# **Project 1: Trading with Momentum**

## Instructions

Each problem consists of a function to implement and instructions on how to implement the function. The parts of the function that need to be implemented are marked with a # TODO comment. After implementing the function, run the cell to test it against the unit tests we've provided. For each problem, we provide one or more unit tests from our project\_tests package. These unit tests won't tell you if your answer is correct, but will warn you of any major errors. Your code will be checked for the correct solution when you submit it to Udacity.

# **Packages**

When you implement the functions, you'll only need to you use the packages you've used in the classroom, like <a href="Pandas (https://pandas.pydata.org/">Pandas (https://pandas.pydata.org/</a>) and <a href="Pandas (https://pandas.pydata.org/">Numpy (http://www.numpy.org/</a>). These packages will be imported for you. We recommend you don't add any import statements, otherwise the grader might not be able to run your code.

The other packages that we're importing are helper, project\_helper, and project\_tests. These are custom packages built to help you solve the problems. The helper and project\_helper module contains utility functions and graph functions. The project\_tests contains the unit tests for all the problems.

#### **Install Packages**

```
In [1]: import sys
    !{sys.executable} -m pip install -r requirements.txt
```

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Requirement already satisfied: colour==0.1.5 in /opt/conda/lib/python3.6/site-packages (from -r requirements.
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d347bcf8308/tqdm-4.19.5-py2.py3-none-any.whl (51kB)
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2.18.4->-r requirements.txt (line 10)) (2019.11.28)
Requirement already satisfied: future in /opt/conda/lib/python3.6/site-packages (from osqp->cvxpy==1.0.3->-r
requirements.txt (line 2)) (0.16.0)
Collecting dill>=0.3.1 (from multiprocess->cvxpy==1.0.3->-r requirements.txt (line 2))
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630985e547d/dill-0.3.1.1.tar.gz (151kB)
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otly==2.2.3->-r requirements.txt (line 6)) (4.4.0)
Building wheels for collected packages: cvxpy, plotly, scs, multiprocess, dill
  Running setup.py bdist wheel for cvxpy ... done
  Stored in directory: /root/.cache/pip/wheels/2b/60/0b/0c2596528665e21d698d6f84a3406c52044c7b4ca6ac737cf3
  Running setup.py bdist wheel for plotly ... done
  Stored in directory: /root/.cache/pip/wheels/98/54/81/dd92d5b0858fac680cd7bdb8800eb26c001dd9f5dc8b1bc0ba
  Running setup.py bdist wheel for scs ... done
  Stored in directory: /root/.cache/pip/wheels/68/3f/24/e9c75d426f600634cdac68321184ba06fdc4ab2d189b5c4541
  Running setup.py bdist wheel for multiprocess ... done
  Stored in directory: /root/.cache/pip/wheels/96/20/ac/9f1d164f7d81787cd6f4401b1d05212807d021fbbbcc301b82
  Running setup.py bdist wheel for dill ... done
  Stored in directory: /root/.cache/pip/wheels/59/b1/91/f02e76c732915c4015ab4010f3015469866c1eb9b14058d8e7
Successfully built cvxpy plotly scs multiprocess dill
tensorflow 1.3.0 requires tensorflow-tensorboard<0.2.0,>=0.1.0, which is not installed.
moviepy 0.2.3.2 has requirement tqdm==4.11.2, but you'll have tqdm 4.19.5 which is incompatible.
Installing collected packages: numpy, scipy, osqp, ecos, scs, dill, multiprocess, cvxpy, pandas, plotly, tqdm
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  Found existing installation: pandas 0.23.3
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  Found existing installation: plotly 2.0.15
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 pandas-0.21.1 plotly-2.2.3 scipy-1.0.0 scs-2.1.1.post2 tqdm-4.19.5
```

#### **Load Packages**

```
In [29]: import matplotlib as plt

In [24]: %matplotlib inline

In [1]: import pandas as pd import numpy as np import helper import project_helper import project_tests
```

### **Market Data**

#### **Load Data**

The data we use for most of the projects is end of day data. This contains data for many stocks, but we'll be looking at stocks in the S&P 500. We also made things a little easier to run by narrowing down our range of time period instead of using all of the data.

#### **View Data**

Run the cell below to see what the data looks like for close.

