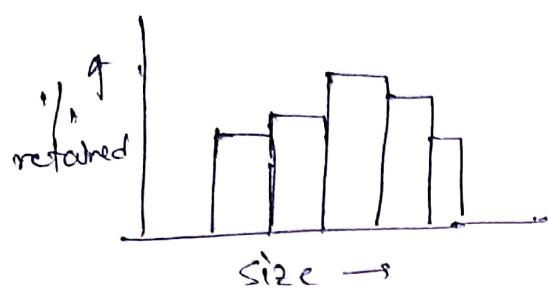
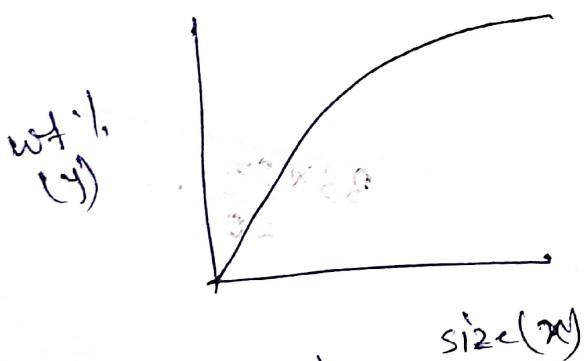
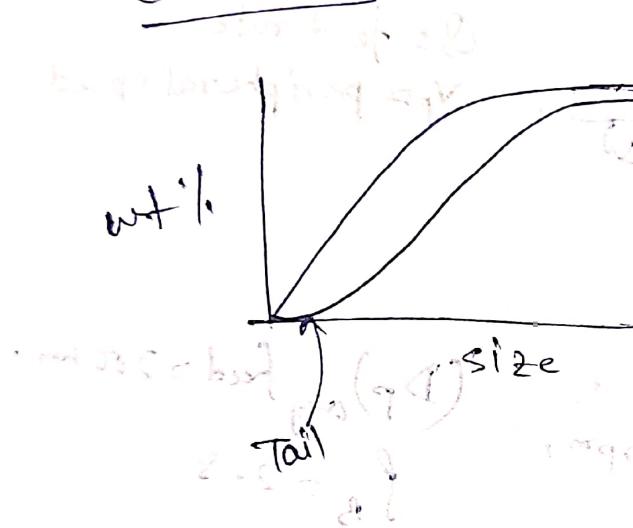


09/10

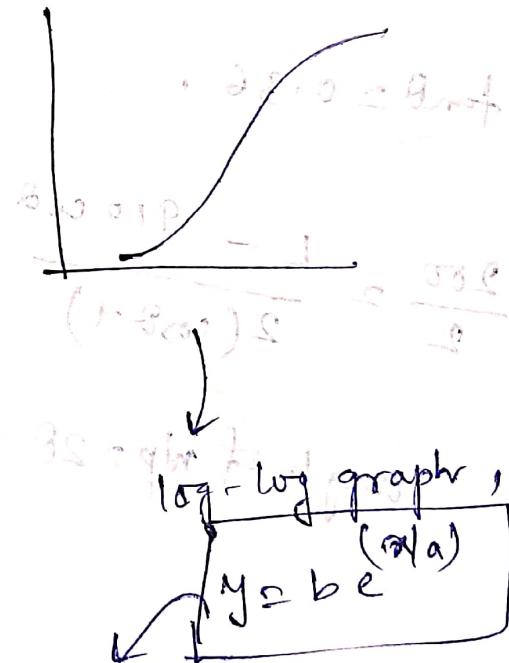
Differential :-



Cumulative :-



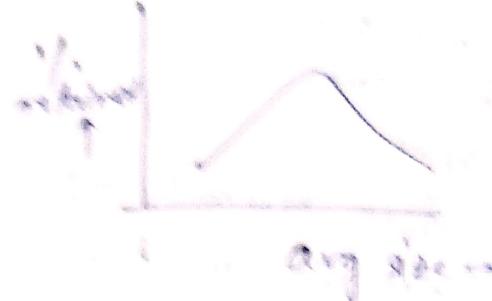
in log-log graph,
linear graph.



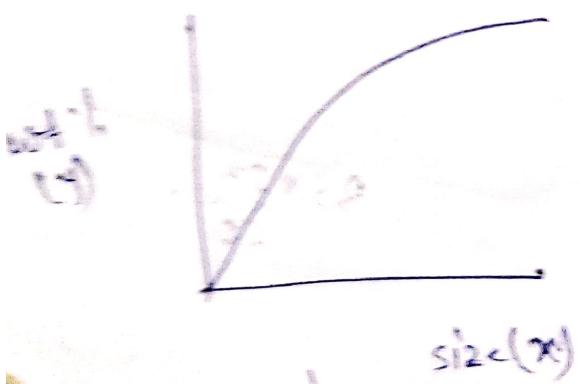
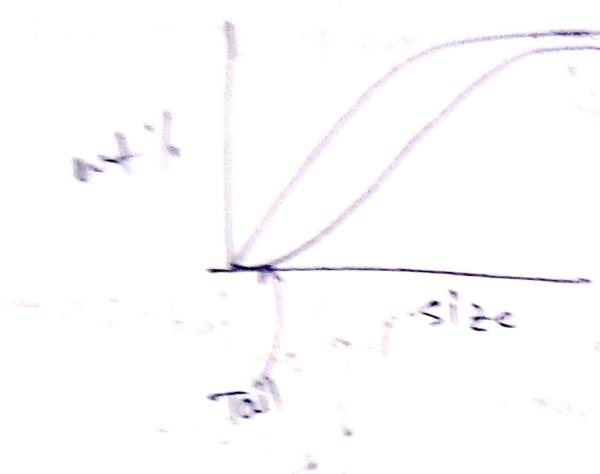
Rosin - Ramler distribution



