

CUDA SDK — LIBRARIES, NUMERICAL ACCURACY

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→ <https://tinyurl.com/cudafordummies/ii/l4/notes-l4.pdf>

TO THE FORTRAN-MINDED

CUBLAS

CUSOLVER

MORE LIBRARIES

NUMERICAL ACCURACY & PERFORMANCE

5_DOMAIN_SPECIFIC/MARCHINGCUBES

PROFILING CUDA CODE

HIP

TAKE HOME MESSAGES

TO THE FORTRAN-MINDED

CUDA SDK

- Fortran is the language of choice in many scientific code development projects

TO THE FORTRAN-MINDED

CUDA SDK

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- Professional coverage from the NVIDIA hpc SDK — formerly portland group compilers — now an entire suite of compilers, libraries and developmental tools

→ <https://developer.nvidia.com/hpc-sdk>

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- Install and load the module to get ready
- ```
cuda-zen sh@n3073-004:~$ module purge
cuda-zen sh@n3073-004:~$ module load nvhpc/25.1-gcc-9.5.0-efr6qch
```

# TO THE FORTRAN-MINDED CONT.

## CUDA SDK CONT.

### vecadd.cuf

```
! host
program t1
use cudafor
use myvecadd
 integer, parameter :: n = 100
 integer :: i
 real, allocatable, device :: da(:), db(:), dc(:)
 real :: ha(n), hb(n), hc(n)
 istat = cudaSetDevice(0)
 allocate(da(n))
 ...
 da = ha
 ...
 call vecadd<<< 1, n >>>(da, db, dc)
 ha = da
 ...
 deallocate(da)
 ...
end program t1
```

```
! kernel
module myvecadd
contains
attributes(global) &
subroutine vecadd(a, b, c)
 integer :: i
 real :: a(*), b(*), c(*)

 i = (blockidx%x-1) * blockdim%x + threadidx%x
 c(i) = a(i) + b(i)
end subroutine vecadd
end module myvecadd
```

→ <https://tinyurl.com/cudafordummies/ii/l4/vecadd.cuf>

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## CUDA SDK CONT.

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Select GPU 0

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...
da = ha
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call vecadd<<< 1, n >>>>(da, db, dc)
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end program t1
```

Select GPU 0

Simple  
htod/dtoh  
copies

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Slightly different syntax

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end subroutine vecadd
end module myvecadd
```

Slightly different syntax

Fortran counting  
1,2,3...

→ <https://tinyurl.com/cudafordummies/ii/14/vecadd.cuf>

# TO THE FORTRAN-MINDED CONT.

## CUDA SDK CONT.

```
cuda-zen sh@n3073-004:~$ nvfortran vecadd.cuf
cuda-zen sh@n3073-004:~$./a.out
```

|       |          |          |          |
|-------|----------|----------|----------|
| 1     | 1.000000 | 99.00000 | 100.0000 |
| 2     | 2.000000 | 98.00000 | 100.0000 |
| 3     | 3.000000 | 97.00000 | 100.0000 |
| 4     | 4.000000 | 96.00000 | 100.0000 |
| 5     | 5.000000 | 95.00000 | 100.0000 |
| ..... |          |          |          |
| 98    | 98.00000 | 2.000000 | 100.0000 |
| 99    | 99.00000 | 1.000000 | 100.0000 |
| 100   | 100.0000 | 0.000000 | 100.0000 |

→ <https://tinyurl.com/cudafordummies/ii/l4/vecadd.cuf>

# TO THE FORTRAN-MINDED CONT.

CUDA SDK CONT.

- Frequently — only a single Fortran subroutine/function needs to be ported

→ <https://www.pgroup.com/resources/docs/18.4/pdf/pgi18cudaforug.pdf>

# TO THE FORTRAN-MINDED CONT.

## CUDA SDK CONT.

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## CUDA SDK CONT.