```
In [8]: close.shape
Out[8]: (1009, 495)
```

In [20]: close.head()

Out[20]:

Α	AAL	AAP	AAPL	ABBV	ABC	ABT	ACN	ADBE	
29.99418563	16.17609308	81.13821681	53.10917319	34.92447839	50.86319750	31.42538772	64.69409505	46.23500000	39.91336
29.65013670	15.81983388	80.72207258	54.31224742	35.42807578	50.69676639	31.27288084	64.71204071	46.03000000	39.86057
29.70518453	16.12794994	81.23729877	54.61204262	35.44486235	50.93716689	30.72565028	65.21451912	46.42000000	40.18607
30.43456826	16.21460758	81.82188233	54.17338125	35.85613355	51.37173702	31.32670680	66.07591068	47.00000000	40.6523
30.52402098	16.31089385	82.95141667	53.86579916	36.66188936	52.03746147	31.76628544	66.82065546	46.62500000	40.2564
	29.99418563 29.65013670 29.70518453 30.43456826	29.99418563 16.17609308 29.65013670 15.81983388 29.70518453 16.12794994 30.43456826 16.21460758	29.99418563       16.17609308       81.13821681         29.65013670       15.81983388       80.72207258         29.70518453       16.12794994       81.23729877         30.43456826       16.21460758       81.82188233	29.99418563       16.17609308       81.13821681       53.10917319         29.65013670       15.81983388       80.72207258       54.31224742         29.70518453       16.12794994       81.23729877       54.61204262         30.43456826       16.21460758       81.82188233       54.17338125	29.99418563       16.17609308       81.13821681       53.10917319       34.92447839         29.65013670       15.81983388       80.72207258       54.31224742       35.42807578         29.70518453       16.12794994       81.23729877       54.61204262       35.44486235         30.43456826       16.21460758       81.82188233       54.17338125       35.85613355	29.99418563       16.17609308       81.13821681       53.10917319       34.92447839       50.86319750         29.65013670       15.81983388       80.72207258       54.31224742       35.42807578       50.69676639         29.70518453       16.12794994       81.23729877       54.61204262       35.44486235       50.93716689         30.43456826       16.21460758       81.82188233       54.17338125       35.85613355       51.37173702	29.99418563       16.17609308       81.13821681       53.10917319       34.92447839       50.86319750       31.42538772         29.65013670       15.81983388       80.72207258       54.31224742       35.42807578       50.69676639       31.27288084         29.70518453       16.12794994       81.23729877       54.61204262       35.44486235       50.93716689       30.72565028         30.43456826       16.21460758       81.82188233       54.17338125       35.85613355       51.37173702       31.32670680	29.99418563       16.17609308       81.13821681       53.10917319       34.92447839       50.86319750       31.42538772       64.69409505         29.65013670       15.81983388       80.72207258       54.31224742       35.42807578       50.69676639       31.27288084       64.71204071         29.70518453       16.12794994       81.23729877       54.61204262       35.44486235       50.93716689       30.72565028       65.21451912         30.43456826       16.21460758       81.82188233       54.17338125       35.85613355       51.37173702       31.32670680       66.07591068	29.99418563       16.17609308       81.13821681       53.10917319       34.92447839       50.86319750       31.42538772       64.69409505       46.23500000         29.65013670       15.81983388       80.72207258       54.31224742       35.42807578       50.69676639       31.27288084       64.71204071       46.03000000         29.70518453       16.12794994       81.23729877       54.61204262       35.44486235       50.93716689       30.72565028       65.21451912       46.42000000         30.43456826       16.21460758       81.82188233       54.17338125       35.85613355       51.37173702       31.32670680       66.07591068       47.00000000

5 rows × 495 columns