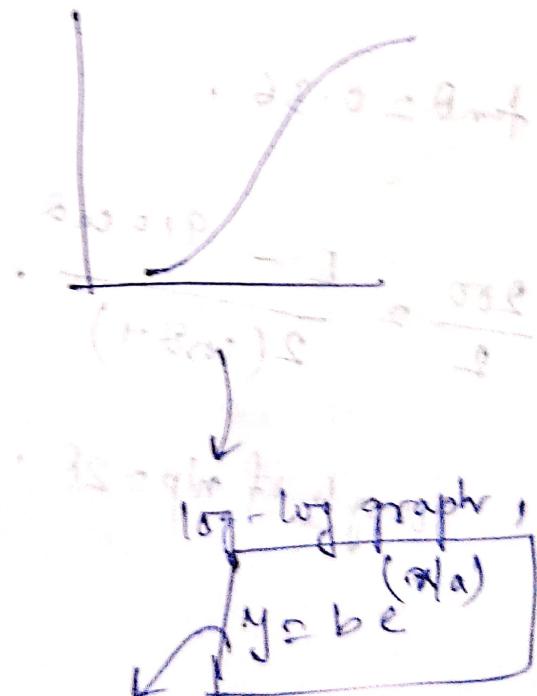
Distribution



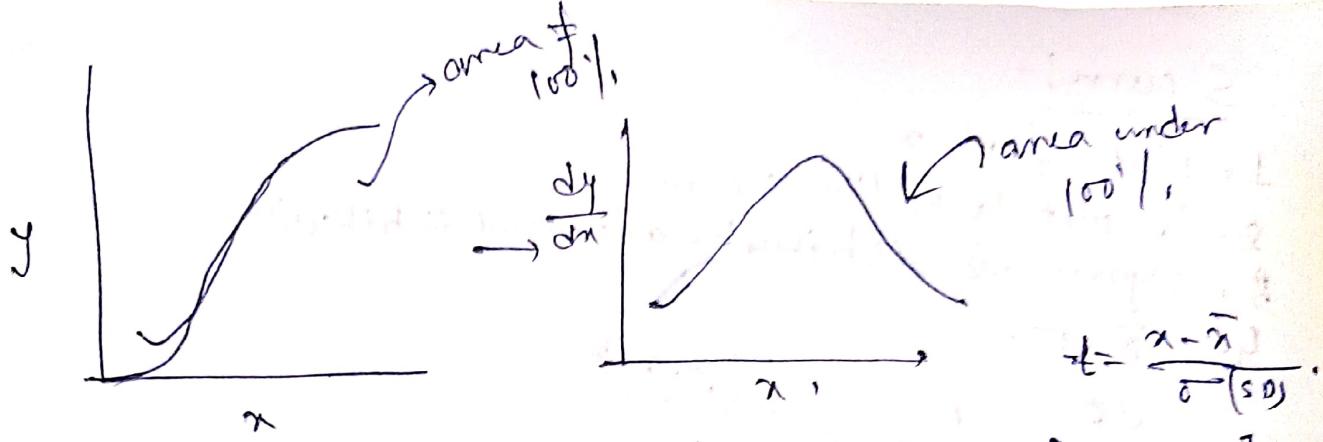
Cumulative



In log-log graph,
linear graph.



Rosin - Rammler distribution



perfect normal distribution form: $-4\sigma \leq t \leq 4\sigma$

$$\frac{dy}{dx}$$

$$(avg) \bar{x} \quad y(\text{wt}) \quad \text{wt avg } \bar{x} = \frac{\sum ny}{\sum y}$$

2

4

6

8

10

$$\frac{dy}{dx} = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\bar{x})^2}{2\sigma^2}}$$

① avg size (\bar{x})

Rosin Ramler's distribution

$$\phi = 100 e^{-6x}$$

wt % (ϕ)

$$\log \left(-\log \left(\frac{\phi}{100} \right) \right) = \log b + n \log x$$

R^2 = root mean square error.

$R^2 \rightarrow 1$ (best fit)

$R^2 \rightarrow 0$ (bad fit).

(for S curve, Rosin Ramler distribution is not used)

S curve:-

1. Plot ϕ vs x
2. If plot looks like S-curve
3. Measures size distribution as normal distribution.

4. $\sqrt{N} \sigma$.

$$\frac{d\phi}{dx} = \frac{1}{\delta \sqrt{2\pi}} e^{-\frac{1}{2} \left(\frac{x-\bar{x}}{\delta} \right)^2}$$

5. If plot looks like exp curve.

6. Go to Rosin-Ramler distribution.

7. Estimate b and n .

8. To these plot below $\log(-\log(\phi/100))$ vs $\log x$.
From slope and intercept \rightarrow bond n value.

Fine particle characterisation:-

particlessize $< 10 \mu\text{m}$,

Now, $\sim < 2.5 \mu\text{m}$,

Microscopic techniques

Optical:- theoretically, 0.18 to 0.150 microns.

Actual \rightarrow 3 to 150 micrometers.

Limit of resolution $d = f \lambda / \sin \phi$.

$$f = \text{factor} = 0.6$$

$$\lambda = \text{WL}$$

N.A = numerical aperture $= \mu \sin \phi$.

μ = refractive index



Laser diffraction -

size < 3 micron, small size, diffraction dominates scattering.

Rayleigh scattering.

$$T = T_0 \left(\frac{1 + \cos^2 \theta}{2R^m} \right) \left(\frac{2\pi}{\lambda} \right)^4 \left(\frac{m^2 - 1}{n^2 + 2} \right)^2 \left(\frac{d}{2} \right)^6 \cdot$$

$\left. + \frac{\kappa^y d^6 (m-1)^{m+1}}{8\pi} \right)$

Mie scattering :

$$T = E \left\{ \kappa^2 D^4 [J I]^2 \theta + (\kappa_1 \theta)^4 + (\kappa_3 \theta)^3 + (\kappa_5 \theta)^2 + \frac{\kappa^y d^6 (m-1)^{m+1}}{8\pi} \right\}$$

Dynamic Light Scattering (DLS)

Γ = diffusion length,

$$\Gamma = D \tau^q \quad \left(\text{eq. } 1 \right)$$

$$\therefore q_r = \frac{4\pi n}{\lambda} \sin \frac{\theta}{2}$$

$$\text{mean } \langle q_r^2 \rangle = \frac{12}{5} \frac{\sigma^2}{\tau^2} = \frac{12}{5} \frac{D^2}{\tau^2}$$

