

Internal Memory

HAMMING CODE

↳ to check error for data

- ↳ 9. Suppose an 8 bit data word stored in memory is 11000010. Using the Hamming algorithm, determine what check bits would be stored in memory with the data word. Show how you got your answer.

calculate parity bit, P needed

$$2^p \geq m + p$$

\uparrow number of bits \uparrow number of redundant bits

$$2^4 \geq 8 + 4$$

$$16 \geq 12$$

from msb →

$\begin{matrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ P_1 & P_2 & 1 & P_3 & 1 & 0 & 0 & P_4 & 0 & 0 & 1 & 0 \end{matrix}$
 } original bits + parity bits

$\begin{matrix} 2^1 & 2^2 & & 2^3 & & & & 2^4 \end{matrix}$

* in reverse

* default even parity bits

add to become even

	C_1	C_2	C_3	C_4	
0	0	0	0	0	
1	0	0	0	<u>1</u>	need 1 to become even
2	0	0	<u>1</u>	0	1
3	0	0	<u>1</u>	<u>1</u>	0 → need 0 to become even
4	0	<u>1</u>	0	0	1
5	0	<u>1</u>	0	<u>1</u>	0
6	0	<u>1</u>	<u>1</u>	0	0
7	0	<u>1</u>	<u>1</u>	<u>1</u>	1
8	<u>1</u>	0	0	0	1

$$\begin{aligned}
 P_1 &= C_4(1, 3, 5, 7) \Rightarrow 1001 = 0 \text{ (even)} \\
 P_2 &= C_3(2, 3, 7, 8) \Rightarrow 1001 = 0 \text{ (even)} \\
 P_3 &= C_2(4, 5, 6, 7) \Rightarrow 0001 = 1 \text{ (odd)} \\
 P_4 &= C_1(8) \Rightarrow 0 = 0 \text{ (even)}
 \end{aligned}$$

$$\Rightarrow \begin{matrix} P_1 & P_2 & & P_3 & & & & P_4 \end{matrix}$$

$$\Rightarrow 0 \quad 0 \quad 1 \quad 1 \quad 1 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 1 \quad 0_2$$

* only till 8 bits
09 bit = 8

anti aah?
tanya