

# Syntax Analysis

## [Chapter 4]

Lectures 11

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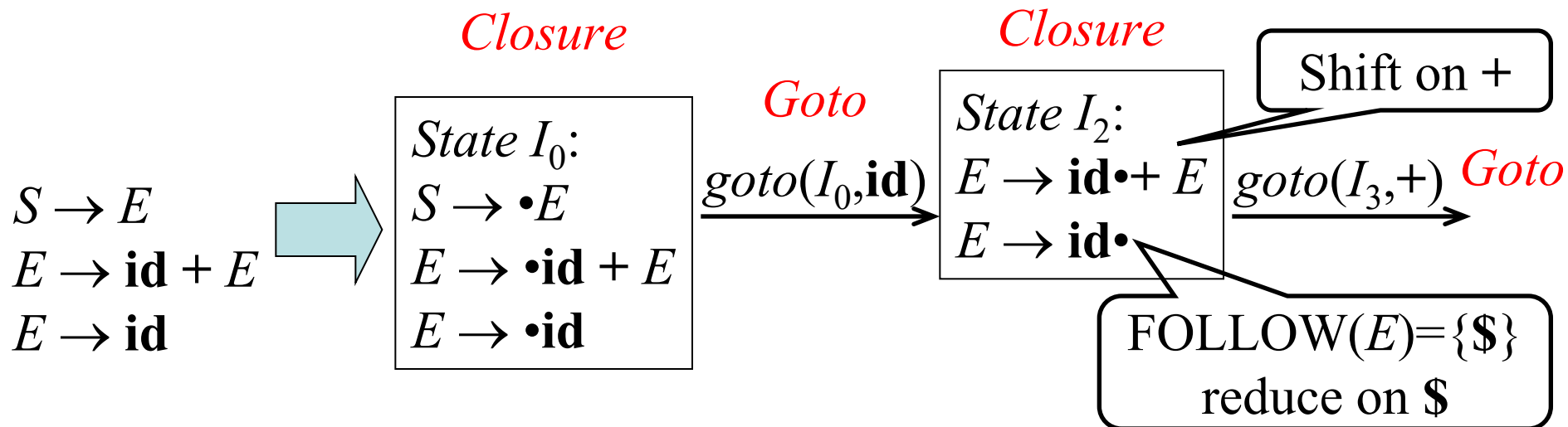
*Adapted from slides by Dr. Robert A. Engelen*

# SLR Grammars

- SLR (**Simple LR**): a simple **extension of LR(0)** automation that used to **eliminate some LR(0) conflicts**.
- LR(0) automation use **0 lookahead** (only considers the current character without reading the next character).
- **SLR extend LR(0) by using Follow(A)**.
- SLR is a kind of lookahead (but not LR(1)).

# SLR Grammars

- **SLR eliminates some conflicts** by populating the parsing table with reductions  $A \rightarrow \alpha$  on symbols in  $\text{FOLLOW}(A)$ . (**it should know follow for all non-terminals**). Example:



# Constructing SLR Parsing Table

- **LR(0) state** is a set of LR(0) items
  - **LR(0) item** is a production with a • (dot) in the right-hand side
1. Build the **LR(0) DFA** by constructing
    - *Closure operation* to construct LR(0) **items**
    - *Goto operation* to determine **transitions**
  2. Construct the **SLR parsing table** from the LR(0) DFA
  3. LR **parser program** uses the SLR parsing table to **determine shift/reduce operations**.

# Constructing SLR Parse Table

1. Extend the grammar with  $S' \rightarrow S$
2. Construct the closure set  $C = \{I_0, I_1, \dots, I_n\}$  of *LR(0) items*
3. If  $[A \rightarrow \alpha \bullet a \beta] \in I_i$  and  $\text{goto}(I_i, a) = I_j$  then set ***action* $[i, a] = \text{shift } j$**  (*a* must be a terminal).
4. If  $[A \rightarrow \alpha \bullet] \in I_i$  then set ***action* $[i, a] = \text{reduce}$**   $A \rightarrow \alpha$  for all  $a \in \text{FOLLOW}(A)$  (**apply only if  $A \neq S'$** )
5. If  $[S' \rightarrow S \bullet]$  is in  $I_i$  then set ***action* $[i, \$] = \text{accept}$**
6. If  $\text{goto}(I_i, A) = I_j$  then set ***goto* $[i, A] = j$**  (for all nonterminals A)
7. Repeat 3-6 until no more entries added