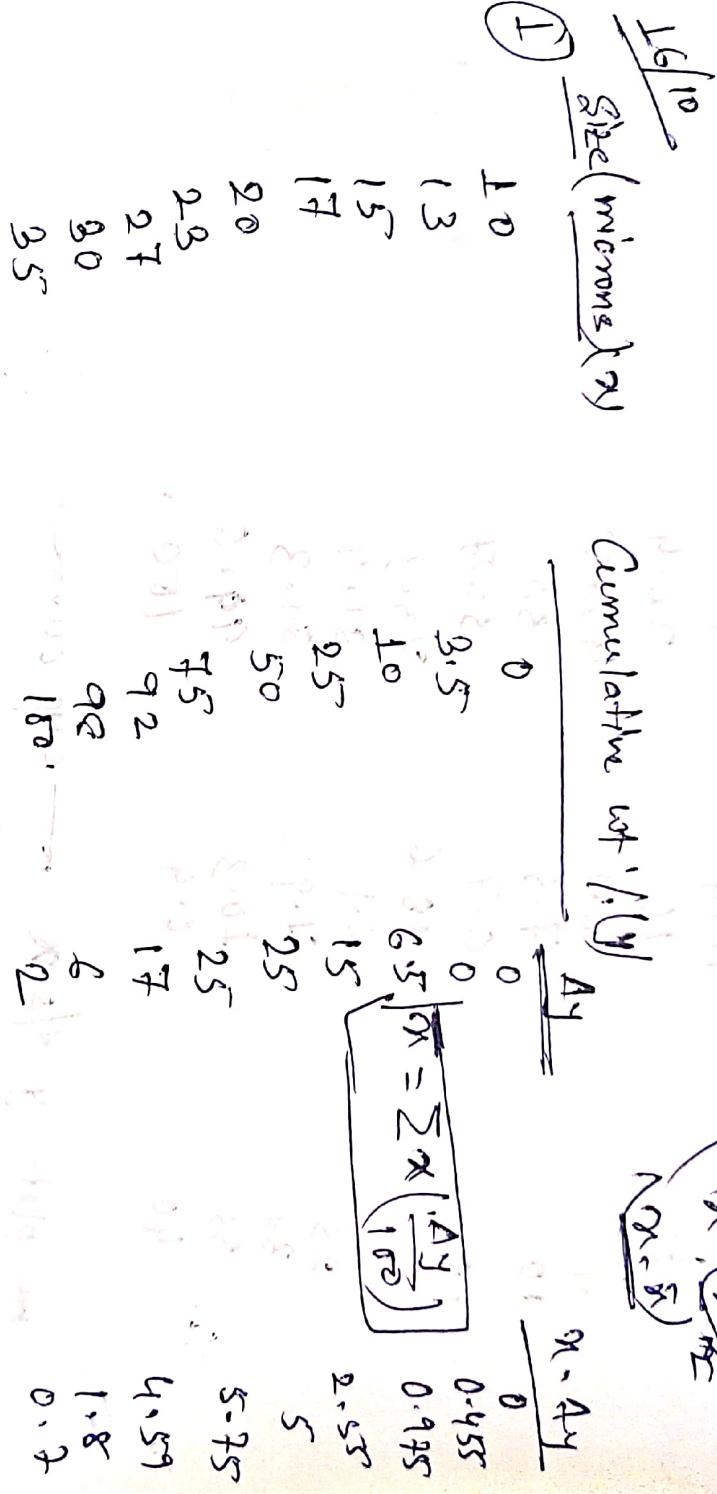
Diffusion coefficient $D = 2.5 \times 10^{-10} \text{ m}^2/\text{s}$

$$\therefore \langle q_r^2 \rangle = \frac{12}{5} \frac{(2.5 \times 10^{-10})^2}{(10^{-9})^2} = 1.2 \times 10^{-10} \text{ m}^2$$



Colloid mill - mainly for wet feeds.

Fluid energy mill
dry feed



$$\frac{dy}{dx} = \frac{1}{\sigma \sqrt{2\pi}} \exp\left(-\frac{1}{2} \left(\frac{x-\bar{x}}{\sigma}\right)^2\right)$$

$$\sigma = \sqrt{\frac{\sum (x - \bar{x})^2 \cdot A_y}{\sum A_y}}$$

$$\bar{x} = \frac{\sum x \cdot A_y}{\sum A_y}$$

$$\bar{x} = 21.82$$

Wet feed - Colloid mill

Wet feed - Colloid mill

Colloid mill

(2) Express the suitable size distribution expression for the ground

$$\frac{\text{Size (mm)}}{x} \quad \text{wt. % (A)} \quad \frac{y(\text{cumulative})}{n_A}$$

2	10.4
5	16.1
7	16.1
10	17.5
15	18.6
20	19.1
25	19.9
30	20.3
35	20.9
40	21.4

plot $y^{1/50}$ vs cum curve.

R-R distribution.

$$y = 150 \exp(-bx^n)$$

$\ln y = \ln 150 - \text{constant} - bn^{\frac{1}{n}}$

$$\ln\left(-\ln \frac{y}{150}\right) = \ln b + n \ln x$$

$$Y = mx + c.$$

plot $\ln\left(-\ln \frac{y}{150}\right)$ vs $\ln x$.

after plotting

$$y = -1.58672 + 2.7851$$

$$R = 0.6366$$

$$m = -1.58 \\ m^b = 2.7851 \Rightarrow b = 16.2$$



Dynamic Light Scattering (DLS) :-

Fine particles
↓
Brownian motion.

(Translational) Diffusion Coeff (Dr) — depends on particle size.

Flux & conc' gradient

$$\text{Flux} \equiv D_T \cdot \frac{dc}{dx}$$

$$\text{Stoke Eqn}:$$

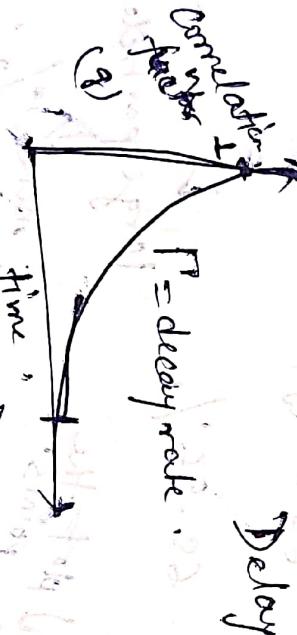
$$R_p = \frac{kT}{6\pi\mu D_T}$$

k = Boltzmann const.

Intensity v/s Time graph → Correlation funcn.

