



**BHASKARACHARYA COLLEGE OF APPLIED SCIENCES**

(University of Delhi)

Accredited 'A' Grade by NAAC

'Star College Status' by DBT

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# MATHEMATICAL PHYSICS 3

## PRACTICAL FILE



**SUBMITTED BY**

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**2<sup>st</sup> Year 4<sup>st</sup> Semester**

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# SHOOTING METHOD

## Program

```
funcprot(1);clear;clc;clf;
xi=0;xf=%pi/2;h=0.1;x=xi:h:xf;n=length(x);yi=1;yf=1;
function[g]=f(x,y,z)
    g=20*y +32;
endfunction

function [y,z]=RK2(yi,zi)
    y(1)=yi;z(1)=zi;
    for i=1:n-1
        s1=z(i);p1=f(x(i),y(i),z(i));
        s2=z(i)+h*p1;p2=f(x(i)+h,y(i)+s1*h,z(i)+p1*h);
        y(i+1)=y(i)+(h/2)*(s1+s2);
        z(i+1)=z(i)+(h/2)*(p1+p2);
    end
endfunction

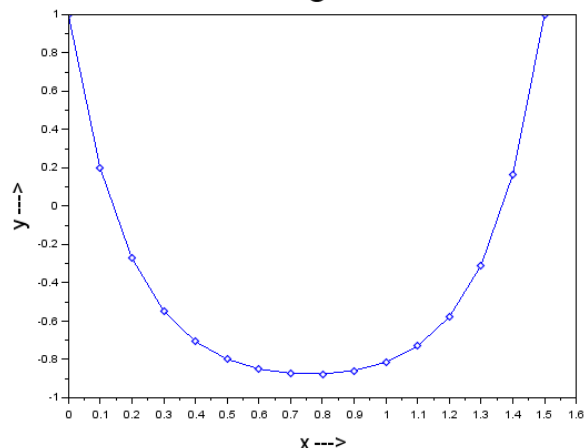
for i=1:2
    zt(i)=input("Enter guess"+string(i)+"for initial slope (dy/dx): ");
    [y,z] = RK2(yi,zt(i));
    yn(i)=y(n,1);
end
zc=zt(1)+(zt(2)-zt(1))*(yf-yn(1))/(yn(2)-yn(1));
[y,z]=RK2(yi,zc);
disp(" x          y          z");disp([x' y z]);
plot(x',y,'d-');
xlabel("x ---->","fontsize",4);
ylabel("y ---->","fontsize",4);
title("Shooting Method","fontsize",6);
```

## Output

```
Enter guess1for initial slope (dy/dx): 0
Enter guess2for initial slope (dy/dx): 9
```

x	y	z
0.	1.	- 11.313922
0.1	0.1986078	- 6.6372891
0.2	- 0.2713578	- 3.8903618
0.3	- 0.5465248	- 2.2743399
0.4	- 0.7068680	- 1.3191621
0.5	- 0.7989518	- 0.7467711
0.6	- 0.8494507	- 0.3901584
0.7	- 0.8728732	- 0.1446178
0.8	- 0.8757234	0.0630283
0.9	- 0.8582936	0.2962834
1.	- 0.8145752	0.6284534
1.1	- 0.7302076	1.1657349
1.2	- 0.5777694	2.081204
1.3	- 0.3078698	3.6705927
1.4	0.1668516	6.4478362
1.5	1.	11.311264

