

Feb 10, 25

ungrouped data:

, Mean :

$$\mu, \bar{X}$$

, Trimmed Mean:

$$U_{\text{trim}}, \bar{X}_{\text{trim}}$$

Measures of  
skewness

↳ outliers

, Median:

$$\tilde{\mu}, \tilde{X}$$

, Mode:

$$\hat{\mu}, \hat{X}$$

$$\text{Range} = R = X_m - X_o$$

absolute  
↳ same unit

At the Coefficient of dispersion

$$= \frac{\text{Range}}{X_m + X_o}$$

$$V_{\text{er}} = S^2 = \frac{\sum (X - \bar{X})^2}{n-1}$$

$$S \cdot d = \sigma = \sqrt{V_{\text{er}}}$$

$$C.V = \left( \frac{S \cdot d}{\text{Mean}} \times 100 \right) \%$$

$$Q_1$$



$$P_{25}$$

$$Q_2$$



$$P_{50}$$

$$Q_3$$



$$P_{75}$$

$$i = \left( \frac{P}{100} \right) \times \text{total obs.}$$

→ integer :  $\frac{i + (i+1) \text{ value}}{2}$

→ not an integer: Round up  $i$ th observation.

$$Q_1 = 0.25 \times \text{total no. of observation.}$$

$$Q_2 = \text{median} = P_{50} = 0.50 \times \text{total}$$

$$P_{75} = Q_3 = 0.75 \times$$

$$P_{80} = 0.80 \times \text{total..}$$

$$\text{IQR} = Q_3 - Q_1$$

$$\text{Coef. of Q. Dev} = \frac{\text{IQR}}{Q_3 + Q_1}$$

$$\text{Semi IQR} = \text{IQR}/2.$$

## Data:

Range has significant limitations:

- Sensitive to outliers,
- Variance & S.D consider all the pts
- Var. & S.D are more consistent & reliable

if naturally  
outliers  
exists & median/  
trimmed  
mean

Question:

data of 12 graduates

3450, 3550, 3650,  
3480, 3355, 3310, 3490, 3730  
3540, 3925, 3520, 3480.

Sorted data:

3310, 3450, 3480, 3480, 3490,  
3520, 3540, 3925, 3550, 3650,  
3730, 3925.

1) mean = 3540

2) Trimmed mean:  
20%.

10%

10%

10% of 12 observations = 1.2.1.  
round off to 1  
drop 1, 1 values from both sides

Trimmed mean =  $\frac{\sum X_{\text{trim}}}{n_{\text{trim}}} = 3524.5$

3) Median:

Even:  $\left(\frac{n}{2}\right)^{\text{th}} + \left(\frac{n}{2} + 1\right)^{\text{th}} = \frac{6^{\text{th}} + 7^{\text{th}}}{2}$

odd:  $\frac{n+1}{2}^{\text{th}}$  2 =  $\frac{3490 + 3520}{2}$   
3505

8.4 10.2 11.5 11.8 10.0 12.2 12.5 11.1  
 10.0 12.2 9.8 9.5 11.5 11.8 14.9 15.1 10.0 9.0  
 15.8 11.5

<sup>4)</sup> mode: Most Frequent = 3480

Range:

$$X_m - X_o = 3925 - 3310 \\ = 615$$

Coef. of Dispersion:

$$= \frac{\text{Range}}{X_m + X_o} = \frac{615}{7235} = 0.085$$

$$P_{25} = Q_1 = 0.25 \times 12 = 3 \\ = \frac{3\text{rd} + 4\text{th}}{2} = 3465 - \left( \frac{3450 + 3480}{2} \right)$$

$$PQ_2 = 0.50 \times 12 = 6 \\ = \frac{6\text{th} + 7\text{th}}{2}$$

$$Q_3 = 0.75 \times 12 = 9 = \\ = \frac{9\text{th} + 10\text{th}}{2} = \frac{3550 + 3650}{2} \\ = 3600$$

$$P_{80} = 0.80 \times 12 = 9.6 = 10\text{th value.} \\ 3650.$$

$$IQR = Q_3 - Q_1 = 3600 - 3465 \\ = 135$$

$$\text{Semi-IQR} : \frac{IQR}{2} =$$

$$\text{cof of Q. Dev} = \frac{IQR}{Q_3 + Q_1}$$

mean > median > mode  
 ↳ +ively skewed.

mean = med. = mode  
 ↳ symmetrical

mean < med < mod  
 ↳ -ively skewed.