Delay time

$$q = 1 + \beta e^{-\tau \frac{t}{\tau}}$$



Correlation factor

$\tau = \text{decay rate}$

$$\tau = \frac{D_T}{q^2}$$

$q = \text{scattering factor}$

$$= \frac{n_r n_o}{n_i} \sin\left(\frac{\alpha}{2}\right)$$

n_r = ref index.
 n_i = ref index of incident light.

α = incident angle.

Reverse flow cyclone separator.

Wave formation {
on boundary layer } → functional → Δp & θ increases \rightarrow High

Cyclone ← particles from gas
Hydroclone ← m " liquid.

30/10

Q1 A cyclone separator is used to separate coal particles from air. Estimate the cut particle diameter of the separator. Below table, gives information of the size distribution of the feed and collected sample.

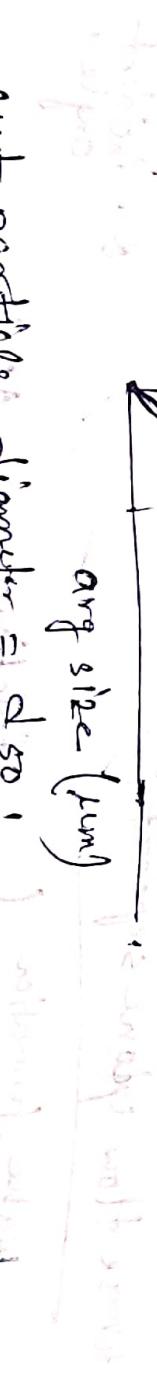
<u>avg size</u>	<u>size (microns)</u>	<u>feed</u>	<u>collected particle</u>	<u>Grade n</u>
2.5	0-5	10	0.1	$0.1/10 \times 100 = 1\%$
7.5	5-10	15	3.53	$3.53/15 \times 100 = 23\%$
12.5	10-15	25	18	$18/25 \times 100 = 72\%$
17.5	15-20	30	27.3	$27.3/30 \times 100 = 91\%$
22.5	20-25	15	14.63	$14.63/15 \times 100 = 97.5\%$
27.5	25-30	5	57.5	$57.5/15 \times 100 = 385\%$

$$\text{total wt (mass)} = 100 \text{ g}$$

$$\text{Overall} (m) = \frac{68.56}{100} \times 100 = 68.56 \text{ g}$$

S curve: plot other points with more % eff ↑

Grade rank 1.9
start with origin:



Cut particle diameter, d_{50} :

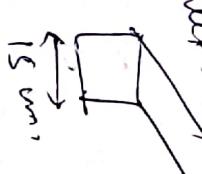
$$d_{50} = 9 \text{ mm}$$



Scanned with OKEN Scanner

(2)

Inlet width = $B_c = 15 \text{ cm}$
shortest length of 25 cm with diameter 0.5 m operating at
five effective terms. Gas temp $= 345 \text{ K}$ and inlet vel = 20 m/s .
avg particle size = $10 \mu\text{m}$.
particle density = 1.2 g/cc.
density of air = 1.2 kg/m^3 .
viscosity = $\nu = 0.0745 \text{ kg/m.s.}$



$$\rightarrow d_{pe} = \left(\frac{q \mu B_c}{2 \pi N v_i (\rho_p - \rho)} \right)^{1/2}.$$

$$\frac{1.2 \times 10^{-3}}{10^{-6}} \\ 1.2 \times 10^3.$$

$$q = 0.0745 \times 0.15$$

$$3600 \times 2 \times \pi \times 5 \times 20 \times 1.2 \times (1000 - 1)$$

$$d_{pe} = 6.09 \times 10^{-6} \text{ m.}$$

$ab = \text{inlet area}$.

$$\text{pressure drop} = \Delta P = 0.8 \frac{\rho_0 V_{lab}^2}{D_e}$$

$$= 0.8 \times \frac{1.2 \times 20 \times 20 \times (0.15)^2}{(0.5)^2}$$

$$\Delta P = 34.56 \text{ Pa}$$

length = 100 cm
width = 15 cm
height = 10 cm

Air flow cyclone separator

Flow direction and separator direction same.

$$\Delta P = \rho_{air} \text{ drop } \downarrow$$



Vortex flow direction

Electrostatic Precipitator

Used for fine gas

Charged particles \rightarrow ESP

Necessary Conditions:-

$$\frac{\text{Voltage}}{\text{distance}} = 10 \left[1 + \frac{0.3}{R_1^{0.5}} \right] R_1 \ln\left(\frac{R_2}{R_1}\right) \text{ kV/m}$$

R_1 = radius of wire electrode

R_2 = radius of collecting plate

red :-

electrical conducting particles

$$w = 0.16 \left[\frac{dp^2 v^2}{\mu} \right]$$

non conducting :-

$$w = 0.095 \left[\frac{dp^2 v^2}{\mu} \right]$$

$$\text{Collection efficiency} = 1 - e^{-\mu \left(Q_g / w.A_e \right)}$$

collecting & calculating

$$\frac{\text{residence time}}{m/s} = s.$$

positive particles have longer residence time than negative particles.

positive particles have longer residence time than negative particles.

conducting particles — pores \rightarrow charge difference.

\rightarrow for separation

positive particles have longer residence time than negative particles.

positive particles have longer residence time than negative particles.

conducting particles — pores \rightarrow charge difference.

\rightarrow for separation

Filtration :-

Separation of solid from liquid.
crystallization.

membrane filtration \rightarrow particles are very small,

filter media \rightarrow polymers/cloth



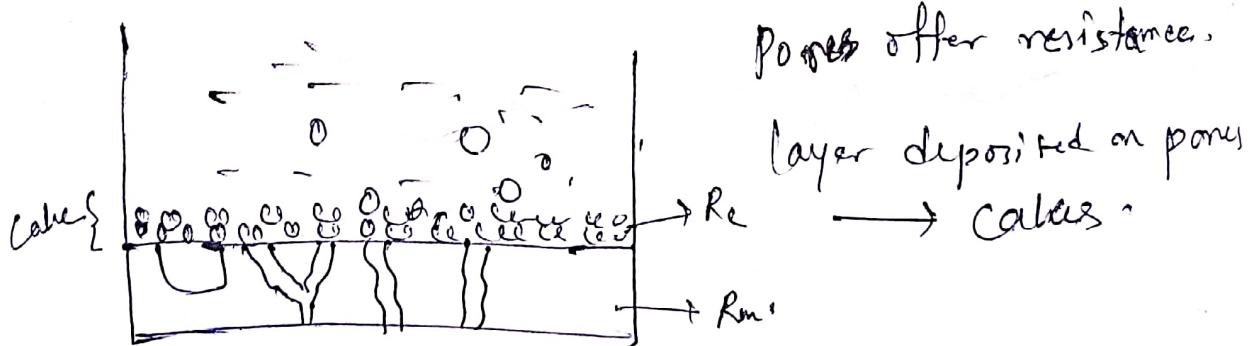
size exclusion \rightarrow particle bigger than pore size, it excludes.