- Frequently — only a single Fortran subroutine/function needs to be ported
- Basic feasibility studies can already be done with the help of short C routines called from Fortran
- The usual Fortran $\leftrightarrow$ C interfacing rules apply
- Memory management is more complicated, would prefer `cudaMallocManaged()`

# TO THE FORTRAN-MINDED CONT.

## CUDA SDK CONT.

### fvcadd.f

```
PROGRAM FVCADD
IMPLICIT NONE
INTEGER N
PARAMETER (N = 100)
INTEGER I
REAL A(N), B(N), C(N)

DO I=1, N
 A(I) = REAL(I)
 B(I) = REAL(N) - REAL(I)
 C(I) = REAL(0)
ENDDO

CALL NTMDTR(A, B, C, N)

DO I=1, N
 WRITE(6, '(I6F12.6)') I, C(I)
ENDDO

END
```

### ntmdtr.cu

```
__global__ void VecAdd(float *A, float *B, float *C)
{
 int i = threadIdx.x;
 C[i] = A[i] + B[i];
}

extern "C" void ntmdtr_(float *A, float *B, float *C, int *N)
{
 dim3 numBlocks, threadsPerBlock;
 float *AD, *BD, *CD;
 threadsPerBlock.x = *N;
 numBlocks.x = 1;
 cudaMalloc((void **) &AD, (*N) * sizeof(float));
 cudaMalloc((void **) &BD, (*N) * sizeof(float));
 cudaMalloc((void **) &CD, (*N) * sizeof(float));
 cudaMemcpy(AD, A, (*N) * sizeof(float), cudaMemcpyHostToDevice);
 cudaMemcpy(BD, B, (*N) * sizeof(float), cudaMemcpyHostToDevice);
 cudaMemcpy(CD, C, (*N) * sizeof(float), cudaMemcpyHostToDevice);
 VecAdd <<< numBlocks, threadsPerBlock >>> (AD, BD, CD);
 cudaDeviceSynchronize();
 cudaMemcpy(C, CD, (*N) * sizeof(float), cudaMemcpyDeviceToHost);
 cudaFree(AD);
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 return;
}
```

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```

Intermediator in C

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```

Trailing underscore !

Intermediator in C

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Trailing underscore !

Call by Reference

Intermediator in C

# TO THE FORTRAN-MINDED CONT.

## CUDA SDK CONT.

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 cudaDeviceSynchronize();
 cudaMemcpy(C, CD, (*N) * sizeof(float), cudaMemcpyDeviceToHost);
 cudaFree(AD);
 cudaFree(BD);
 cudaFree(CD);
 return;
}
```

Trailing underscore !

Call by Reference

Intermediator in C

Extra data transfer ↔

# TO THE FORTRAN-MINDED CONT.

## CUDA SDK CONT.

```
cuda-zen sh@n3073-004:~$ ls
fvcadd.f ntmctr.cu

cuda-zen sh@n3073-004:~$ gfortran -c fvcadd.f
cuda-zen sh@n3073-004:~$ nvcc -c ntmctr.cu
cuda-zen sh@n3073-004:~$ nvcc fvcadd.o ntmctr.o -lcudart -lgfortran
cuda-zen sh@n3073-004:~$./a.out

 1 100.000000
 2 100.000000
 3 100.000000
 4 100.000000
 5 100.000000
 6 100.000000
 7 100.000000
 ...
 98 100.000000
 99 100.000000
100 100.000000
```

→ <https://www.olcf.ornl.gov/tutorials/compiling-mixed-gpu-and-cpu-code>

→ <https://tinyurl.com/cuda4dummies/ii/l4/fvcadd.f>

→ <https://tinyurl.com/cuda4dummies/ii/l4/ntmctr.cu>

# TO THE FORTRAN-MINDED CONT.

## CUDA SDK CONT.

```
cuda-zen sh@n3073-004:~$ ls
```

```
fvcadd.f ntmldr.cu
```

```
cuda-zen sh@n3073-004:~$
```

```
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```

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```
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```
gfortran -c fvcadd.f
```

```
nvcc -c ntmldr.cu
```

```
nvcc fvcadd.o ntmldr.o -lcudart -lgfortran
```

```
./a.out
```

Name mangling 2b considered !