Shooting Method



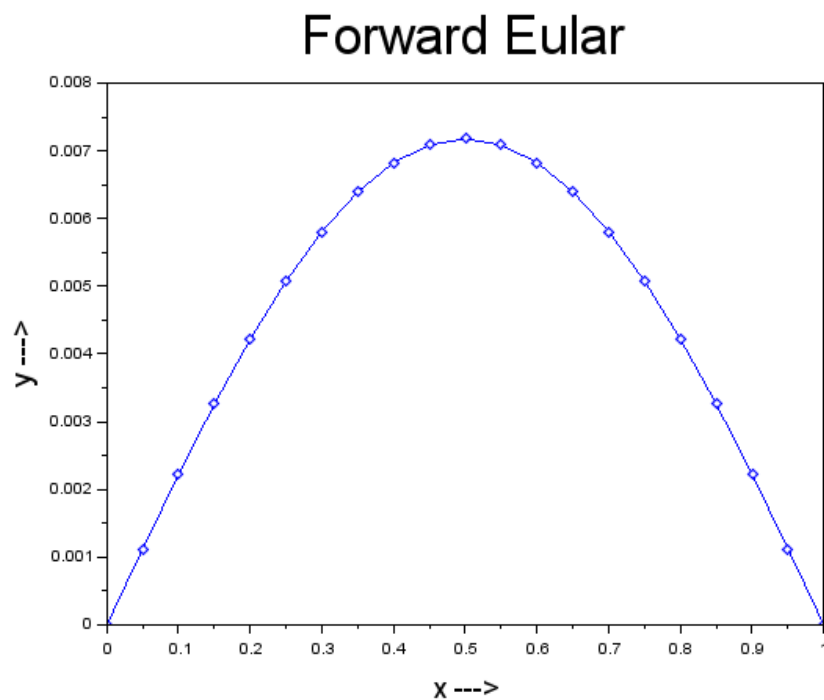
## FORWARD EULAR METHOD

### **Program**

```
clear;clc;clf;
function u=f(x,t)
    u=sin(%pi*x)
endfunction
function g=ex(x,t)
    g=exp((-pi^2)*t)*sin(%pi*x)
endfunction
xi=0
xf=1
ti=0
tf=0.5
h=0.05
k=0.0005
alp=1
lambda=((alp^2)/(h^2))*k
n=floor((xf-xi)/h)
m=floor((tf-ti)/k)
u(1)=0;u(n+1)=0
x(1)=xi;x(n+1)=xf
for i=1:n-1
    x(i+1)=x(i)+h
end
for i=1:n-1
    w(i)=f(x(i+1))
end
for i=1:n-1
    for j=1:n-1
        if i==j then
            A(i,j)=(1-(2*lambda))
        elseif i==j+1 then
            A(i,j)=lambda
        elseif i==j-1 then
            A(i,j)=lambda
        else
            A(i,j)=0
        end
    end
end
for t=1:m
    w=A*w
end
for i=1:n-1
    u(i+1)=w(i)
end
disp("x          y");disp([x u]);
plot(x,u,'d-')
xlabel("x ---->","fontsize",4);
ylabel("y ---->","fontsize",4);
title("Forward Euler","fontsize",6);
```

## Output

x	y
0.	0.
0.05	0.0011228
0.1	0.0022179
0.15	0.0032584
0.2	0.0042187
0.25	0.0050751
0.3	0.0058066
0.35	0.0063950
0.4	0.0068260
0.45	0.0070890
0.5	0.0071773
0.55	0.0070890
0.6	0.0068260
0.65	0.0063950
0.7	0.0058066
0.75	0.0050751
0.8	0.0042187
0.85	0.0032584
0.9	0.0022179
0.95	0.0011228
1.	0.



# CRANK NICHOLSON

## **Program**

```
clear;clc;clf;
function u=f(x,t)
    u=sin(%pi*x)
endfunction
function g=ex(x,t)
    g=exp((- %pi^2)*t)*sin(%pi*x)
endfunction
xi=0
xf=1
ti=0
tf=0.5
h=0.05
k=0.0005
alp=1
lambda=((alp^2)/(h^2))*k
n=floor((xf-xi)/h)
m=floor((tf-ti)/k)
u(1)=0;u(n+1)=0
x(1)=xi;x(n+1)=xf
for i=1:n-1
    x(i+1)=x(i)+h
end
for i=1:n-1
    w(i)=f(x(i+1))
end
for i=1:n-1
    for j=1:n-1
        if i==j then
            B(i,j)=(1-lambda)
            A(i,j)=(1+lambda)
        elseif i==j+1 then
            B(i,j)=lambda/2
            A(i,j)=-lambda/2
        elseif i==j-1 then
            B(i,j)=lambda/2
            A(i,j)=lambda/2
        else
            A(i,j)=0
            B(i,j)=0
        end
    end
end
end

disp(A,B)
for t=1:m
    h=A*w
    h=B*w
end
for i=1:n-1
```

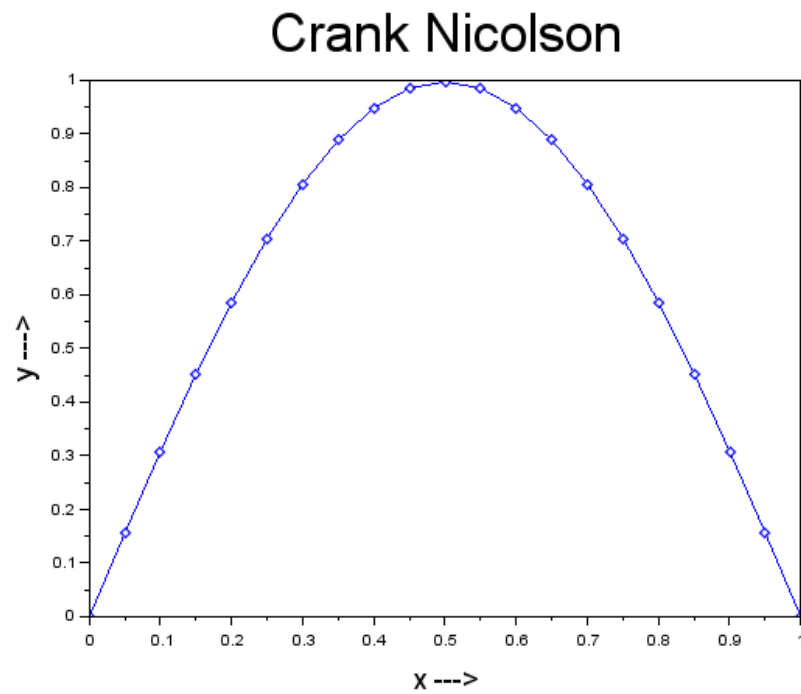
```

    u(i+1)=h(i)
end
for i=1:n+1
    exf(i)=ex(x(i),0.5)
end
disp(x,u)
plot(x,u,'d-')

