int_0^1 3du - \int_0^1 2udu$$

$$= 3[u]_0^1 - 2 \frac{[u^2]_0^1}{2}$$

$$= 3 - 1 = 2$$

$$(ii) f(u) = 3u^2. \quad 0 < u < 1$$

$$\int_0^1 3u^2 du$$

$$= \frac{3[u^3]_0^1}{3}$$

$$= 1^3 - 0$$

$$= 1$$



A  
✓

### Practical 3:

#### Binomial Distribution

① Find the probability of exactly 10 success in 100 trials with  $p = 0.1$

- ② Suppose there are 12 MCQs. Each question has 5 options out of which 1 is correct, find the probability
- ① of having exactly 4 correct answers.
  - ② Atmost 4 correct answers.
  - ③ More than 5 correct answers.

④ Find complete distribution when  $n=5$  &  $p=0.1$

$$\text{⑤ } n=12$$

$$p=0.25$$

Find:

- ①  $P(n=5)$
- ②  $P(n \leq 5)$
- ③  $P(n > 7)$
- ④  $P(5 < n < 7)$

Ans:

i)  $>\text{dbinom}(10, 100, 0.1)$   
[1] 0.1318653

ii)  $>\text{dbinom}(4, 12, 0.2)$  [1] 0.1328756

iii)  $>\text{dbinom}(4, 12, 0.2)$  [1] 0.927445

Solve  
③  $\rightarrow$  dbinom  
[1] 0

(iii)  $> 1 - \text{pbinom}(5, 12, 0.2)$   
[2] 0.01940628

3)  $> \text{dbinom}(0.5, 5, 0.1)$   
[2] 0.59049 0.3808 0.07290  
0.00810 0.00048 0.00001

4)  $> \text{dbinom}(5, 12, 0.25)$   
[2] 0.1032414

(2)  $> \text{pbinom}(5, 12, 0.25)$   
[2] 0.9455928

(3)  $> 1 - \text{pbinom}(7, 12, 0.25)$   
[2] 0.00278151

(4)  $> \text{dbinom}(6, 12, 0.25)$   
[2] 0.04014945

- ⑤ the probability of a sales man making sell to a customer out of 10 customers.
- ① No. sale out of 10 customers.
  - ② More than 3 sale out of 20 customers.

- ⑥ A salesman of 20% of 30 customers, what minimum no. sale he can make
- ⑦ X follows binomial dist. with  $n=10$ ,  $p=0.3$ , plot the graph of

Solu

(i) > dbinom(0, 10, 0.15)

[1] 0.1968744

(ii) > 1 - pbinom(3, 20, 0.15)

[1] 0.3522748

Q.6 > qbinom(0.88, 30, 0.2)

[1] 9

~~>~~ n = 10

> p = 0.3

> n = 0:n

> prob = dbinom(n, n, p)

> cumprob = pbinom(n, n, p)

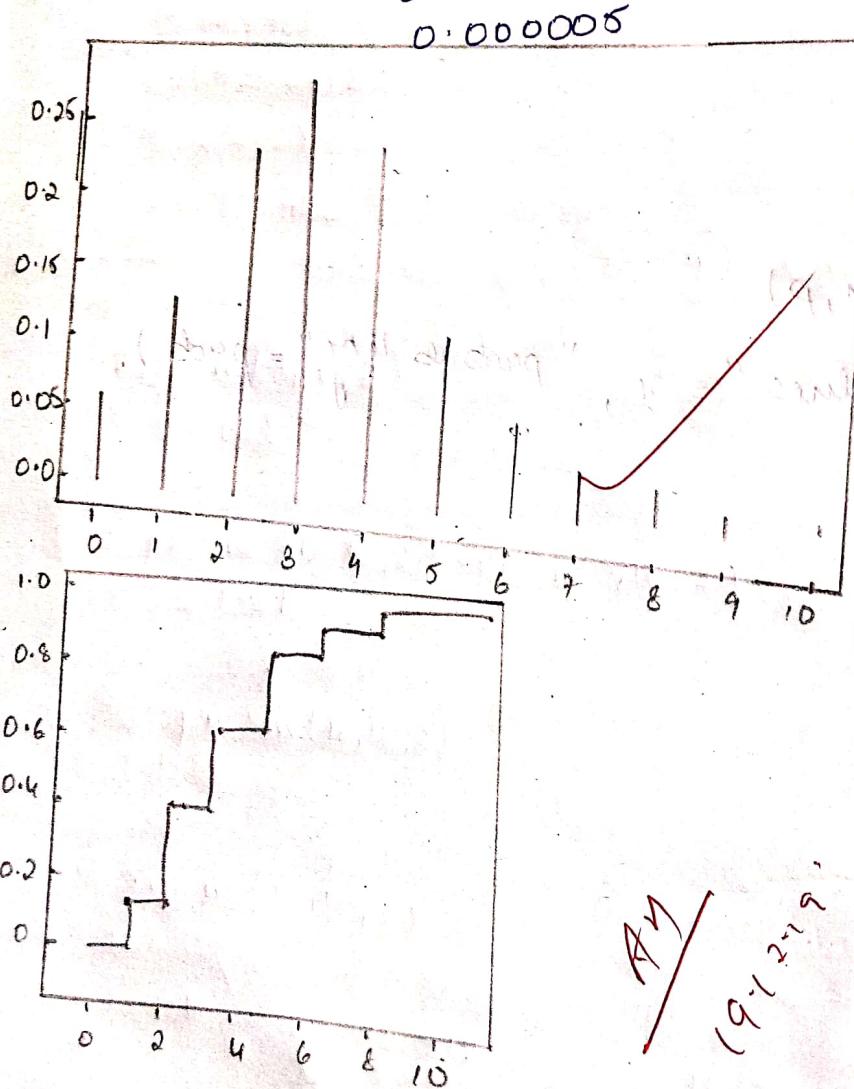
> d = data frame("n values" = n, "probability" = prob)