Diffusion \rightarrow individual molecule diffuses.

(mass transfer) \downarrow
kinetic energy \rightarrow thermal energy \rightarrow greatest
polymer chain.

By applying high pressure \rightarrow speed \uparrow

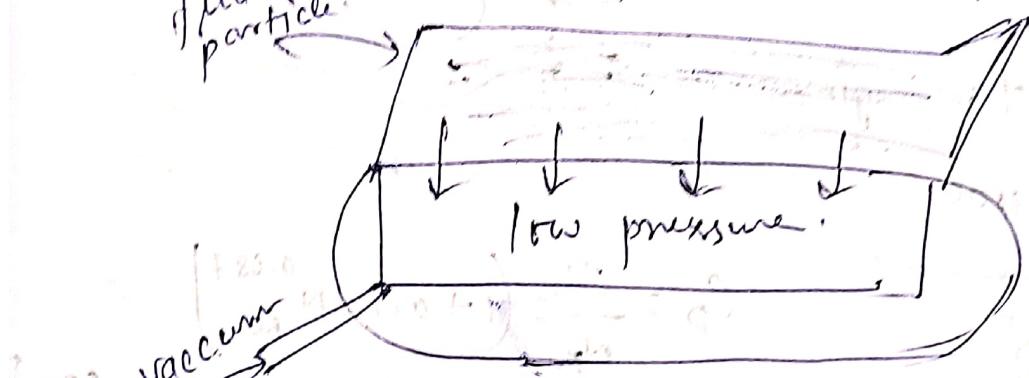
filter media:-



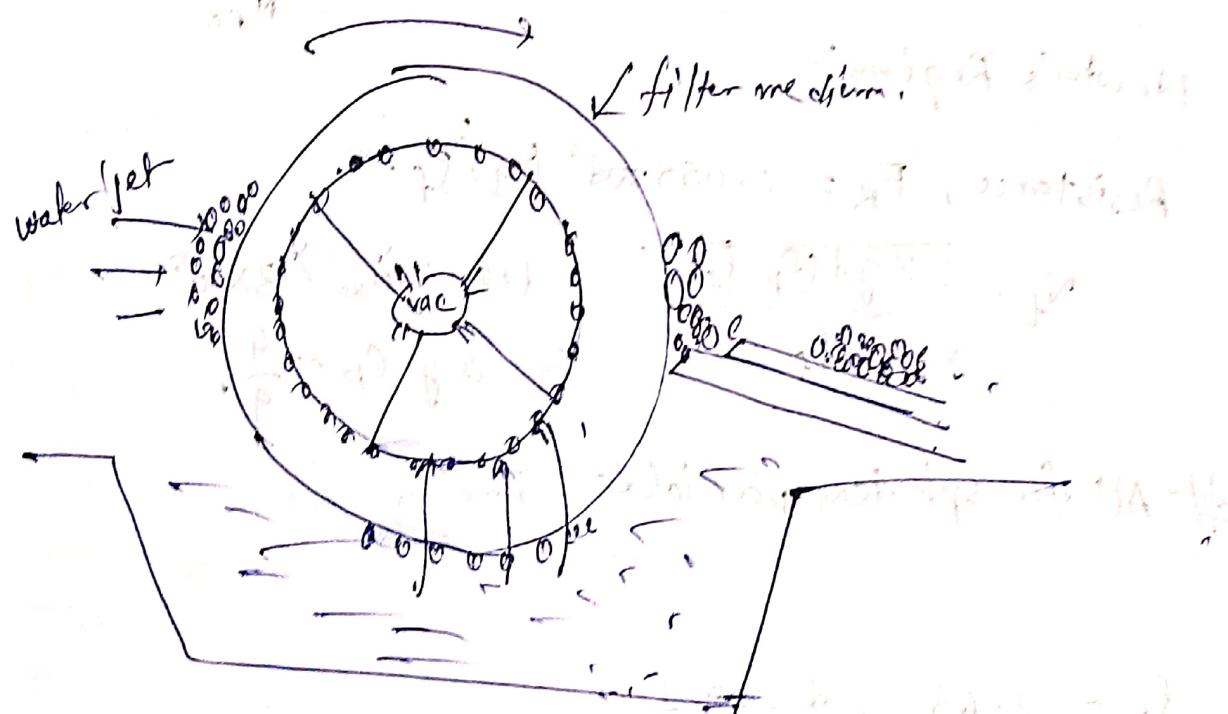
-) constant pressure \rightarrow flow rate with time decreases.
-) constant rate filtration = $\Delta P \uparrow$ to maintain flow rate constant.

- 1) Plate and frame filter press → internal press
- 2) Rotary drum filter
- 3) Belt filter