# LR(0) Grammar Items

- *LR(0) item* of a grammar  $G$  is a production of  $G$  with  $\bullet$  at some position of the **right-hand side**
- Example: the following production

$$A \rightarrow X Y Z$$

has 4 items:

$$[A \rightarrow \bullet X Y Z]$$

$$[A \rightarrow X \bullet Y Z]$$

$$[A \rightarrow X Y \bullet Z]$$

$$[A \rightarrow X Y Z \bullet]$$

- Note that production  $A \rightarrow \epsilon$  has **one item**  $[A \rightarrow \bullet]$

# Steps of Constructing the Grammar Items Set <sup>7</sup>

To construct the closure set  $C = \{I_0, I_1, \dots, I_n\}$  of  $LR(0)$  items:

1. The grammar is increased by a new start symbol  $S'$  to represent the production  $S' \rightarrow S$
2. Initially, set  $I_0 = closure(\{[S' \rightarrow \bullet S]\})$   
(this is the start state of the DFA)
3. For each set of items  $I \in C$  and each grammar symbol  $X \in (N \cup T)$  such that  $goto(I, X) \notin C$  and  $goto(I, X) \neq \emptyset$ , add the set of items  $goto(I, X)$  to  $C$
4. Repeat 3 until no more sets can be added to  $C$

# The Closure of LR(0) Items

1. Start with  $\text{closure}(I) = I$
2. If  $[A \rightarrow \alpha \bullet B \beta] \in \text{closure}(I)$  then for each production  $B \rightarrow \gamma$  in the grammar, **add** the item  $[B \rightarrow \bullet \gamma]$  to  $I$  if not already in  $I$
3. Repeat 2 until no new items can be added



# The Goto of LR(0) Items

1. For each item  $[A \rightarrow \alpha \bullet X \beta] \in I$ , add the set of items  $\text{closure}(\{[A \rightarrow \alpha X \bullet \beta]\})$  to  $\text{goto}(I, X)$  if not already included (for grammar symbol  $X$ )
2. Repeat step 1 until no more items can be added to  $\text{goto}(I, X)$

# The Closure of LR(0) Items - Example

Grammar:

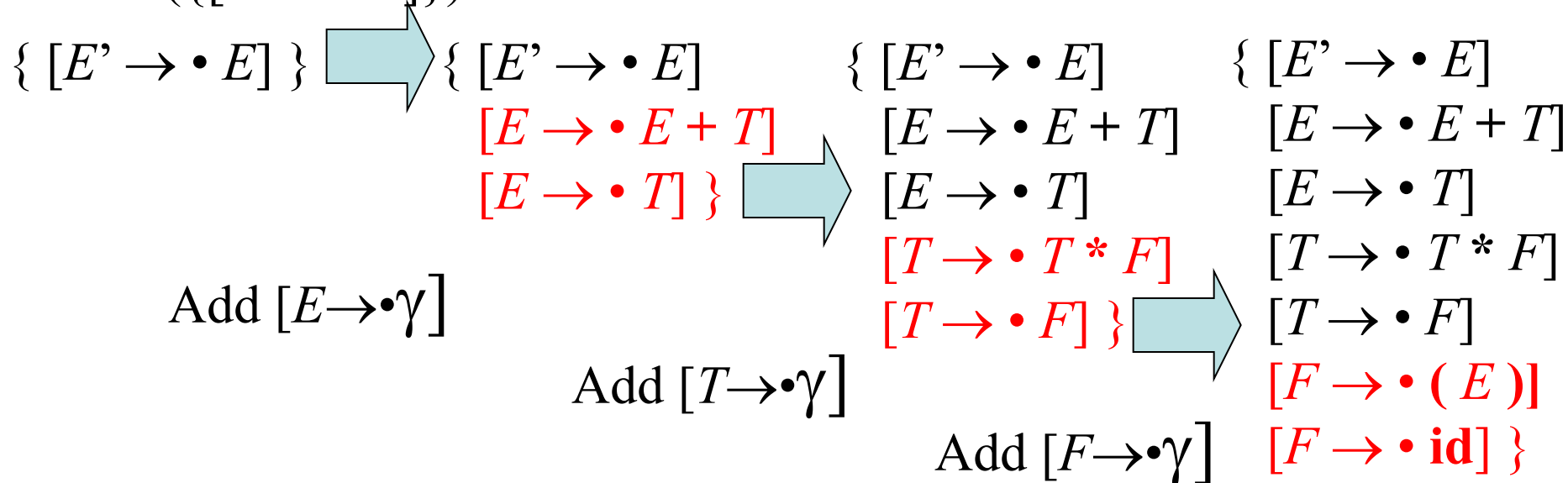
$E \rightarrow E + T \mid T$       *new start symbol  $E'$  is created*