> print(d)

> plot(n, prob, "h")

> plot(n, cumprob, "s")

$n$ -values	S.E.D.	probability.
1	0	0.0282
2	1	0.1210
3	2	0.2334
4	3	0.2668
5	4	0.2001
6	5	0.1029
7	6	0.367
8	7	0.009
9	8	0.001
10	9	0.0001
11	10	0.000005



RD  
19.2.2

: Practical No. 4:Normal Distribution

\* Formulas:-

$$P(x=n) = dnorm(n, \mu, 5)$$

$$P(x \leq n) = pnorm(n, \mu, 5)$$

$$P(x > n) = 1 - pnorm(n, \mu, 5)$$

To generate random no. & code  $\rightarrow \text{rnorm}(n, \mu, 5)$

Q A random variable  $x$  follows normal distribution with mean

$\mu = 12$ ,  $S.D = \sigma = 3$  : find (i)  $P(x \leq 15)$  (ii)  $P(10 \leq x \leq 13)$

(iii)  $P(x > 14)$  (iv)  $P(x > 14)$  (v) generate 5 obs (rand. no.)

$$> p1 = pnorm(15, 12, 3)$$

$$> p1$$

$$> 0.8413447$$

$$> p2 = pnorm(13, 12, 3) - pnorm(10, 12, 3)$$

$$> p2$$

$$> 0.3780661$$

8.80

>  $p_B = 1 - \text{pnorm}(14, 12, 3)$

>  $p_B$

> 0.2524925

> rnorm(5, 12, 3)

[1] 8.825718 13.798846 11.05 8.683 15.467502

2. X follows ND with  $\mu=10$ ,  $\sigma=2$ ; find:

(i)  $P(x \leq 7)$

$P(5 \leq x \leq 12)$

$P(x > 12)$

gen 10 obs

(v) Find  $k$  such that  $P(x < k) = 0.4$

> rnorm(7, 10, 2)

> 0.1668

>  $\text{pnorm}(12, 10, 2) - \text{pnorm}(5, 10, 2)$   
0.8851361

>  $1 - \text{pnorm}(12, 10, 2)$   
0.1586

> rnorm(10, 10, 2)

10.805

11.288

13.06

11.512

8.444

11.65

8.047

6.38

13.01

11.02

? qnorm(0.4, 10, 2)  
9.493306

③ Generate 5 random no. from ND with  $\mu=15$ ,  $\sigma^2=4$  034  
Find Sample mean, median, SD & print it.

- ①  $x$  follows normal i.e.  $N(\mu, \sigma^2)$   $\mu=30$ ,  $\sigma^2=10$ . Find  
②  $P(x \leq 40)$  ③  $P(x \geq 35)$  ④  $P(25 \leq x \leq 35)$   
⑤ Find  $x$  such that  $P(x \leq x) = 0.6$

⑥ code :-

`y=rnorm(40,30,10)`

0.841

`> 1-pnorm(35,30,10)`

0.3065

`> pnorm(35,30,10) - pnorm(25,30,10)`

0.3829

`>qnorm(0.6,30,10)`

32.83397

⑦ Code:-

`n=rnorm(5,15,4)`

`n`

14.295 16.433 14.205 19.932 11.389

`am=mean(n)`

am

15.309

`me=median(n)`

me

14.2984

180:

> n = 5  
> variance =  $(n-1) \times \text{var}(x)/n$

> variance

[1] 6.967

> sd = sqrt(variance)

> sd

[1] 2.63929

> cat("8M", am)

[1] 15.30922

> cat("8M", me)

SM 14.29548

> cat("SD", sd)