```
In [4]: project_helper.print_dataframe(close)
```

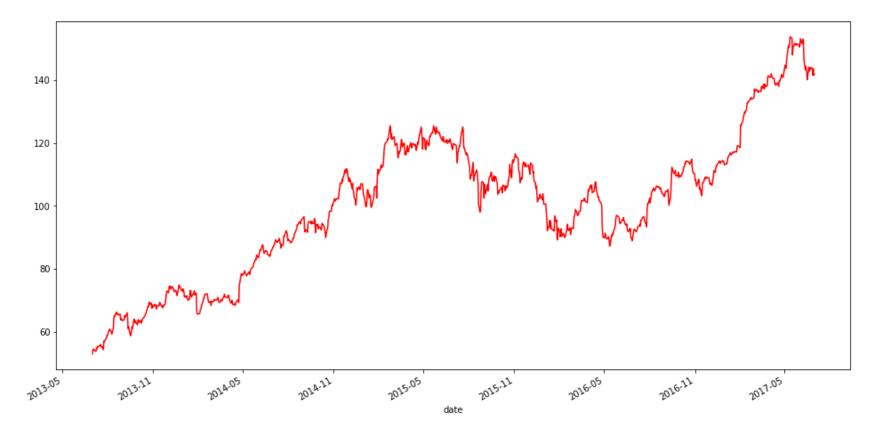
	А	AAL	AAP	
013-07-0	29.994	16.176	81.138	
013-07-0	29.650	15.820	80.722	
013-07-0	29.705	16.128	81.237	
013-07-0	30.435	16.215	81.822	
013-07-0	30.524	16.311	82.951	
013-07-0	30.689	16.715	82.436	
013-07-1	31.178	16.532	81.990	
013-07-1	31.460	16.725	82.000	
013-07-1	31.480	16.908	81.911	
013-07-1	31.728	17.100	82.615	

# **Stock Example**

Let's see what a single stock looks like from the closing prices. For this example and future display examples in this project, we'll use Apple's stock (AAPL). If we tried to graph all the stocks, it would be too much information.

In [32]: close['AAPL'].plot(figsize=(16,8),color='r')

Out[32]: <matplotlib.axes.\_subplots.AxesSubplot at 0x7f6a6922b5f8>



```
In [21]: apple_ticker = 'AAPL'
project_helper.plot_stock(close[apple_ticker], '{} Stock'.format(apple_ticker))
```

## **AAPL Stock**



# **Resample Adjusted Prices**

The trading signal you'll develop in this project does not need to be based on daily prices, for instance, you can use month-end prices to perform trading once a month. To do this, you must first resample the daily adjusted closing prices into monthly buckets, and select the last observation of each month.

Implement the resample prices to resample close prices at the sampling frequency of freq.