$T \rightarrow T * F \mid F$       *and a new production is added*

$F \rightarrow ( E )$        $E' \rightarrow E$

$F \rightarrow \text{id}$

$\text{closure}(\{[E' \rightarrow \bullet E]\}) =$



# The Goto of LR(0) Items - Example 1

Grammar:

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow ( E )$$

$$F \rightarrow \mathbf{id}$$

Assume Items

of set  $I = \{ [E' \rightarrow \bullet E]$       *Then,*  
 $[E \rightarrow \bullet E + T]$        $\text{goto}(I, E) = \text{closure}(\{[E' \rightarrow E \bullet, E \rightarrow E \bullet + T]\})$   
 $[E \rightarrow \bullet T]$   
 $[T \rightarrow \bullet T * F]$   
 $[T \rightarrow \bullet F]$   
 $[F \rightarrow \bullet ( E )]$   
 $[F \rightarrow \bullet \mathbf{id}] \}$

# The Goto of LR(0) Items - Continue

Grammar:

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow ( E )$$

$$F \rightarrow \mathbf{id}$$

*Assume Items*

*of set*  $I = \{ [E' \rightarrow E \bullet], [E \rightarrow E \bullet + T] \}$

Then,  $\text{goto}(I, +) = \text{closure}(\{[E \rightarrow E + \bullet T]\}) = \{$

- $[E \rightarrow E + \bullet T]$
- $[T \rightarrow \bullet T * F]$
- $[T \rightarrow \bullet F]$
- $[F \rightarrow \bullet ( E )]$
- $[F \rightarrow \bullet \mathbf{id}] \}$