Pearson's cof. of Skewness :

$$\rightarrow Sk = \frac{\text{mean} - \text{mode}}{S.d.}$$

$$\star \text{mode} = 3 \text{median} - 2 \text{mean}$$

$$Sk = \frac{\text{mean} - 3\text{med} + 2\text{medn}}{S.d.}$$

can be determine  
 H.S. program left -3 to +3 → skewed  
 mean med. right.  
 Pearson's 3mean - 3med  
 s.d. =  $\sqrt{\text{Box whisker plot}}$   
 $\rightarrow S_k = \frac{3(\text{mean} - \text{median})}{\text{s.d.}}$  exact  
 slowness.

$$s^2 = \frac{3(3540 - 3505)}{165.65} = 0.63$$

	X	$(X - \bar{X})^2$
1)	3310	52900.
2)	3355	34225
3)	3450	8100
4)	3480	3600
5)	3480	3600
6)	3490	2500
7)	3520	400
8)	3540	0
9)	3550	12000
10)	3650	36100
11)	3730	148225.
12)	3925	19 301850 11

$$= 27440.91$$

$$\text{Var} = 27440.91$$

$$s_d = \sqrt{\text{Var}} = 165.65$$

For outliers

- ↳ Box & W Plot
- ↳ Z-Scores

biggest  
outlier  
+/-  
upper right  
lower left

Skewness

- histogram
- mean / mode / median
- Pearson's
- Box & Whisker's Plot.

→ Five Point Summary:

Min	$Q_1$	Med	$Q_3$	Max
3310.	3465	3505	3600	3925

Fences:

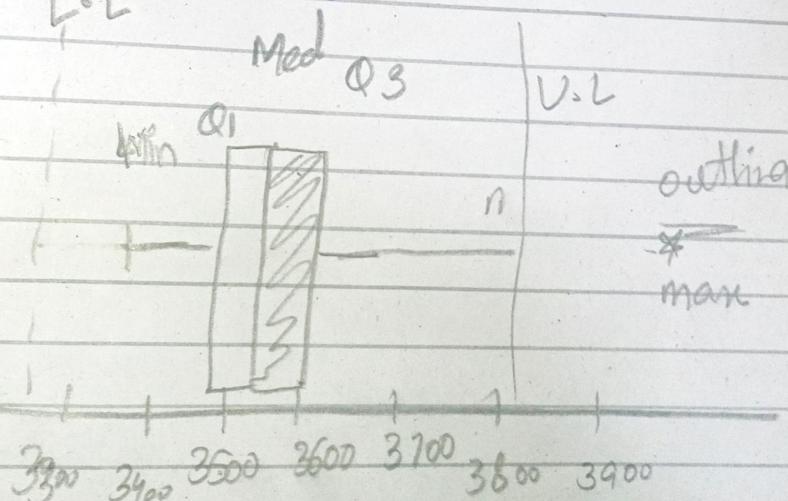
$$U.L = Q_3 + 1.5(IQR)$$

$$= 3600 + 1.5(135)$$

$$= 3802.5$$

$$L.L = Q_1 - 1.5(IQR) = 3465 - 1.5(135)$$

$$= 3262.5$$



# Machine learning ↳ anomaly.

Z-scores:

$$Z_i = \frac{X - \text{mean}}{S \cdot d}$$

Sample :  $\frac{X - \bar{X}}{S}$

pop :  $\frac{X - U_x}{S_x}$

if  $Z_i$  lies b/w -3 to +3, then there is no outlier in data.

$Z \sim \text{mean} = 0$   
 $S \cdot d = 1$