```
In [45]: def resample prices(close prices, freq='M'):
             Resample close prices for each ticker at specified frequency.
             Parameters
             _____
             close prices : DataFrame
                 Close prices for each ticker and date
             freq : str
                 What frequency to sample at
                 For valid freq choices, see http://pandas.pydata.org/pandas-docs/stable/timeseries.html#offset-aliase
         S
             Returns
             prices resampled : DataFrame
                 Resampled prices for each ticker and date
             # TODO: Implement Function
             monthly close = close prices.resample(freq).last()
             return monthly close
         project tests.test resample prices(resample prices)
```

Tests Passed

In [46]: resample\_prices(close).head()

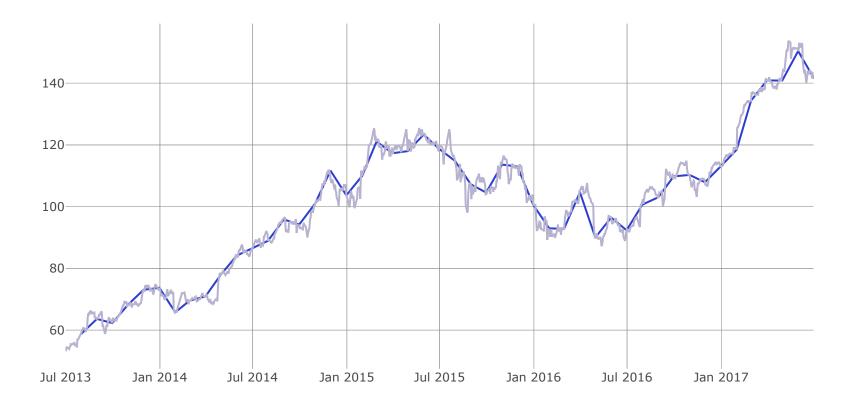
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ticker	Α	AAL	AAP	AAPL	ABBV	ABC	ABT	ACN	ADBE	
date										
2013- 07-31	30.77861719	18.63139292	81.73270857	58.73000866	38.52144972	53.87744989	32.99081455	66.22844876	47.28000000	43.441(
2013- 08-31	32.09288410	15.55986096	79.33492514	63.64994327	36.09056668	53.01732111	30.01866909	64.82868748	45.75000000	41.0137
2013- 09-30	35.34697923	18.25587647	81.98212977	62.28266407	37.88620154	56.91072241	29.89257807	66.07591068	51.94000000	41.696 <sup>-</sup>
2013- 10-31	35.00902763	21.15409315	98.34285959	68.28583759	41.39637606	60.85069550	33.05576095	66.82299697	54.22000000	43.6900
2013- 11-30	36.94707663	22.60801580	100.15741326	73.07037475	41.39637606	65.91719111	34.53897430	70.43234797	56.78000000	42.7329
5 rows	× 495 column	S								
4										<b>+</b>

## **View Data**

Let's apply this function to close and view the results.

## AAPL Stock - Close Vs Monthly Close



# **Compute Log Returns**

Compute log returns  $(R_t)$  from prices  $(P_t)$  as your primary momentum indicator:  $R_t = log_e(P_t) - log_e(P_{t-1})$ 

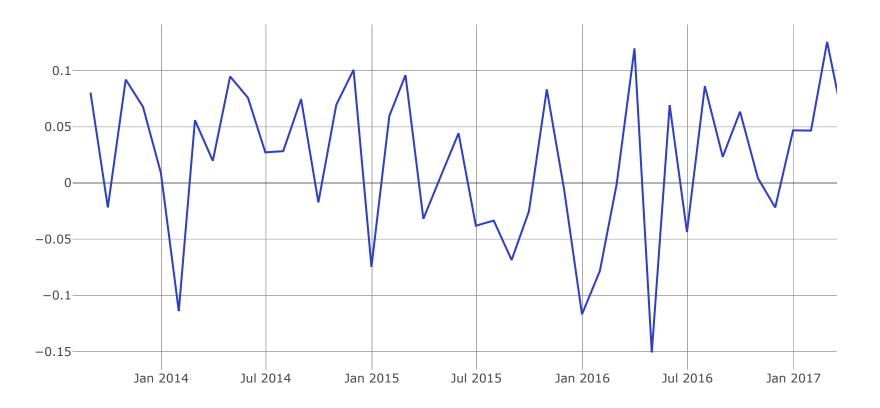
Implement the compute\_log\_returns function below, such that it accepts a dataframe (like one returned by resample\_prices), and produces a similar dataframe of log returns. Use Numpy's log function (https://docs.scipy.org/doc/numpy/reference/generated/numpy.log.html) to help you calculate the log returns.

Tests Passed

#### **View Data**

Using the same data returned from resample\_prices, we'll generate the log returns.

## Log Returns of AAPL Stock (Monthly)



# **Shift Returns**

Implement the shift\_returns function to shift the log returns to the previous or future returns in the time series. For example, the parameter shift\_n is 2 and returns is the following:

	Α	В	С	D	
2013-07-08	0.015	0.082	0.096	0.020	
2013-07-09	0.037	0.095	0.027	0.063	
2013-07-10	0.094	0.001	0.093	0.019	
2013-07-11	0.092	0.057	0.069	0.087	
• • •					

the output of the shift\_returns function would be:

		Shift Re	turns		
	Α	В	С	D	
2013-07-08	NaN	NaN	NaN	NaN	
2013-07-09	NaN	NaN	NaN	NaN	
2013-07-10	0.015	0.082	0.096	0.020	
2013-07-11	0.037	0.095	0.027	0.063	
	• • •	• • •	• • •		

Using the same returns data as above, the shift\_returns function should generate the following with shift\_n as -2:

Shift Returns										
	Α	В	С	D						
2013-07-08	0.094	0.001	0.093	0.019						
2013-07-09	0.092	0.057	0.069	0.087						
• • •	• • •	• • •	• • •	• • •	• • •					
•••	• • •	• • •	• • •	• • •	• • •					
• • •	NaN	NaN	NaN	NaN						
	NaN	NaN	NaN	NaN						

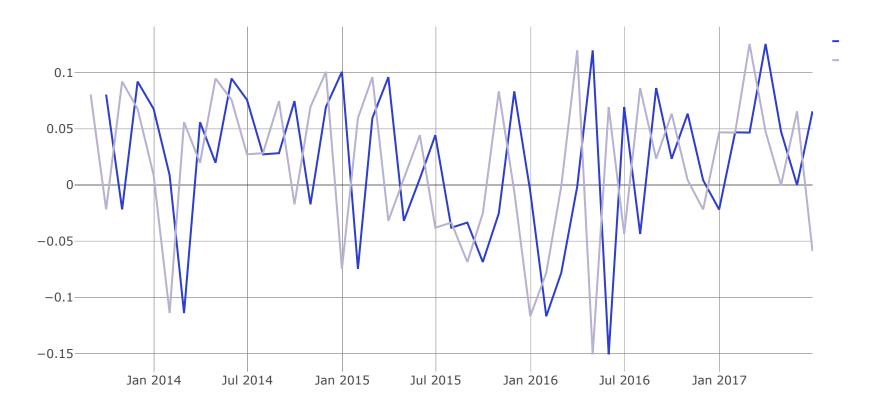
Note: The "..." represents data points we're not showing.

Tests Passed

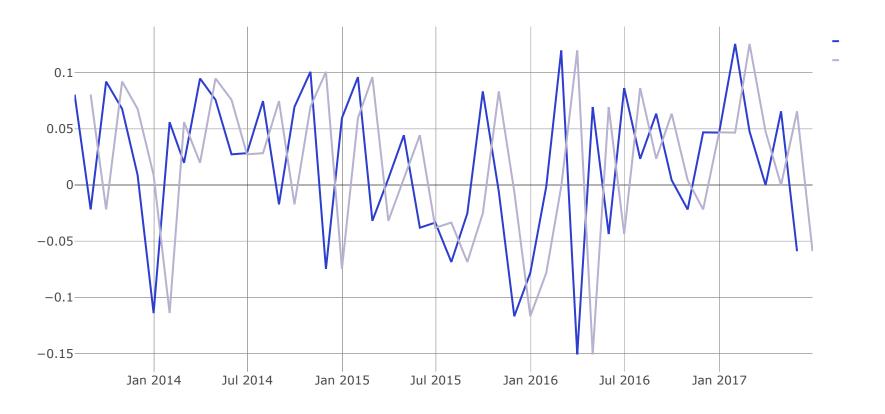
#### **View Data**

Let's get the previous month's and next month's returns.

## Previous Returns of AAPL Stock



## Lookahead Returns of AAPL Stock



# **Generate Trading Signal**

A trading signal is a sequence of trading actions, or results that can be used to take trading actions. A common form is to produce a "long" and "short" portfolio of stocks on each date (e.g. end of each month, or whatever frequency you desire to trade at). This signal can be interpreted as rebalancing your portfolio on each of those dates, entering long ("buy") and short ("sell") positions as indicated.

Here's a strategy that we will try:

For each month-end observation period, rank the stocks by *previous* returns, from the highest to the lowest. Select the top performing stocks for the long portfolio, and the bottom performing stocks for the short portfolio.

Implement the get\_top\_n function to get the top performing stock for each month. Get the top performing stocks from prev\_returns by assigning them a value of 1. For all other stocks, give them a value of 0. For example, using the following prev\_returns:

	Previous Returns									
	Α	В	С	D	E	F	G			
2013-07-08	0.015	0.082	0.096	0.020	0.075	0.043	0.074			
2013-07-09	0.037	0.095	0.027	0.063	0.024	0.086	0.025			
							• • •			

The function get\_top\_n with top\_n set to 3 should return the following:

	Previous Returns									
	Α	В	С	D	Е	F	G			
2013-07-08	0	1	1	0	1	0	0			
2013-07-09	0	1	0	1	0	1	0			
• • •										

Note: You may have to use Panda's <u>DataFrame.iterrows</u> <u>(https://pandas.pydata.org/pandas-docs/version/0.21/generated/pandas.DataFrame.iterrows.html)</u> with <u>Series.nLargest</u> <u>(https://pandas.pydata.org/pandas-docs/version/0.21/generated/pandas.Series.nlargest.html)</u> in order to implement the function. This is one of those cases where creating a vecorization solution is too difficult.

In [158]: #step1 get some sample of data
a=prev\_returns.tail(10).T.tail(10).T

### Out[158]:

ticker	XL	XLNX	XOM	XRAY	XRX	XYL	YUM	ZBH	ZION	ZTS
date										
2016- 09-30	-0.01104021	0.06579968	-0.01191629	-0.04112133	-0.04467244	0.06487578	0.01432323	-0.01173551	0.09555297	0.01240540
2016- 10-31	-0.01178072	0.00239521	0.00160532	-0.03228879	0.03568895	0.03078357	0.00110181	0.00504351	0.01395900	0.01765151
2016- 11-30	0.03132116	-0.06598725	-0.04643273	-0.03179755	-0.03618485	-0.08180785	-0.04530849	-0.20992565	0.03764481	-0.08441037
2016- 12-31	0.04038386	0.06594093	0.05541489	0.01054005	-0.04394012	0.06826631	0.02387708	-0.03416331	0.21341820	0.05457719
2017- 01-31	0.03615589	0.11187869	0.03334393	-0.00643281	-0.06031217	-0.04075737	-0.00094697	0.01539556	0.07851429	0.06064797
2017- 02-28	0.00828549	-0.03660694	-0.07318798	-0.01800276	0.14387403	-0.00424973	0.03879000	0.13680848	-0.01994669	0.02796748
2017- 03-31	0.07484917	0.01624776	-0.02195182	0.11358061	0.07101104	-0.02065858	-0.00320978	-0.01061987	0.06402762	-0.03011775
2017- 04-30	-0.01017620	-0.01593728	0.00844920	-0.01575947	-0.00497178	0.04271546	-0.02197891	0.04404029	-0.06676818	0.00112486
2017- 05-31	0.04871848	0.08633458	-0.00439937	0.01273092	-0.02064767	0.02341935	0.03320595	-0.02035146	-0.04804045	0.05205758
2017- 06-30	0.04302745	0.06090411	-0.00482798	0.00441780	-0.01683069	0.01750300	0.09965606	-0.00368417	0.00296435	0.10432630
4										<b>•</b>