# SLR Grammar - Example

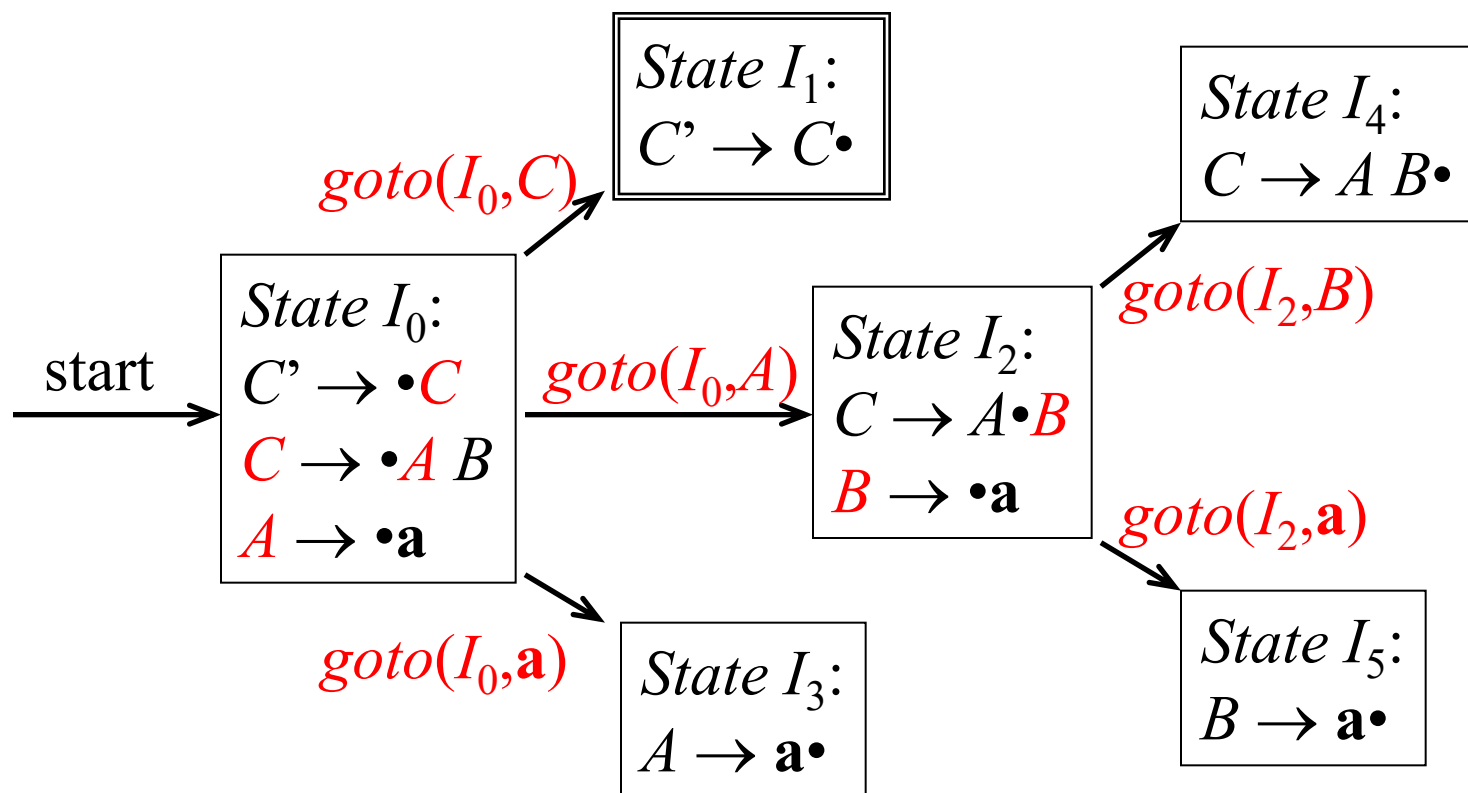
Expanded  
grammar:

1.  $C' \rightarrow C$
2.  $C \rightarrow A B$
3.  $A \rightarrow a$
4.  $B \rightarrow a$

$$I_0 = \text{closure}(\{[C' \rightarrow \bullet C]\})$$

$$I_1 = \text{goto}(I_0, C) = \text{closure}(\{[C' \rightarrow C \bullet]\})$$

...



# Constructing SLR Parse Table

State  $I_0$ :

$$C' \rightarrow \bullet C$$

$$C \rightarrow \bullet A B$$

$$A \rightarrow \bullet a$$

State  $I_1$ :

$$C' \rightarrow C \bullet$$

State  $I_2$ :

$$C \rightarrow A \bullet B$$

$$B \rightarrow \bullet a$$

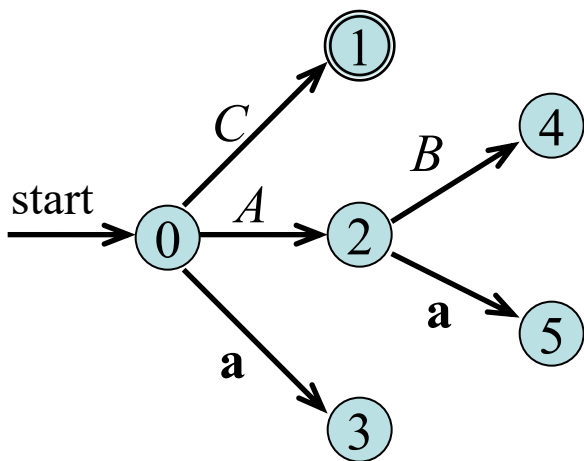
State  $I_3$ :

$$A \rightarrow a \bullet$$

State  $I_4$ :

$$C \rightarrow A B \bullet$$

State  $I_5$ :

$$B \rightarrow a \bullet$$


	a	\$	C	A	B
0	s3		1	2	
1		acc			
2	s5				4
3	r3				
4		r2			
5		r4			

Expanded grammar:

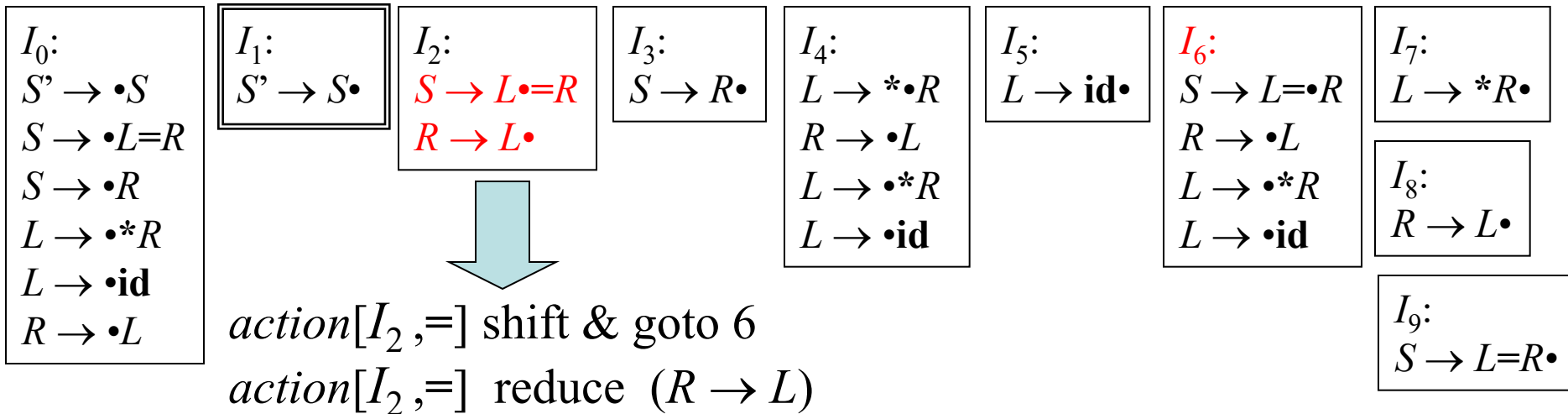
1.  $C' \rightarrow C$
2.  $C \rightarrow A B$
3.  $A \rightarrow a$
4.  $B \rightarrow a$

# SLR and Ambiguity

- Every SLR grammar is unambiguous, but **not** every unambiguous grammar is SLR
- Example: Consider the unambiguous grammar

$$S \rightarrow L = R \mid R$$

$$L \rightarrow * R \mid \text{id}$$

$$R \rightarrow L$$


The  $\text{action}[I_2, =]$  could be shift/reduce entry  $\Rightarrow$  (conflict).

The Grammar is not SLR. Solution is LR(1).

# LR(1) Grammars

- SLR is too simple
- LR(1) parsing uses lookahead to avoid unnecessary conflicts in parsing table
- LR(1) item = LR(0) item + lookahead

$[A \rightarrow \alpha \bullet \beta]$   
LR(0) item

$[A \rightarrow \alpha \bullet \beta, a]$   
LR(1) item

*$a$  has no effect on the item if beta is not Epsilon. But an item  $[A \rightarrow \alpha \bullet, a]$  calls for a reduction by  $[A \rightarrow \alpha]$  only if the next symbol is  $a$ .*