SD 2.639

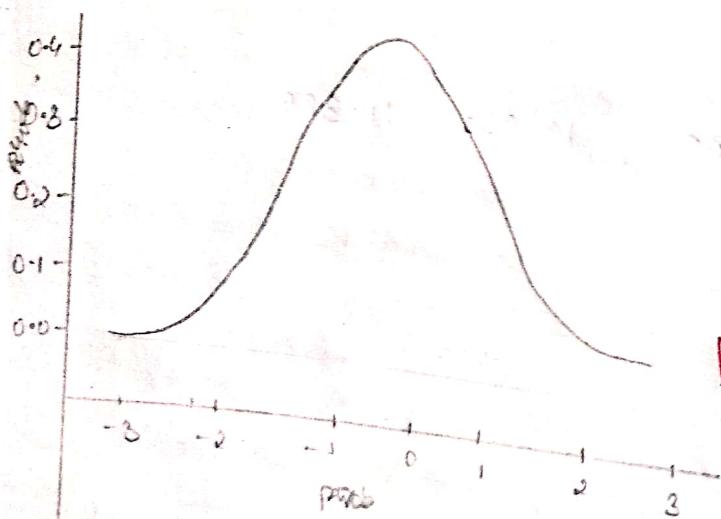
⑤ Plot standard normal graph

> n = seq(-3, 3, by = 0.1)

> y = dnorm(n)

> plot(x, y, xlab = "x", ylab = "prob", main = "sd")

sd



## Practical 5:

## Normal Q-Q-Test:

- For the hypothesis  $H_0: \mu = 15$  against  $H_1: \mu \neq 15$ . Random sample of size 400, is drawn, and the calculated the sample mean  $\bar{x} = 14$ , std dev is 3, test the hypothesis at 5% level of significance formula: `</code>`

$$\left[ z = \frac{\bar{x} - \mu_0}{\frac{\sigma}{\sqrt{n}}} \right] \quad \begin{aligned} &> \mu_0 = 15; \bar{x}_n = 14; \sigma = 3; n = 400 \\ &> z_{\text{cal}} = (\bar{x}_n - \mu_0) / (\sigma / \sqrt{n}) \end{aligned}$$

>  $z_{\text{cal}}$ 

[2] = 6.666

> cat ("calc value at alpha = ",  $z_{\text{cal}}$ )> calc value at  $\alpha = 2 = -6.666667$ 

~~if pvalue < 0.05  
then np = wrong.~~

~~> pvalue = 2 \* (1 - pnorm(abs(zcal)))~~

~~if pvalue > 0.05  
then np = right.~~

~~[2] 2.616796e-11~~
~~</code>~~

Ans: Since pvalue  $\neq 0.5$ , we accept  $H_0: \mu = 15$ .

- For the  $H_0: \mu = 10$  against  $H_1: \mu \neq 10$ , random sample of size 400, with sample mean 10.2, std dev 2.25, test the hypothesis at 5% level of significance.

$$</code> \quad \begin{aligned} &> \mu_0 = 10, \bar{x}_n = 10.2, \sigma = 2.25, n = 400 \end{aligned}$$

$$> z_{\text{cal}} = (\bar{x}_n - \mu_0) / (\sigma / \sqrt{n})$$

$$> pvalue = 2 * (1 - pnorm(abs(zcal)))$$

&gt; pvalue

[2] 0.075

&lt;/code&gt;

Ans: Since pvalue  $> 0.5$ , we accept  $H_0: \mu = 10$

Ex 80.

1. Test the sample

3. Test the hypothesis  $H_0: \mu = 0.2$ . Proportion of oranges in a bag is 0.2, a sample of 100 collected & the sample proportion is calculated as 0.125 test the hypo at 5% level of significance, sample size = 400.

$$\rightarrow n = 400, H_0: \mu = 0.2; P = D \cdot 125; Q = 1 - P$$

$$\rightarrow z_{\text{cal}} = (p - P) / \sqrt{P(1 - P)/n}$$

$$[1] = 3.75$$

$$\rightarrow p\text{value} = (2 * (1 - \text{norm}(abs(z_{\text{cal}}))))$$

$$\rightarrow p\text{value}$$

$$[2] = 0.00017$$

Ans: Since  $p\text{value} < 0.05$ , we do not accept  $H_0: \mu = 0.2$

Ans:

4. Last year, the farmer took 200, a random sample = 60 fields are collected and it is found that 9 fields were polluted, test hypothesis at 1% level of significance.

$$\rightarrow P = 0.2, p = 9/60, n = 60, Q = 1 - P$$

$$\rightarrow z_{\text{cal}} = ((p - P) / \sqrt{P(1 - P)/n})$$

$$\rightarrow p\text{value} = (2 * (1 - \text{norm}(abs(z_{\text{cal}}))))$$

$$\rightarrow p\text{value}$$

$$[2] = 0.3329$$

Ans: Since  $p\text{value} > 0.01$ , we do not accept  $H_0: 200$ .