```
In [159]: #step 2, finding maximum of numbers in different columns
top_a = a.apply(lambda x: x.nlargest(3), axis=1)
top_a
```

### Out[159]:

	XL	XLNX	XOM	XRAY	XRX	XYL	YUM	ZBH	ZION	ZTS
date										
2016-09-30	nan	0.06579968	nan	nan	nan	0.06487578	nan	nan	0.09555297	nan
2016-10-31	nan	nan	nan	nan	0.03568895	0.03078357	nan	nan	nan	0.01765151
2016-11-30	0.03132116	nan	nan	-0.03179755	nan	nan	nan	nan	0.03764481	nan
2016-12-31	nan	0.06594093	nan	nan	nan	0.06826631	nan	nan	0.21341820	nan
2017-01-31	nan	0.11187869	nan	nan	nan	nan	nan	nan	0.07851429	0.06064797
2017-02-28	nan	nan	nan	nan	0.14387403	nan	0.03879000	0.13680848	nan	nan
2017-03-31	0.07484917	nan	nan	0.11358061	0.07101104	nan	nan	nan	nan	nan
2017-04-30	nan	nan	0.00844920	nan	nan	0.04271546	nan	0.04404029	nan	nan
2017-05-31	0.04871848	0.08633458	nan	nan	nan	nan	nan	nan	nan	0.05205758
2017-06-30	nan	0.06090411	nan	nan	nan	nan	0.09965606	nan	nan	0.10432630