```

## **Output**

x	u
0.	0.
0.05	0.1560493
0.1	0.3082561
0.15	0.4528726
0.2	0.5863379
0.25	0.7053656
0.3	0.8070249
0.35	0.8888126
0.4	0.9487147
0.45	0.9852563
0.5	0.9975377
0.55	0.9852563
0.6	0.9487147
0.65	0.8888126
0.7	0.8070249
0.75	0.7053656
0.8	0.5863379
0.85	0.4528726
0.9	0.3082561
0.95	0.1560493
1.	0.

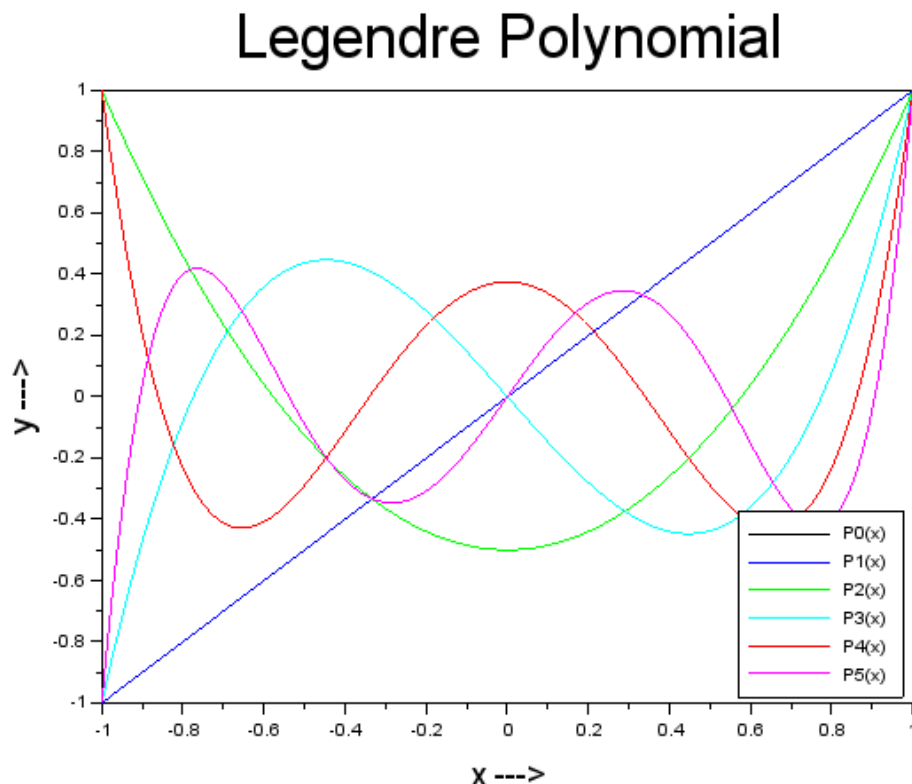


# LEGENDRE POLYNOMIAL

## Program

```
function pl=p(n,x)
    sum = 0
    for m=0:n/2
        den=factorial(m)*factorial(n-m)*(2^n)*factorial(n-2*m)
        sum=sum+((-1)^m)*factorial(2*n-2*m)*(x.^(n-2*m))/den
    end
    pl=sum
endfunction
disp(p(n,x))
clf;
x=-1:0.01:1
for n=0:5
    xlabel("x --->","fontsize",4);
    ylabel("y --->","fontsize",4);
    title("Legendre Polynomial","fontsize",6);
    plot2d(x,p(n,x),n+1)
    hl=legend(['P0(x)'; 'P1(x)'; 'P2(x)'; 'P3(x)'; 'P4(x)'; 'P5(x)';],4);
end
```

## Output



# GAUSS QUADRATURE METHOD

## Program

```
clear;clc;
function [l]=GQ(npt,w,x)
    l = 0
    f = (3/2)*((x.*x).*x)-(x/2)
endfunction
npt = 1
w(1) = 2
x(1) = 0
l = GQ(npt,w,x)
disp("Result from 1 point quadrature = ",l)
npt = 2
w(1) = 1
w(2) = 1
x(1) = -1/sqrt(3)
x(2) = 1/sqrt(3)
I = GQ(npt,w,x)
disp("Result from 2 point quadrature = ",l)
npt = 3
w(1) = 5/9
w(2) = 5/9
w(3) = 8/9
x(1) = -sqrt(3)/5
x(2) = sqrt(3)/5
x(3) = 0
I = GQ(npt,w,x)
disp("Result from 3 point quadrature = ",l)
```

## Output

0.