036

Q. Test the hypothesis  $H_0: \mu = 12.5$ , from the following sample at 5% level of significance if the sample  $\text{diff} > 30 - \text{real}$ .  
 $\text{c}(\text{12.25}, 11.97, 12.15, 12.04, 12.31, 12.28, 11.94, 11.89, 12.16, 12.04)$

$$\rightarrow n = \text{length}(n)$$

$$\rightarrow m_n = \text{mean}(n)$$

$$\rightarrow \text{variance} = ((n-1) * \text{var}(n)) / n$$

$$\rightarrow s_d = \sqrt{\text{variance}}$$

$$\rightarrow m_0 = 12.5$$

$$\rightarrow t = (m_n - m_0) / (s_d / \sqrt{n})$$

$$\rightarrow \text{pvalue} = 1 - \text{pnorm}(\text{abs}(t))$$

$\rightarrow 0$

Ans:

$$\cancel{\begin{array}{l} \text{AM} \\ 16.170 \end{array}}$$

## Practical 6:

## Testing Proportion

- ① Let the population mean (the amount spent per customer in a restaurant) is 250. A sample of 100 customers selected. The sample mean is calculated as 275 & SD 30, test the hypothesis that the population mean is 250 or not at 5% level of significance.
- ② In a random sample of 1000 students, 879 is found that 750 use blue pen, test the hypothesis that the population proportion is 0.8 at 1% level of significance.

$$\text{① } \mu_x = 275, \mu_0 = 250, \text{ sd} = 30, n = 100$$

$$\Rightarrow z_{\text{cal}} = (\mu_x - \mu_0) / (\text{sd} / \sqrt{n})$$

$$\Rightarrow z_{\text{cal}}$$

$$8.333$$

$\downarrow \text{abs}(z_{\text{cal}})$

$$\Rightarrow p\text{value} = 2 * (1 - \text{pnorm}(z_{\text{cal}}))$$

Since, less than 0.5%, we do not accept.

$$\text{② } P = 0.8; Q = 1 - P; p = 750/1000; n = 1000$$

$$\Rightarrow z_{\text{cal}} = (p - P) / \sqrt{P(1-P)/n}$$

$$= 3.952847$$

$$\Rightarrow p\text{value} = 2 * (1 - \text{pnorm}(z_{\text{cal}}))$$

$$= 7.72268 < 0.05$$

Ans. since  $< 0.01$  we do not accept.

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- (3) Two random samples of size 1000 & 2000 are drawn from a population with the same standard deviation 2.5, the sample mean are 67.5 & 68.0 resp, test the hypothesis  $H_0: \mu_1 = \mu_2$  at 5% level of significance.

- (4) A study of noise level in 2 hospitals is given below, test the claim that the 2 hospitals have same level of noise at 1% level of significance.

- (5) In a sample of 600 students in a college, 400 use blue ink, in another college from a sample of 900 students 450 use blue ink, test the hypothesis that the proportion of students using blue ink in 2 colleges are equal or not at 1% level of significance.

Sol:

$$(3) n_1 = 1000; n_2 = 2000; \bar{x}_1 = 67.5; \bar{x}_2 = 68.0; s_d = 2.5$$
$$z_{\text{cal}} = (\bar{x}_1 - \bar{x}_2) / \sqrt{(s_d^2 / n_1) + (s_d^2 / n_2)}$$
$$\text{car}("z_{\text{cal}}:", z_{\text{cal}})$$
$$z_{\text{cal}} = -5.163978$$
$$\text{pvalue} [2 * (1 - pnorm(\text{abs}(z_{\text{cal}})))]$$
$$> 2.417564e-07.$$

We do not agree  $< 0.05$ .

(4) H0:  $\mu_1 = \mu_2$   
H1:  $\mu_1 \neq \mu_2$   
mean  $\bar{x}_1 = 61.2$   
 $\bar{x}_2 = 7.9$   
 $n_1 = 84; n_2 = 84$   
 $z_{\text{cal}} = 1.001$   
 $|z_{\text{cal}}| = 1.160943$   
 $p_{\text{val}} = 1.2 \times 10^{-5}$   
 $p_{\text{val}} = 0.2423$   
Since  $> 0.1$ , we  
 $n_1 = 600; n_2 = 600$   
 $P = 1 - p$   
 $q = 1 - p$   
 $z_{\text{cal}} = 1.01$   
 $|z_{\text{cal}}| = 0.01772$   
 $6.381534$   
 $p_{\text{val}} = 1.2 \times 10^{-5}$   
 $1.753222$   
Since  $< 0.5$ ; we

	HDS A	HDS B
nsize	84	34
mean	61.2	59.4
s.d.	7.9	7.5

038

>  $n_1 = 84$ ;  $n_2 = 34$ ;  $m_{n1} = 61.2$ ;  $m_{n2} = 59.4$ ;  $s_{d1} = 7.9$ ;  $s_{d2} = 7.5$   
 $\chi_{\text{cal}} = (m_{n1} - m_{n2}) / \sqrt{(s_{d1}^2/n_1) + (s_{d2}^2/n_2)}$

>  $\chi_{\text{cal}}$   
 $\approx 1.160943$

>  $p_{\text{val}} = 2 * (1 - \text{pnorm}(\text{abs}(\chi_{\text{cal}})))$

>  $p_{\text{val}}$

> 0.2423

> since > 0.1, we accept.

⑤  $n_1 = 600$ ;  $n_2 = 900$ ;  $p_1 = 400/600$ ;  $p_2 = 450/900$ ;

$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

$q = 1 - p$

$\chi_{\text{cal}} = (p_1 - p_2) / \sqrt{(p * q) / ((1/n_1 + 1/n_2))}$  ← mult.