```
In [160]: #step 3 mapping nulls to 0 and the rest to 1 using applymap
top_a = top_a.applymap(lambda x: 0 if pd.isna(x) else 1)
top_a = top_a.astype(np.int64)
top_a
```

Out[160]:

	XL	XLNX	XOM	XRAY	XRX	XYL	YUM	ZBH	ZION	ZTS
date										
2016-09-30	0	1	0	0	0	1	0	0	1	0
2016-10-31	0	0	0	0	1	1	0	0	0	1
2016-11-30	1	0	0	1	0	0	0	0	1	0
2016-12-31	0	1	0	0	0	1	0	0	1	0
2017-01-31	0	1	0	0	0	0	0	0	1	1
2017-02-28	0	0	0	0	1	0	1	1	0	0
2017-03-31	1	0	0	1	1	0	0	0	0	0
2017-04-30	0	0	1	0	0	1	0	1	0	0
2017-05-31	1	1	0	0	0	0	0	0	0	1
2017-06-30	0	1	0	0	0	0	1	0	0	1

Tests Passed

### **View Data**

We want to get the best performing and worst performing stocks. To get the best performing stocks, we'll use the get\_top\_n function. To get the worst performing stocks, we'll also use the get\_top\_n function. However, we pass in -1\*prev\_returns instead of just prev\_returns. Multiplying by negative one will flip all the positive returns to negative and negative returns to positive. Thus, it will return the worst performing stocks.