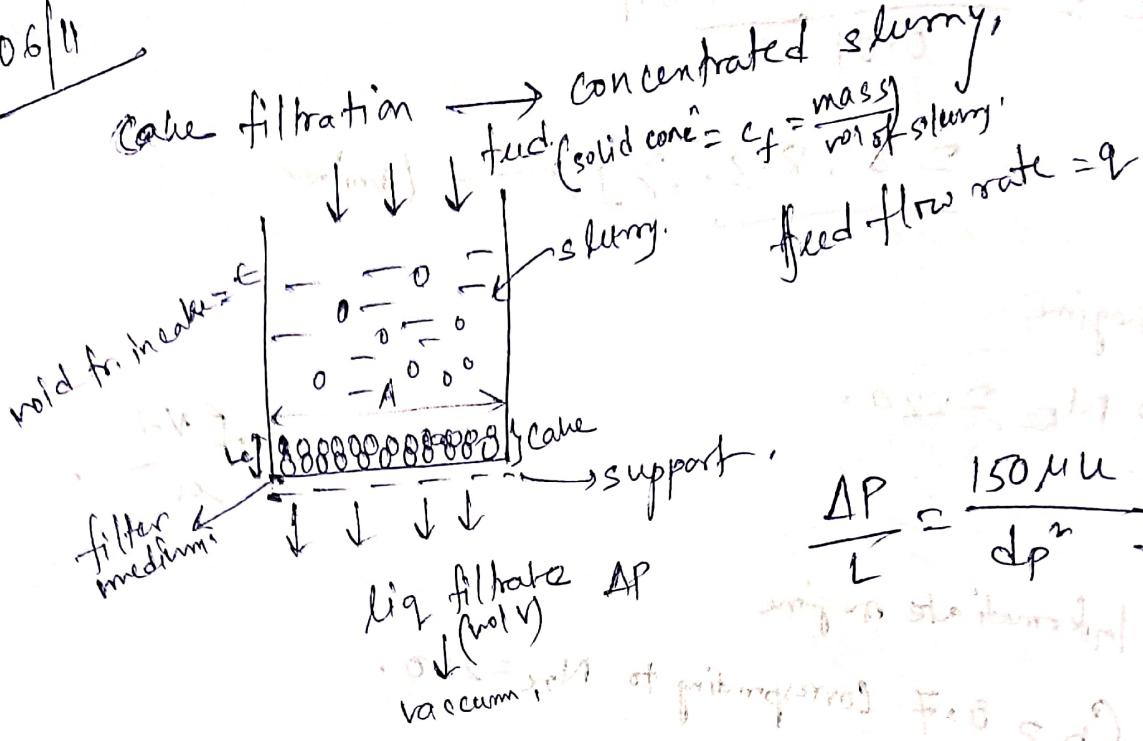
Belt filter: → filter medium → Discontinuous pressure filter



Rotary drum filter: → Continuous vacuum filter

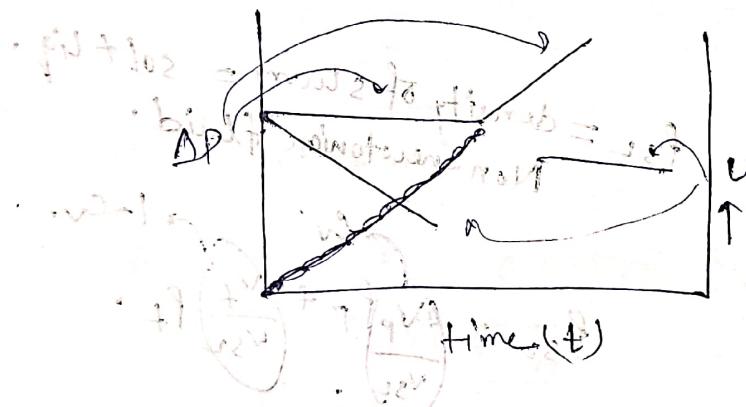


06/11



$$\frac{\Delta P}{L} = \frac{150 \mu u (1-\epsilon)^m}{dp^2 + \epsilon^3}$$

Flow through cake resembles flow through packed usually 'Re' in filtration is low



$$\Delta P, u, t = f(t)$$

$$\frac{\Delta P}{L}, u = \frac{6}{(SP/V_P)^2}$$

$$\therefore \frac{\Delta P}{L} = \frac{150 \mu u (1-\epsilon)^m}{36 / (SP/V_P)^2 + \epsilon^3}$$

$$\frac{\Delta P}{L} = \frac{130}{36} \mu \mu \left(\frac{1-e}{e^3} \right)^n \left(\frac{s_p}{\nu_p} \right)^n \quad \text{--- mom balance eqn^n}$$

$$\frac{\Delta P}{L} = K \cdot \mu \mu \left(\frac{1-e}{e^3} \right)^n \cdot \left(\frac{s_p}{\nu_p} \right)^n \quad \text{--- } ①$$

vol of cake = $A L_c$

vol in cake = $A l_{at}$

$\text{sol in } \dots = A L_c (1-e)$

Solids in feed slurry = solids deposit on the filter medium.

$$c_f [v_{xt}] = A L_c (1-e) \rho_s$$

if) $c_f \rightarrow \frac{\text{mass of solids}}{\text{vol of liquid}}$

$$c_f \times v_f = A L_c (1-e) \rho_s$$

Solid mass balance

vol balance

ligr in feed slurry = ligr in the cake + filter plate.

$$v_f = A L_c e + v$$

$$v = \frac{dV(t)}{dt}$$

$$\therefore c_f (A L_c e + v) = A L_c (1-e) \rho_s$$

$$\Rightarrow L_c^2 \frac{v c_f}{\left(A (1-e) \rho_s - A e c_f \right)} = \frac{v c_f}{A ((1-e) \rho_s - e c_f)}$$

$$\text{if) } c_f \rightarrow \frac{\text{mass of solid}}{\text{vol of liquid}}$$

$$\frac{c_f}{\rho_s} = \frac{\text{vol of solid}}{\text{vol of slurry}}$$

$$\Rightarrow \left(\frac{\rho_s}{c_f} - 1 \right) = \frac{v_f}{v_s} \quad , \quad \Rightarrow \frac{v_s}{v_f} = \frac{c_f}{(\rho_s - c_f)}$$



$$\Rightarrow \frac{P_s \times V_s}{V_f} = \frac{C_f}{C_f + P_s} \times P_s$$

$$L_c = \frac{V_{cf}}{A(1-\epsilon)P_s - C_f A \epsilon}$$

$$L_c = \frac{V_{cf}}{A[1-\epsilon]P_s - C_f \epsilon]$$

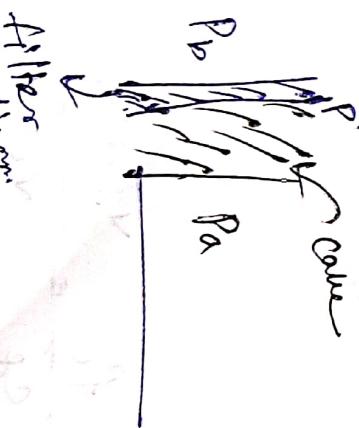
$$L_c = \frac{V_{cf}}{A}$$

$$\frac{\Delta P}{L_c} = \kappa \mu_f \frac{(1-\epsilon)}{e^3} \left(\frac{S_p}{V_p} \right)^m$$

$$\Delta P_2 = \kappa \mu_f V \left(\frac{S_p}{V_p} \right)^m \cdot \mu_f \frac{V_p}{A}$$

$$\rightarrow \frac{\Delta \mu_f V}{A}$$

$$\frac{dt}{dv} = \frac{\lambda \rho \mu_f}{\Delta P_c} \times \frac{V}{\Delta P_c}$$



$$\Delta P = P_a - P_b$$

$$\Delta P = \Delta P_c + \Delta P_m$$

filter
medium

R_m = resistance of filter medium.