> ~~0.01772648~~

> 6.381534

>  $p_{\text{val}} = 2 * (1 - \text{pnorm}(\text{abs}(\chi_{\text{cal}})))$

>  $p_{\text{val}}$

> 1.753222e-10

& since < 0.5; we do not accept.

⑥

For sample sizes,  
 $n_1 = 200$ ;  $n_2 = 200$ ;  
 $p_1 = 44/200$ ;  $p_2 = 30/200$ ; test 5% level of significance;

Soln

$$n_1 = 200; n_2 = 200; p_1 = 44/200; p_2 = 30/200$$

$$z_{\text{cal}} = (p_1 - p_2) / \sqrt{(p_1(1-p_1) * (1/n_1 + 1/n_2))}$$

$$z_{\text{cal}}$$

$$[1] 1.802748$$

$$p_{\text{val}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$[1] 0.1577646$$

Since  $> 0.5$ ; we do not accept:

AN  
27-01-20

①

The marks  
68, 69, 70,  
comp commun  
 $n_0 \cdot n = 66$   
 $n = c$   
 $t \cdot t_{\text{test}}$

data = x

t = 68.319,  
alternate hypothesis  
95% confidence

68.65171  
Sample size  
mean of

67.75

As 1.55  
 $p_{\text{value}} =$   
 $> 1$  if  $(p_{\text{value}} < \alpha)$   
reject  $H_0$

③

2 groups  
the hypothesis

$G_1 = 1.8$

$G_2 = 1.6$

$n_0 = n_0$

$n = c$

$\gamma_1 = c$

Practical 7:

## Small Sample Test

1. The marks of 10 students are given by 63, 66, 67, 63, 68, 69, 70, 70, 71, 72. Test the hypothesis that sample comes from population that has average 66.

$$H_0: \mu = 66$$

$$> n = c(\dots \text{data} \dots)$$

$$> t.tst(x)$$

One sample t-test

data: x

$$t = 68.319, df = 9, p\text{-value} = 1.558e^{-13}$$

alternative hyp: mean is not equal to 0

95% confidence interval:

$$65.65171 \text{ to } 70.14829$$

Sample estimate

mean of x

$$67.9$$

As  $1.558e^{-13} < 0.05$ , we reject  $H_0$

$\text{pvalue} = 1.558e^{-13}$

$\text{if } (\text{pvalue} > 0.05) \text{ print ("accepts") } \text{ else print ("rejects")}$

reject

- 2 groups of students scored the following marks. Test the hypothesis that there is no significant difference b/w 2 groups.

$$> G1 = 18, 22, 12, 10, 17, 20, 17, 23, 20, 22, 21, 11$$

$$> G2 = 16, 20, 14, 21, 20, 18, 13, 15, 12, 21$$

$H_0 \rightarrow$  no difference in b/w groups.

$$> n = c(G1)$$

$$> m = c(G2)$$

8.80

> t-test (x, y)  
with two sample t-test

data: x & y  
 $t = 2.2573$ ,  $p\text{value} = 0.03798$   
alternative hyp: true difference in mean is  $\neq 0$   
conf. interval:

0.1628205 5.0371795

### Sample Estimate

mean of x mean of y

> pvalue = 0.03798

> if ( $p\text{value} > 0.05$ ) {

> Reject H<sub>0</sub>.

8. The Balus data of 6 shops before & after a special campaign given below:

Before - 53, 28, 31, 48, 50, 42

After - 58, 29, 30, 55, 56, 45

Test the hypothesis that campaign is effective or not, H<sub>0</sub>: no significant diff.

n = c (Before)

y = c (After)

t-test (x, y)

Paired t-test;

data: x & y.

t = -2.3815

Alt. Hypo

95% conf

-6.05

Sample

> pvalue = 0

> if ( $p\text{value}$

> Accept -

) Two means respectively

AP 1 → 10, 1

AP 2 → 8, 9

) There are

joll all

I am. adi

ou = 120

u = 100

= c (Before)

c (After)

ttest (x, y)

value = 0.4

(pvalue >

> Accept H

$t = 2.3815$ ,  $df = 5$ ,  $p\text{value} = 0.9806$ . 040  
 Alt. Hypo : true diff. in mean > than 0.  $\Rightarrow H_1$   
 95% confidence interval: (-6.0254, 4.71)  $\Rightarrow p <$   
 $-6.0254 \in$  In f.P. : R code, p < 0.05  
 Sample Estimer.  
 $\Rightarrow p\text{value} = 0.9806$ .  
 $\{$  if ( $p\text{value} > 0.05$ ) { cat ("accept") } else { cat ("reject") }  $\}$ .  
 $\Rightarrow \text{Accept}$ .

④ Two medicines are applied to 2 groups of patient respectively

$H_0 \rightarrow$   
 Gp1  $\rightarrow 10, 12, 13, 11, 14$   
 Gp2  $\rightarrow 8, 9, 12, 14, 15, 10, 9$ .

Is there any diff. b/w 2 elements?