```
In [163]: top_bottom_n = 50
    df_long = get_top_n(prev_returns, top_bottom_n)
    df_short = get_top_n(-1*prev_returns, top_bottom_n)
    project_helper.print_top(df_long, 'Longed Stocks')
    project_helper.print_top(df_short, 'Shorted Stocks')

10 Most Longed Stocks:
    INCY, AMD, AVGO, NFX, NFLX, SWKS, ILMN, NVDA, UAL, MU
    10 Most Shorted Stocks:
    RRC, CHK, FCX, MRO, FTI, DVN, GPS, WYNN, SPLS, MAT
```

# **Projected Returns**

It's now time to check if your trading signal has the potential to become profitable!

We'll start by computing the net returns this portfolio would return. For simplicity, we'll assume every stock gets an equal dollar amount of investment. This makes it easier to compute a portfolio's returns as the simple arithmetic average of the individual stock returns.

Implement the portfolio\_returns function to compute the expected portfolio returns. Using df\_long to indicate which stocks to long and df\_short to indicate which stocks to short, calculate the returns using lookahead\_returns. To help with calculation, we've provided you with n\_stocks as the number of stocks we're investing in a single period.

```
In [170]: | def portfolio_returns(df_long, df_short, lookahead_returns, n_stocks):
              Compute expected returns for the portfolio, assuming equal investment in each long/short stock.
              Parameters
              df Long : DataFrame
                  Top stocks for each ticker and date marked with a 1
              df short : DataFrame
                  Bottom stocks for each ticker and date marked with a 1
              Lookahead returns : DataFrame
                  Lookahead returns for each ticker and date
              n stocks: int
                  The number number of stocks chosen for each month
              Returns
              portfolio returns : DataFrame
                  Expected portfolio returns for each ticker and date
              # TODO: Implement Function
              return (df_long - df_short)*lookahead_returns / n_stocks
          project tests.test portfolio returns(portfolio returns)
```

Tests Passed

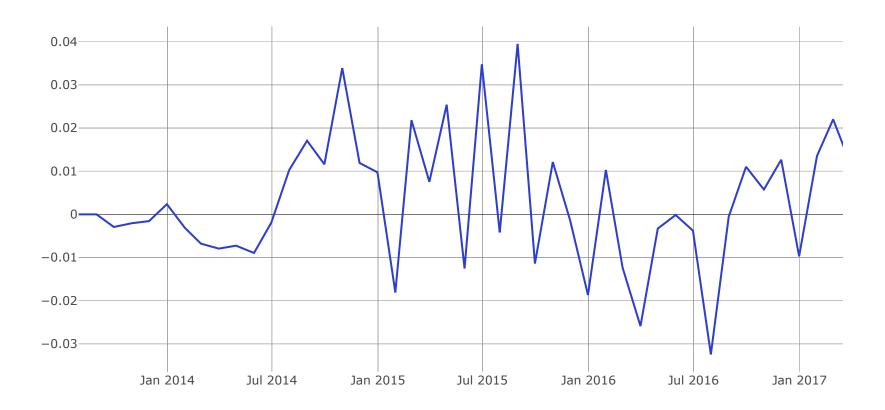
#### **View Data**

Time to see how the portfolio did.