# LR(1) Items Shift/Reduce

- *LR(1) item*  $[A \rightarrow \alpha \bullet \beta, a]$   
contains *lookahead* terminal  $a$ ,  
meaning  $\alpha$  already on top of the stack,  
expect to see  $\beta a$
- For items of the form  $[A \rightarrow \alpha \bullet, a]$   
lookahead  $a$  is used to *reduce*  $A \rightarrow \alpha$   
*only if the next input is  $a$*
- For items of the form  $[A \rightarrow \alpha \bullet \beta, a]$   
with  $\beta \neq \epsilon$  the *lookahead* has no effect

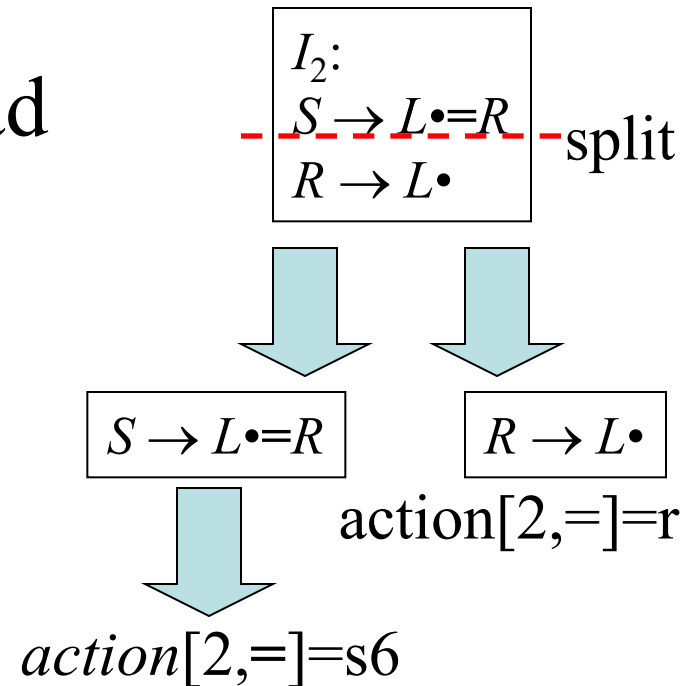
# LR(1) Ambiguity Elimination

- Split the SLR states by adding LR(1) lookahead

- Grammar

$$S \rightarrow L = R \mid R$$

$$L \rightarrow * R \mid \text{id}$$

$$R \rightarrow L$$


If the next input (lookahead) is “=”, don’t reduce because **no right-sentential form of the grammar begins with  $=R$**

# Constructing LR(1) Items - Example

- Construct the LR(1) items for the following grammar:

$$S \rightarrow C C$$

$$C \rightarrow c C \mid d$$

1. Expand the grammar with  $S' \rightarrow S$
2. LR(1) items (**next slide**)

$I_0$ :  $[S' \rightarrow \bullet S, \$]$       goto( $I_0, S$ ) =  $I_1$   
 $[S \rightarrow \bullet CC, \$]$       goto( $I_0, C$ ) =  $I_2$   
 $[C \rightarrow \bullet cC, c/d]$       goto( $I_0, c$ ) =  $I_3$   
 $[C \rightarrow \bullet d, c/d]$       goto( $I_0, d$ ) =  $I_4$

LR(1) grammar:

$S \rightarrow C \underline{C}$

$C \rightarrow c \underline{C} \mid d$

$I_1$ :  $[S' \rightarrow S \bullet, \$]$

$[S \rightarrow C \bullet C, \$]$       goto( $I_2, C$ ) =  $I_5$   
 $I_2$ :  $[C \rightarrow \bullet cC, \$]$       goto( $I_2, c$ ) =  $I_6$   
 $[C \rightarrow \bullet d, \$]$       goto( $I_2, d$ ) =  $I_7$

$I_3$ :  $[C \rightarrow c \bullet C, c/d]$       goto( $I_3, d$ ) =  $I_8$   
 $[C \rightarrow \bullet cC, c/d]$       goto( $I_3, c$ ) =  $I_6$   
 $[C \rightarrow \bullet d, c/d]$       goto( $I_3, C$ ) =  $I_7$