⑤ foll are weight before & After. a diet pg.  
 wI estm. adiff?

~~Before~~ = 120, 125, 115, 130, 123, 119

After = 100, 114, 95, 90, 115, 99

$H_0 \rightarrow$  No difference b/w 2 groups.

$x = c(\text{Before})$

$y = c(\text{After})$

to t.test(x, y)

$p\text{value} = 0.4406$

$\{$  if ( $p\text{value} > 0.05$ ) { cat ("A") } else { cat ("R") }  $\}$

$\Rightarrow \text{Accept } H_0$ .

Ansver  $\text{H}_0: \mu_1 = \mu_2$   $H_0 \rightarrow \text{No difference b/w Before & After}$

⑤  $x_1 = [120, 125, 115, 130, 123, 119]$   
 $x_2 = [100, 114, 95, 90, 115, 99]$

& t-test ( $x_1, x_2$ , paired) :  $T$ , alternative = "less"

& p-value = 0.0963

& if (pvalue > 0.05) { cat ("accept") } else { cat ("reject") }

Accept  $H_0$ .

## FYCS Practical 8

### Large and Small Sample tests

Q.1 The arithmetic mean of a sample of 100 items from a large population is 52. If the standard is 7, test the hypothesis that the population mean is 55 against the alternative it is more than 55 at 5% LOS.

Q.2 In a big city 350 out of 700 males are found to be smokers. Does the information supports that exactly half of the males in the city are smokers? Test at 1% LOS.

Q.3 Thousand article from a factory A are found to have 2% defectives, 1500 articles from a 2nd factory B are found to have 1% defective. Test at 5% LOS that the two factory are similar or not.

Q.4. A sample of size 400 was drawn at a sample mean is 99. Test at 5% LOS that the sample comes from a population with mean 100 and variance 64.

Q.5. The flower stems are selected and the heights are found to be (cm) 63, 63, 68, 69, 71, 71, 72 test the hypothesis that the mean height is 66 or not at 1% LOS.

Q.6. Two random samples were drawn from 2 normal populations and their values are A- 66, 67, 75, 76, 82, 84, 88, 90, 92 B- 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97. Test whether the populations have the same variance at 5% LOS.

7. A company producing light bulbs finds that mean life span of the population of bulbs is 1200 hours with s.d. 125. A sample of 100 bulbs have mean 1150 hours. Test whether the difference between population and sample mean is significantly different?

8. From each of two consignments of apples, a sample of size 200 is drawn and number of bad apples are counted. Test whether the proportion of rotten apples in two assignments are significantly different at 1% LOS?

	Sample size	No. of bad apples
Consignment 1	200	44
Consignment 2	300	56

Answe

$H_0$ :

$$Q_1. \quad n = 100$$

$$mn = 52$$

$$mw = 55$$

$$sd = 7$$

$$z_{\text{cal}} = (mn - mw) / (sd / \sqrt{n})$$

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$z_{\text{cal}} = -4.285714$$

$$p\text{value} = 1.82153e-05$$

042

$$(H_0: \mu = 55) \quad (H_1: \mu < 55) \quad \text{Left-tailed}$$

Ans: Since less than 0.05, we don't accept  $H_0$

$$Q_2. \quad H_0: P = 0.5 \quad (350/700)$$

$$H_1: P \neq 0.5$$

$$P = 0.5$$

$$p = 350/700$$

$$n = 700$$

$$z_{\text{cal}} = (p - P) / \sqrt{P(1-P)/n}$$

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$z_{\text{cal}} = 0$$

$$p\text{val} = 1$$

Ans: Since  $> 0.01$ , we accept  $H_0$

$$Q_3. \quad H_0: P_1 = P_2$$

$$H_1: P_1 \neq P_2$$

$$n_1 = 1000$$

$$n_2 = 1500$$

$$P_1 = 0.02$$

$$P_2 = 0.01$$

$$p = (n_1 + P_1 + n_2 + P_2) / (n_1 + n_2)$$

$$q = 1 - p$$

$$\chi_{\text{cal}}^2 = \frac{(p_1 - p_2)^2}{(p_1 + p_2)} \left[ \frac{1}{n_1} + \frac{1}{n_2} \right]$$

pvalue =  $2 + (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

$z_{\text{cal}} = 2.084842$   
 $\text{pvalue} = 0.03708364$

Since  $< 0.05$ , we do not accept  $H_0$

Q4.  $H_0: \mu = 99$      $H_1: \mu = 100$

$n = 400$

$m_n = 100$

$m_0 = 99$

$s_n = 64$

$s_d = \sqrt{s_n^2 + s_0^2}$

$$\chi_{\text{cal}}^2 = (m_n - m_0) / (s_d / \sqrt{n})$$

pvalue =  $2 + (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

$z_{\text{cal}} = 2.5$

pvalue = 0.01241433

Since  $< 0.05$ , we do not accept  $H_0$

Q5.  $H_0: \mu = 66$      $H_1: \mu \neq 66$

$n = c(63, 63, 68, 69, 72, 71, 72)$

t-test(n)

pvalue =  $5.522 \times 10^{-9}$

### One Sample t-test

data: n

t = 47.94, df = 6, pvalue =  $5.522 \times 10^{-9}$

alt.hypo: true mean != 0  
 95% confidence interval:

64.66479

mean of x

68.14286

$$Q3. H_0: \mu = 1200$$

$$H_1: \mu \neq 1200$$

$$n=100$$

$$\bar{m} = 1150$$

$$SD = 1200$$

$$SD = 125$$

$$Z_{\text{cal}} = (\bar{m} - \mu_0) / (SD / \sqrt{n})$$

$$P\text{value} = 2 * (1 - \text{pnorm}(|Z_{\text{cal}}|))$$

$$Z_{\text{cal}} = -4$$

$$\text{Pvalue} = 2 * 3.34248e-05 \approx 0.000334248$$

Since  $10.05 > 0.05$ , we do not accept  $H_0$  at 0.05.

$$Q4. H_0: \sigma^2 =$$

$$n = c(66, 67, 75, 76, 82, 88, 84, 90, 92)$$

$$y = c(64, 66, 74, 78, 82, 80, 87, 92, 95, 93, 97)$$

var.t.test(n, y)

F test to compare 2 variance

data: n & y

F = 0.70686, num df = 8, denom df = 10,

Pvalue = 0.6359

alt hypo: true ratio of variance is != 1

95% confidence int:

0.183622 3.0360393

Sample estimate

ratio of variance

0.7068567

Since  $> 0.05$ , we accept  $H_0$

① Use the  
the ho  
not.  
Condition  
Clean

Q8.

Consignment 1

Sample 200

badapple 44

$$H_0: \mu = P_1 = P_2$$

Consignment 2.

300

56

$$H_1: \mu \neq P_1 \neq P_2$$

$$\rightarrow n_1 = 200$$

$$n_2 = 300$$

$$P_1 = 44/200$$

$$P_2 = 56/300$$

$$P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$$

$$q = 1 - P$$

$$Z_{\text{cal}} = ((P_1 - P_2) / (\text{sqrt}((P_1 * q) / (n_1 + n_2))))$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(Z_{\text{cal}})))$$

$$Z_{\text{cal}} = 0.9128709$$

$$\text{pvalue} = 0.3613104$$

Since  $> 0.01$ , we accept  $H_0$ .

AM  
(7-25)

## Chi-Square Tests & ANOVA

041

- ① Use the following data to test whether the condition of the home & the condition of child are independent or not.

Condition of Home

Clean      Dirty

70	50
80	20
35	45

clean      }  
Fairly clean      } condition of child.  
Dirty.

Sol:

$H_0$ : Condition of home & child are independent

$H_1 \neq$

$n = \text{scan}(70, 80, 35, 50, 20, 45)$

$m = 3$

$n = 2$

$y = \text{matrix}(n, \text{ncol} = m, \text{nrow} = n)$

$\text{chisq.test}(y)$

Pearson's chi-squared test

data = y

$\chi^2 = 25.646$ , df = 2, P-value =  $2.698e-06$

Since p-value  $< 0.01$ , we don't accept  $H_0$ .

7 110  
H<sub>0</sub>: that vaccination & disease are independent  
or not

Vaccine

A II	Not A II	All
70	46	
35	37	

All Disease  
Not All

H<sub>0</sub>: vaccination & disease are independent  
 $n = c(70, 35, 46, 37)$

$$m = 2$$

$$n = 2$$

y = matrix(x, nrow=m, ncol=n)

chi.sq.test(y).

Pearson's chi-sq with Yates' cont. corr.

$$\text{data} = y$$

$$\text{chisq} = 2.0275, \text{df} = 1, \text{pvalue} = 0.1545$$

Since  $> 0.01$ , we accept H<sub>0</sub>.

III Perform a ANOVA

ANOVA > Analysis of Variance for the following data.

Type  
A  
B  
C  
D

Soln:

$n_1$   
 $n_2$   
 $n_3$

$n_4$

[1]

One

Type	Observations-
A	50, 52,
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

Soln: Means are  $\bar{x}$  for A, B, C, D

$$\bar{x}_1 = \frac{1}{2}(50, 52)$$

$$\bar{x}_2 = \frac{1}{3}(53, 55, 53)$$

$$\bar{x}_3 = \frac{1}{4}(60, 58, 57, 56)$$

$$\bar{x}_4 = \frac{1}{4}(52, 54, 54, 55)$$

$$d = \text{stack}(\bar{x}_1, \bar{x}_2, \bar{x}_3, \bar{x}_4)$$

names(d)

[1] "values" "ind"

50	{	b1	
52	}		
53	{	b2	
55	}		
53	{		
60	{	b3	
58	}		
57	{		
66	{		
52	{	b4	
54	}		
54	{		
55	}		

One way t-test P values in R output, data=d1, var.equal=T )

One way +

0

p value

Ans; Since

Read f

statistics

40

45

42

15

37

38

59

20

27

36

### One way analysis of means

data: values & End.