Result from 1 point quadrature =

0.

Result from 2 point quadrature =

0.

Result from 3 point quadrature =



# LEAST SQUARE FITTING CURVE

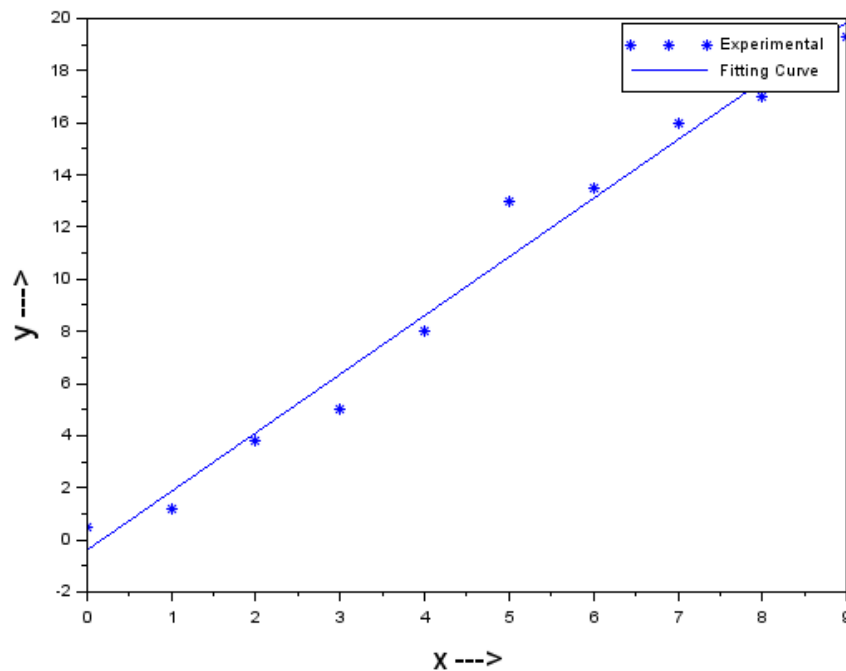
## Program

```
clc;clear;clf;
x = [0,1,2,3,4,5,6,7,8,9]
y = [0.5,1.2,3.8,5,8,13,13.5,16,17,19.3]
n = length(x);
sumx = sum(x)
sumy = sum(y)
sum2x = sum(x.*x)
sum2y = sum(x.*y)
sumxy = sum(x.*y)
c = (sumx*sumxy-sumy*sum2x)/(sumx*sumx-n*sum2x)
m = (sumy-c*n)/sumx
x1 = 0:0.1:9
y1 = m*x1+c
disp(x,y,x1,y1)
plot(x,y,"*", "linewidth",1)
plot(x1,y1,"-", "linewidth",2)
xlabel("x ---->", 'fontsize',4);
ylabel("y ---->", 'fontsize',4);
title("Least Square Fitting Curve", 'fontsize',6);

legend(["Experimental"], ["Fitting Curve"])
```

## Output

### Least Square Fitting Curve



# FOURIER COEFFICIENTS

## Program

```
clc;clear;clf;
L=0
u=2*pi
f='x'
a0=integrate(f,'x',L,u);
n=input("Enter the value of n")
for i = 1:n
    a(i)=integrate('x*cos(i*x)', 'x', L, u, 1e-3)/(%pi)
    b(i)=integrate('x*sin(i*x)', 'x', L, u, 1e-3)/(%pi)
end
function y=f(x)
    y=0
    for i =1:n
        y=y+a(i)*cos(i*x)+b(i)*sin(i*x)
    end
    y=y+a0/2
endfunction

x = -4*pi:0.01:4*pi
disp('a =',a0);
disp('a(n) =',a(n));
disp('b(n) =',b(n));
plot(x,f(x))
xlabel("x ---->","fontsize",4);
ylabel("y ---->","fontsize",4);
title("Fourier Coefficient","fontsize",6);
```

## Output

Enter the value of n2

19.739209

a =

- 3.053D-16

a(n) =

- 1.

b(n) =