```
1 100.000000
```

```
2 100.000000
```

```
3 100.000000
```

```
4 100.000000
```

```
5 100.000000
```

```
6 100.000000
```

```
7 100.000000
```

```
....
```

```
98 100.000000
```

```
99 100.000000
```

```
100 100.000000
```

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→ <https://tinyurl.com/cudafordummies/ii/l4/fvcadd.f>

→ <https://tinyurl.com/cudafordummies/ii/l4/ntmdtr.cu>

# TO THE FORTRAN-MINDED CONT.

## CUDA SDK CONT.

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cuda-zen sh@n3073-004:~$ ls
```

```
fvcadd.f ntmdtr.cu
```

```
cuda-zen sh@n3073-004:~$
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```
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```
nvcc -c ntmdtr.cu
```

```
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```
./a.out
```

Name mangling 2b considered !

C++ like compiler !

```
1 100.000000
2 100.000000
3 100.000000
4 100.000000
5 100.000000
6 100.000000
7 100.000000
...
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99 100.000000
100 100.000000
```

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# TO THE FORTRAN-MINDED CONT.

## CUDA SDK CONT.

- Type analogues,  
int  $\leftrightarrow$  INTEGER  
float  $\leftrightarrow$  REAL  
double  $\leftrightarrow$  DOUBLE PRECISION
- Name mangling: compiling Fortran code will alter names of called subroutines/function by adding a trailing underscore, \_ Therefore C-functions will need to be aware of this and add this underscore ahead of time
- Fortran uses column-major order for storing multidimensional arrays while C uses row-major order
- Linking may need the addition of -lcudart -lgfortran etc

→ [http://www.computationalmathematics.org/topics/files/calling\\_cuda\\_from\\_fortran.html](http://www.computationalmathematics.org/topics/files/calling_cuda_from_fortran.html)

- BLAS/LAPACK are among the most widely used libraries in scientific computing

# CUBLAS

CUDA SDK CONT.

- BLAS/LAPACK are among the most widely used libraries in scientific computing
- General tasks in linear algebra with systematic naming scheme and a focus on high performance computing

→ <http://www.netlib.org/blas/>

# CUBLAS

CUDA SDK CONT.

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- General tasks in linear algebra with systematic naming scheme and a focus on high performance computing
- Standard API for many prominent implementations (MKL, OpenBLAS, ATLAS...)

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- General tasks in linear algebra with systematic naming scheme and a focus on high performance computing
- Standard API for many prominent implementations (MKL, OpenBLAS, ATLAS...)
- Originally written in Fortran

# CUBLAS CONT.

## CUDA SDK CONT.

**S** real, single precision

**D** real, double precision

**C** complex, single precision

**Z** complex, double precision

**DGEMM(...)**

→ <http://www.netlib.org/blas/>

# CUBLAS CONT.

## CUDA SDK CONT.

S real, single precision

D real, double precision

C complex, single precision

Z complex, double precision



DGEMM(...)

# CUBLAS CONT.

## CUDA SDK CONT.

**SY** symmetric

**HE** Hermitian

**HP** Hermitian packed **TP** triangular packed

**SP** symmetric packed

**GB** general band

**HB** Hermitian band **TB** triangular band

**SB** symmetric band

**GE** general

**TR** triangular

**S** real, single precision

**D** real, double precision

**C** complex, single precision

**Z** complex, double precision



**DGE MM(...)**

# CUBLAS CONT.

## CUDA SDK CONT.

|                            |                        |                            |                             |
|----------------------------|------------------------|----------------------------|-----------------------------|
| <b>SY</b> symmetric        | <b>HE</b> Hermitian    | <b>HP</b> Hermitian packed | <b>TP</b> triangular packed |
| <b>SP</b> symmetric packed | <b>GB</b> general band | <b>HB</b> Hermitian band   | <b>TB</b> triangular band   |
| <b>SB</b> symmetric band   | <b>GE</b> general      | <b>TR</b> triangular       |                             |