$I_4$ :  $[C \rightarrow d \bullet, c/d]$

$I_5$ :  $[C \rightarrow CC \bullet, \$]$

$I_6$ :  $[C \rightarrow c \bullet C, \$]$       goto( $I_6, C$ ) =  $I_9$   
 $[C \rightarrow \bullet cC, \$]$       goto( $I_6, c$ ) =  $I_6$   
 $[C \rightarrow \bullet d, \$]$       goto( $I_6, d$ ) =  $I_7$

$I_7$ :  $[C \rightarrow d \bullet, \$]$

$I_8$ :  $[C \rightarrow cC \bullet, c/d]$

$I_9$ :  $[C \rightarrow cC \bullet, \$]$

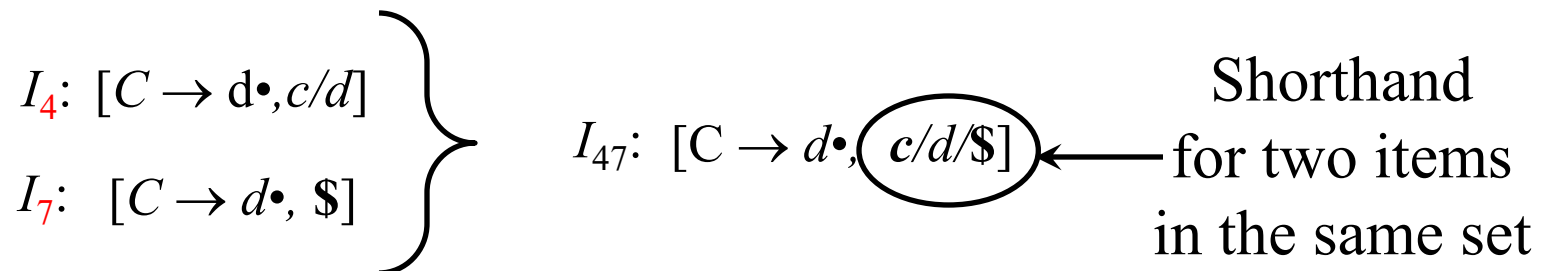


# (LookAhead LR) LALR(1) Parsing Grammars<sup>21</sup>

- Its table is smaller than LR(1)
- LR(1) parsing tables have many states
- LALR(1) combines LR(1) states to reduce table size
- Less powerful than LR(1)
  - Will not introduce shift-reduce conflicts, because shifts don't use lookaheads
  - May introduce reduce-reduce conflicts, but not often for grammars of programming languages.