```
In [167]: df_long.shape,df_short.shape
Out[167]: ((48, 457), (48, 470))
In [168]: top_bottom_n
Out[168]: 50
```

```
In [171]: expected_portfolio_returns = portfolio_returns(df_long, df_short, lookahead_returns, 2*top_bottom_n)
    project_helper.plot_returns(expected_portfolio_returns.T.sum(), 'Portfolio Returns')
```

#### Portfolio Returns



# **Statistical Tests**

### **Annualized Rate of Return**

Mean: 0.003076 Standard Error: 0.002180 Annualized Rate of Return: 3.76%

The annualized rate of return allows you to compare the rate of return from this strategy to other quoted rates of return, which are usually quoted on an annual basis.

#### **T-Test**

Our null hypothesis  $(H_0)$  is that the actual mean return from the signal is zero. We'll perform a one-sample, one-sided t-test on the observed mean return, to see if we can reject  $H_0$ .

We'll need to first compute the t-statistic, and then find its corresponding p-value. The p-value will indicate the probability of observing a t-statistic equally or more extreme than the one we observed if the null hypothesis were true. A small p-value means that the chance of observing the t-statistic we observed under the null hypothesis is small, and thus casts doubt on the null hypothesis. It's good practice to set a desired level of significance or alpha  $(\alpha)$  before computing the p-value, and then reject the null hypothesis if  $p < \alpha$ .

For this project, we'll use  $\alpha=0.05$ , since it's a common value to use.

Implement the analyze\_alpha function to perform a t-test on the sample of portfolio returns. We've imported the scipy.stats module for you to perform the t-test.

Note: <u>scipy.stats.ttest\_1samp\_(https://docs.scipy.org/doc/scipy-1.0.0/reference/generated/scipy.stats.ttest\_1samp.html)</u> performs a two-sided test, so divide the p-value by 2 to get 1-sided p-value

```
In [180]: from scipy import stats
          def analyze_alpha(expected_portfolio_returns_by_date):
              Perform a t-test with the null hypothesis being that the expected mean return is zero.
              Parameters
              _____
              expected_portfolio_returns_by_date : Pandas Series
                  Expected portfolio returns for each date
              Returns
              t value
                  T-statistic from t-test
              p_value
                  Corresponding p-value
              # TODO: Implement Function
              t_,p_ = stats.ttest_1samp(expected_portfolio_returns_by_date, 0)
              return t_, p_/2 #because the function is two sided is devided by two
          project_tests.test_analyze_alpha(analyze_alpha)
```

Tests Passed

#### **View Data**

Let's see what values we get with our portfolio. After you run this, make sure to answer the question below.

#### Question: What p-value did you observe? And what does that indicate about your signal?

#TODO: Put Answer In this Cell

our p-value is .082517, and since it is greater that the alpha=.05, this tells us that Annualized Rate of Return: 3.76% that we have seen is very likely to happen. so this rate of return is just a high probability chance and we cant rely on it.

In fact we want lower p-values to go with this strategy, because then it tells us it would be unlikely to observe a high rate of return, and since it has happened then it is probably not by chance.

### **Submission**

Now that you're done with the project, it's time to submit it. Click the submit button in the bottom right. One of our reviewers will give you feedback on your project with a pass or not passed grade. You can continue to the next section while you wait for feedback.