$$\Delta P \frac{dt}{dV} = \frac{R_m \mu_f}{A^2} \frac{dV}{\Delta P_f}$$

void fraction of cake \ll void fraction of filter medium.

$$\Delta P_c = \frac{\alpha \mu_f}{A^2} V \cdot \frac{dV}{dt}$$

$$\Delta P_m = \frac{R_m}{A^2} \mu_f \cdot \frac{dV}{dt}$$

$$\Delta P = (\Delta P_c + \Delta P_m) \cdot \frac{\mu_f}{A^2} \cdot \frac{dV}{dt}$$

α = cake resistance
 R_m = filter medium resistance

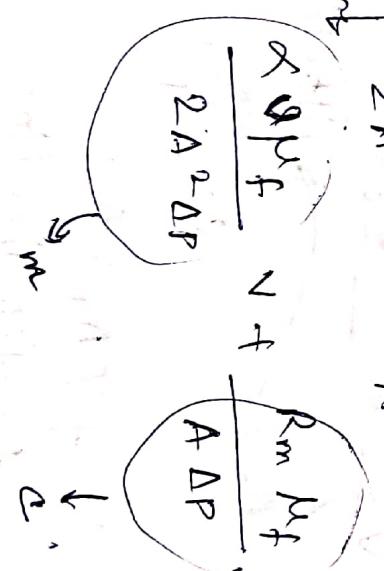
$$\int \Delta P \cdot dt = \int \frac{\mu_f}{A^2} \cdot (\Delta P_c + \Delta P_m) \cdot dV$$

$$\Delta P t = \frac{\mu_f}{A^2} (\Delta P_c + \Delta P_m) \frac{V}{2}$$

$$\therefore \Delta P t = \frac{\alpha \mu_f V}{2 A^2} + \frac{R_m \mu_f V}{A}$$

constant pressure filtration

$$\frac{t}{V} = \frac{\alpha \mu_f}{2 A^2 \Delta P} + \frac{R_m \mu_f}{A \Delta P}$$



$$\frac{\Delta P_m}{L} = \frac{150 \mu\text{v} (1-c)}{\left(\frac{G}{S_p/N_p}\right)^n t^3}$$

After medium
filtration

$$\frac{\Delta P_m}{L_m} = \frac{150}{\left(\frac{G}{S_p/N_p}\right)^n t^3} (1-t)^n \mu\text{v}.$$

$$\Delta P_m = \frac{150 L_m}{\left(\frac{G}{S_p/N_p}\right)^n t^3} (1-t)^n \mu\text{v} + \frac{dN}{dt} \cdot \frac{1}{A}$$



constant rate filtration condition

$$\frac{dN}{dt} = \frac{N}{t}.$$

$$\Delta P = \sqrt{\frac{d \Delta P_m}{dt}} + R_m \mu_f \sqrt{\frac{N}{t}}$$

$$\frac{t}{t^2} = \frac{1}{t} - 1$$

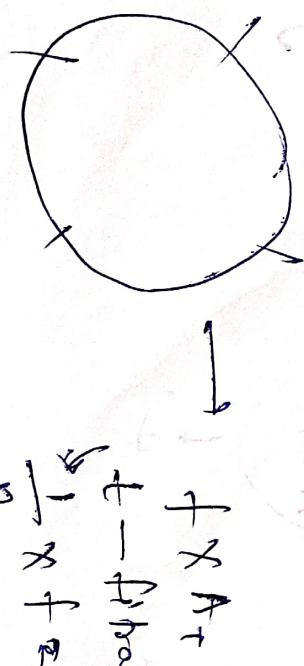
$$\Rightarrow \sqrt{t^2 + t} - t = 0.5c$$

design A_m \rightarrow filtration area

$$A_m = \frac{\pi D_m}{4}$$

$$t \propto A^2$$

$t \propto A^2$
 $t - \text{filtration time}$



Unit operations

by McCabe and Smith

F10

F11

F12

PrSCF

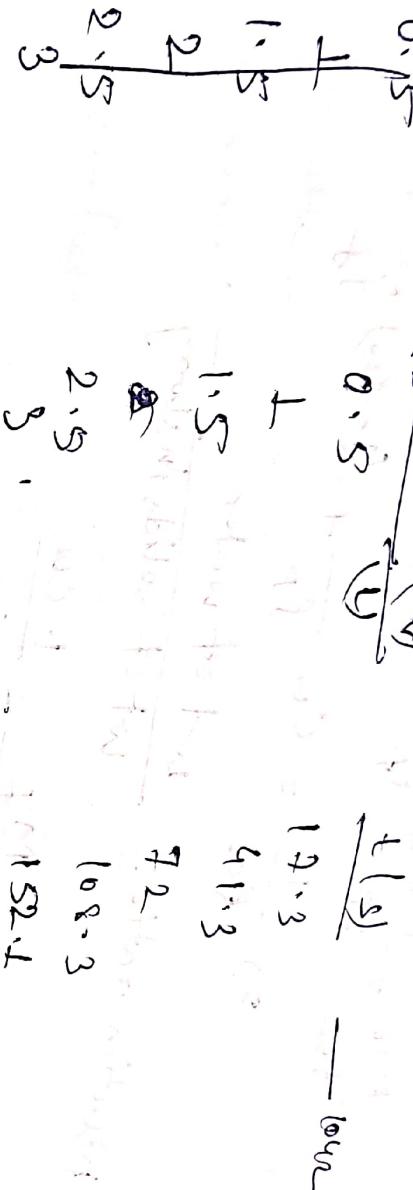
Insert

Delete

Backspace

① Laboratory filtration experiment is conducted at constant pressure. The filter medium and cake. Estimate μ_{Rm} of the slurry is 25°C. Estimated area of filter area is 400 cm². Cone of solids in the slurry is observed to be 23.5 g/L of liquid. Following data is observed.