$F = 11.735$ , num df = 3, denom df = 9, pvalue = 0.001

> anova = aov (values ~ Ind, data = d)

> summary(anova)

	Df	Sum Sq	Mean Sq	F-value	P(F)
Ind	3	71.06	23.688	11.73	0.001
Residuals	9	18.17	2.019		

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '' 0.1 ' ' 1

And since  $<0.001$ , we reject  $H_0$ .

Following data gives the life of tires of 14 brands

Type	Life
A	20, 23, 18, 22, 24, 19.
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20
D	15, 14, 16, 18, 14, 16.

$H_0$ : Average life of ABCD are equal

> n1 = c (data "A")

> n2 = c (data "B")

> n3 = c (data "C")

> n4 = c (data "D")

> d = stack (list (b1 = n1, b2 = n2, b3 = n3, b4 = n4))

~ oneway.tet (values ~ pd, data = d, var.equal = T)  
045

One-way analysis of means -

pvalue = 0.001719.

Now, since < 0.01, we reject H<sub>0</sub>.

Read from cov.

statistic	maths
40	60
45	68
42	47
15	20
37	25
38	27
59	57
20	58
27	25
36	27

%load %/maths.csv  
> n = read.csv ("location")  
> am = mean(x\$statistic)  
> <sup>35.9</sup> am = mean(n\$maths)  
39.4  
> sd = ((n-1) \* var(x\$statistic)) / n  
> 12.32234  
> Sd = ((n-1) \* var(x\$maths)) / n  
> 15.2  
> n = length(x\$statistic)  
> 10  
> n = length(x\$maths)  
> cor(x\$statistic, x\$maths)  
> 0.4435442  
> oneway.tet (values ~ pd, data = d,  
var.equal = T)

~~AN  
20.470~~  
> anova = aov (values ~ pd, data = d)  
> summary (anova)

## Practical 10:

## Non Parametric Test:

Following are the amounts of Sulphur dioxide emitted by a factory in 20 days. Apply a sign test to test the hypothesis that the population median is 21.5 at 5% LOS.

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 28, 24, 26

$H_0$ :

population median = 21.5

$n = 20$

$m_e = 21.5$

$sp = \text{length}(\{n | n > m_e\})$

$sn = \text{length}(\{n | n < m_e\})$

$n = sp + sn$

$pV = \text{pbinom}(sp, n, 0.5)$

$0.4119015$

Since  $H_0 > 0.05$ , we accept  $H_0$ .

- Q. If  $H_0$  :  $m_c \neq m_L$  =  $PV = p_{binom}$   
 $(sp, n, 0.5)$
- Q. else  $pV = p_{binom}(sn, n, 0.5)$
- Following Q. the data of 10 observation  
apply sing test to test  $H_0$  that  
the population median  $625$  against  
alternative  $> 625$

612, 619, 631, 628, 643, 640, 655  
649, 6870, 663.

No : population median.  $625$   $H_1 : m_c > 625$

$n = c(\dots)$  (Excl. 1 of 10) = 9

$m_c = 625$

$sp = \text{length}([n > m_c])$

$sn = \text{length}([n < m_c])$

$n = sp + sn$

$PV = p_{binom}(sn, n, 0.5)$

$PV$

0.054

Since  $> 0.05$ , we accept  $H_0$ .

Q. The following are, for the hypothesis  
the population median = 60 against alt  $> 60$   
at 5% LOS using Wilcoxon Signed Rank Test.

68, 65, 60, 89, 61, 71, 58, 61, 69, 62, 63, 39, 72, 64,  
48, 66, 72, 63, 87, 69.

$H_0: \text{pop } \mu = 60$

$H_1: \dots > 60$

$n = 11$

wilcox.t test 1m, altu = "greater", mu = 60

Wilcoxon Rank sum test with cont. corr.

data: n & mu

w = 15.5, pvalue = 0.2037

alt hyp: true location shift  $> 0$

Since  $> 0.05$ , we accept  $H_0$ .

altu = "less" will have rejected  $H_0$

altu = "two.sided"

840

Q.  $\mu_m \leq 12$  or less than 12.

15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 21, 26

$n = c(\dots)$

wilcox.test (n, alt="less", me=12)

W=11.5, p-value = 0.9463

Since  $> 0.05$ , we accept  $H_0$

WB

65

75

75

62

72

WA

72

74

72

66

78

Q weights of students,

b1 A stopped smoking

using work, rest the

there is no signif

No: Before and After

#WPL(wx) there is no change

H<sub>1</sub>: there is change

$x = c(65, 75, 75, 62, 72)$

$y = c(72, 74, 72, 66, 78)$

$df = n - y$

$mu = 0$

> wilcox.test (d, alt = "two.sided", mu)

W = 2 , pvalue = 1

alt, hyp : true location shift  $\neq 0$

Since  $H_0 \rightarrow$  pvalue  $> 0.05$  , we accept  $H_0$ .

$$\begin{array}{c} \rightsquigarrow \\ \text{pvalue} \\ \cancel{< 0.05} \end{array}$$