# Constructing LALR(1) Parsing Tables

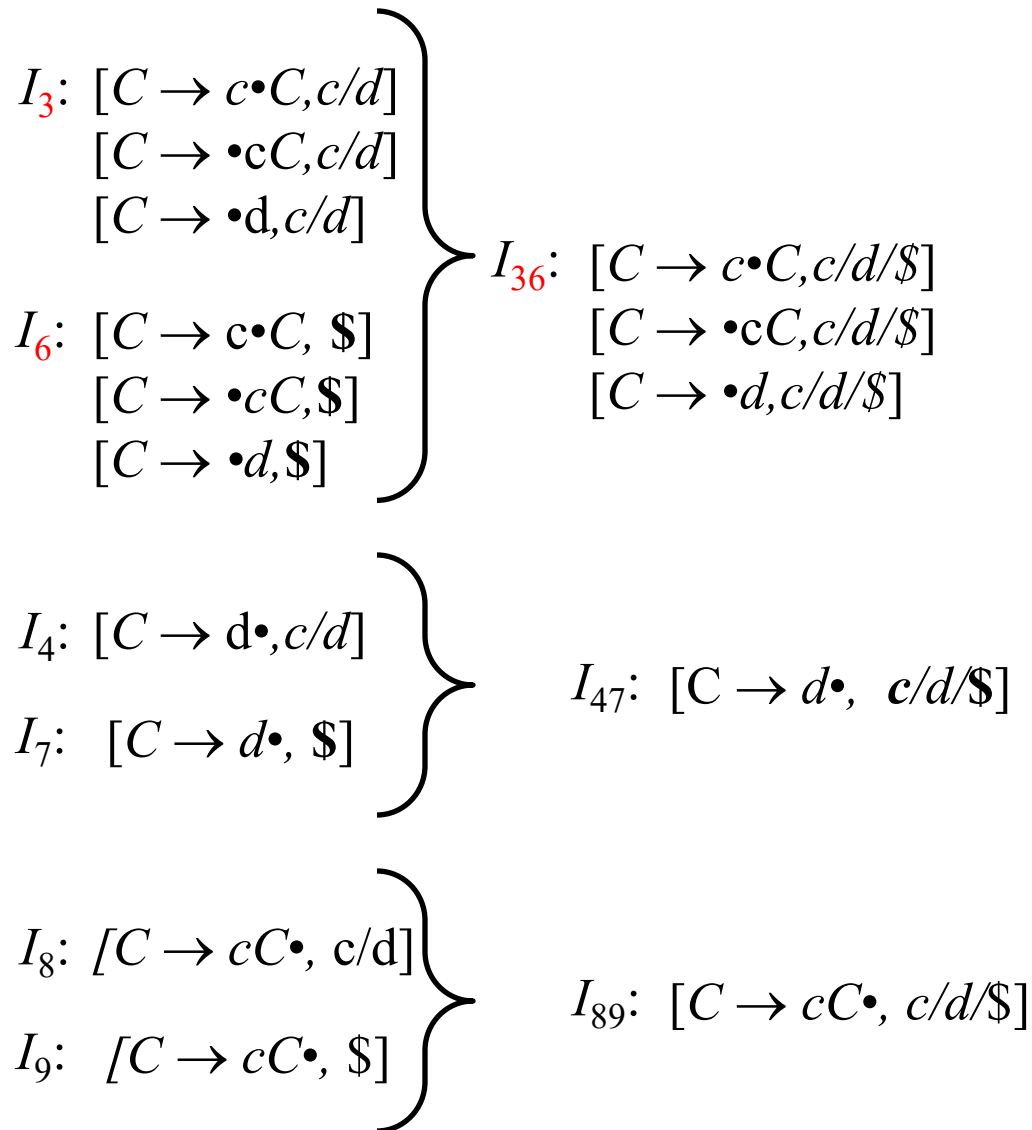
1. Construct sets of LR(1) items
2. **Combine LR(1) sets** with sets of items that share the same first part



# Constructing LALR(1) Parse Table - Example

- LR(1) grammar:  
$$S \rightarrow C C$$
$$C \rightarrow c C \mid d$$
- Augment with  $S' \rightarrow S$
- **LALR(1) items** (next slide)

# Constructing LALR(1) Parse Table





# LALR(1) Parse Table

Grammar:

1.  $S \rightarrow C C$

2.  $C \rightarrow c C$

3.  $C \rightarrow d$

	$c$	$d$	$\$$	$S$	$C$
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

# LL, SLR, LR, LALR Summary

- **LL** parse tables computed using **FIRST/FOLLOW**
  - Nonterminals  $\times$  terminals  $\rightarrow$  productions
- **LR** parsing tables computed using **closure/goto**
  - LR states  $\times$  terminals  $\rightarrow$  shift/reduce actions
  - LR states  $\times$  nonterminals  $\rightarrow$  goto state transitions
- A **grammar is considered**
  - **LL(1)** if its LL(1) parse table has no conflicts
  - **LR(1)** if its LR(1) parse table has no conflicts
  - **SLR** if its SLR parse table has no conflicts
  - **LALR(1)** if its LALR(1) parse table has no conflicts

# LL, SLR, LR, LALR Summary

- Almost all programming languages have LR grammars
- LR is more powerful than LL.

*(i.e, every  $LL(1)$  grammar is also both  $LALR(1)$  and  $LR(1)$ , but not vice versa).*

- **LR grammar** is usually easier to understand than the corresponding LL grammar.
- **LR parser** itself is harder to understand and to write (thus, LR parsers are built using parser generators, rather than being written by hand).