Plot the $\frac{1}{t} \ln \left(\frac{V_f}{V_0} \right)$ vs time t.



Plot the $\frac{1}{t} \ln V_0$.

$$C = \frac{C_f}{1 - \left(\frac{m_f}{m_i} \right)^n} C_s / \beta$$

$$\frac{1}{t} = \left(\frac{\mu_{Rm}}{2} \right)^n + \frac{1}{t_0}$$

$$\frac{1}{t_0} = \frac{\mu_{Rm}}{A \Delta P g_c}$$

$$K_c = \mu_{Rm} A \Delta P g_c$$



SN.

-) Arithmetic normal distribution :-
-) log normal distribution :- $y = \frac{d\phi}{dx} = \frac{1}{\sigma\sqrt{2\pi}} \exp\left[-\frac{(x-\bar{x})^2}{2\sigma^2}\right]$.
-) Rosin - Ramler - Bennet - Sperling formula. $\phi = \exp(-bx^n)$.
-) Gates - Gaudin - Schumann. $F(x) \approx (bx)^n$.
-) Gaudin - Meloy. $F(x) = [1 - (1-bx)^m]$
-) Roller. $F(x) = a\sqrt{x} \exp(-b/x)$.
-) Svensson. $F(x) = x \operatorname{Erf}(y)$.

Optical microscope → theoretically 0.18 to 0.150 microns
 Experimentally : 3 to 150 microns.

Unit of resolution $d = \frac{f\lambda}{NA}$.

f₂ factor = 0.6

λ = wave length.

NA = numerical aperture $\approx \mu \sin(\theta)$.

μ = refractive index.

Laser Diffraction:-

Rayleigh Scattering → particles smaller than wavelength.

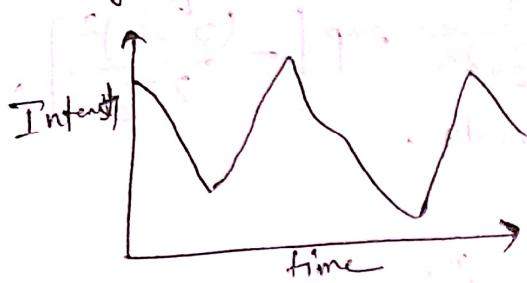
Mie Scattering → particles larger than the wavelength.

$$\text{Rayleigh: } I = I_0 \left(\frac{1 + \cos^2 \theta}{2R^2} \right) \left(\frac{2\pi}{\lambda} \right)^4 \left(\frac{m^2 - 1}{m^2 + 2} \right)^2 \left(\frac{d}{2} \right)^6$$

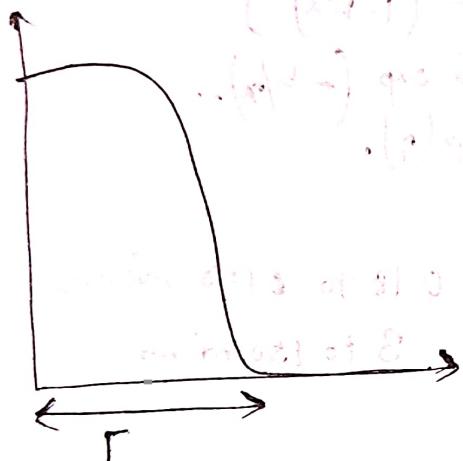
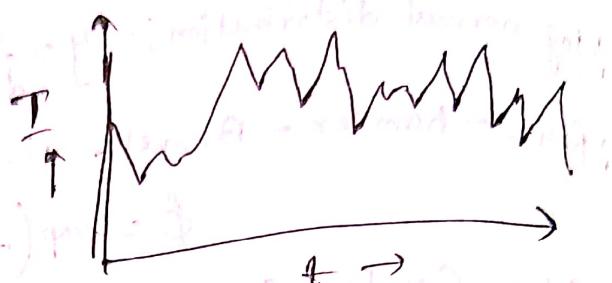
$$\text{Mie: } I = E \left\{ K^2 D^4 [J_1]^2 \theta + (k_1 \theta)^2 + (k_2 \theta)^3 + (k_3 \theta)^5 + \frac{k_4 d^6 (m+1)^2 \theta^6}{8\pi} \right\}$$

DLS :-

large particles.



smaller particles



$$\Gamma = D_T q^2$$

D_T = diffusion coeff

$$q = \frac{4\pi n}{\lambda} \sin \frac{\theta}{2}$$

n = refractive index

λ = wave length

θ = scatter angle

Einstein-Stokes Law:

$$\text{Hydrodynamic diameter } D_h = \frac{k_B T}{6\pi n D_T}$$

Bag Filter:-

$$\text{Filtration vel} = \frac{\text{air}}{\text{cloth ratio}}$$

Reverse Flow Cyclone Separator:-

$$\text{Cut particle diameter, } d_{pc} = \left[\frac{9 \mu B_c}{2 \pi N \gamma_i (\rho_p - \rho)} \right]^{1/2}$$

B_c = inlet width

N = effective no of turns (5-10 for common cyclone)

γ_i = inlet gas vel (m/s).

ρ_p = particle density.

ρ = gas density.

Collection efficiency:-

$$E = \frac{1}{1 + (\frac{dp_c}{dp})^2}$$

Pressure drop:-

Shepard and Lapels equ":-

$$\Delta P = 0.8 \frac{\rho g V_i^2 ab}{D_s^2}$$

$$N_e = \frac{1}{H} \times \left[L_c + \frac{Z_c}{2} \right]$$

N_e = no of turns inside the device.

H = ht of inlet duct

L_c = length of cyclone body.

Z_c = length (vertical) of cyclone cone

Electrostatic Precipitator:-

Necessary voltage:- $V = 18 \left[1 + \frac{0.3}{R_1^{0.5}} \right] R_1 \ln \left(\frac{R_2^2}{R_1} \right)$ KV.

R_1 = radius of wire electrode.

R_2 = radius of collecting electrode.

velocity of collection particles:-

conducting particles :- $w = 0.16 \left[\frac{d_p^2 v^2}{\mu} \right]$

non-conducting particles :- $w = 0.095 \left[\frac{d_p^2 v^2}{\mu} \right]$.

collection efficiency of particle:-

$$\eta = 1 - \exp \left(\frac{Qg}{w \cdot A_c} \right)$$