

homework

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1 Ex 1

$$P(\text{positive}) = P(\text{positive}|\text{Hansen}) * P(\text{Hansen}) + P(\text{positive}|\text{noHansen}) * P(\text{noHansen})$$

=

$$0.98 * 0.05 + 0.03 * 0.95$$

=

$$P(\text{Hansen}|\text{positive}) = \frac{0.0775}{P(\text{positive})} = \frac{P(\text{positive}|\text{Hansen}) * P(\text{Hansen})}{P(\text{positive})}$$

=

$$\frac{0.98 * 0.05}{0.0775} \\ \approx 0.6323$$

2 Ex 2

suppose univariate normal distribution is normalized :

then $Z = \frac{X - \mu}{\sigma}$ ($Z \sim N(0,1)$)

$$+ E(Z) = E\left(\frac{X - \mu}{\sigma}\right) = \frac{1}{\sigma} E(X - \mu) = \frac{1}{\sigma} (E(X) - \mu) = 0$$

$$+ V(Z) = V\left(\frac{X - \mu}{\sigma}\right) = \frac{1}{\sigma^2} V(X - \mu) = 1$$