**S** real, single precision

**D** real, double precision

**C** complex, single precision

**Z** complex, double precision

**DGEMM(...)**

**MV** matrix · vector

**SV** syst eq. 1 vec unk

**R** rank-1 matrix update

**R2** rank-2 matrix update

**MM** matrix · matrix

**SM** syst eq. matrix unk

**C** conjugate vector

**G** Givens rotation

**MG** mod. Givens rot constr

**RK** rank-k matrix update

**R2K** rank-2k matrix update

**U** unconjugate vector

**M** modified Givens rot

→ <http://www.netlib.org/blas/>

# CUBLAS CONT.

## CUDA SDK CONT.

```
...
DGEMM(TRANSA, TRANSB, M, N, K, ALPHA, A, LDA, B, LDB, BETA, C, LDC)
...

...
Atype = Btype = 'T';
Adim = Bdim = Cdim = n;
alpha = (double) 1;
beta = (double) 0;
info = dgemm(&Atype, &Btype, &Adim, &Bdim, &Cdim, &alpha,
 &A[0], &Adim, &B[0], &Bdim, &beta, &C[0], &Cdim);
if (info != 0) {
 printf("blas error in dgemm returning %d\n", info);
 exit(99);
}
...

...
stat = cublasDgemm (handle, dev_Atype, dev_Btype, Adim, Bdim, Cdim, &alpha,
 dev_ptr_A, Adim, dev_ptr_B, Bdim, &beta, dev_ptr_C, Cdim);
if (stat != CUBLAS_STATUS_SUCCESS) {
 printf("cublas error in dgemm \n");
 exit(99);
}
```

→ <http://www.netlib.org/blas/>

# CUBLAS CONT.

## CUDA SDK CONT.

```
...
DGEMM(TRANSA, TRANSB, M, N, K, ALPHA, A, LDA, B, LDB, BETA, C, LDC)
...

...
Atype = Btype = 'T';
Adim = Bdim = Cdim = n;
alpha = (double) 1;
beta = (double) 0;
info = dgemm(&Atype, &Btype, &Adim, &Bdim, &Cdim, &alpha,
 &A[0], &Adim, &B[0], &Bdim, &beta, &C[0], &Cdim);
if (info != 0) {
 printf("blas error in dgemm returning %d\n", info);
 exit(99);
}
...

...
stat = cublasDgemm (handle, dev_Atype, dev_Btype, Adim, Bdim, Cdim, &alpha,
 dev_ptr_A, Adim, dev_ptr_B, Bdim, &beta, dev_ptr_C, Cdim);
if (stat != CUBLAS_STATUS_SUCCESS) {
 printf("cublas error in dgemm \n");
 exit(99);
}
```

gfortran ... -lblas

→ <http://www.netlib.org/blas/>

# CUBLAS CONT.

## CUDA SDK CONT.

```
...
DGEMM(TRANSA, TRANSB, M, N, K, ALPHA, A, LDA, B, LDB, BETA, C, LDC)
...
```

gfortran ... -lblas

```
...
Atype = Btype = 'T';
Adim = Bdim = Cdim = n;
alpha = (double) 1;
beta = (double) 0;
info = dgemm(&Atype, &Btype, &Adim, &Bdim, &Cdim, &alpha,
 &A[0], &Adim, &B[0], &Bdim, &beta, &C[0], &Cdim);
if (info != 0) {
 printf("blas error in dgemm returning %d\n", info);
 exit(99);
}
...
```

gcc -Ddgemm=dgemm\_ ... -lblas

```
...
stat = cublasDgemm (handle, dev_Atype, dev_Btype, Adim, Bdim, Cdim, &alpha,
 dev_ptr_A, Adim, dev_ptr_B, Bdim, &beta, dev_ptr_C, Cdim);
if (stat != CUBLAS_STATUS_SUCCESS) {
 printf("cublas error in dgemm \n");
 exit(99);
}
```

# CUBLAS CONT.

## CUDA SDK CONT.

```
...
DGEMM(TRANSA, TRANSB, M, N, K, ALPHA, A, LDA, B, LDB, BETA, C, LDC)
...
```

gfortran ... -lblas

```
...
Atype = Btype = 'T';
Adim = Bdim = Cdim = n;
alpha = (double) 1;
beta = (double) 0;
info = dgemm(&Atype, &Btype, &Adim, &Bdim, &Cdim, &alpha,
 &A[0], &Adim, &B[0], &Bdim, &beta, &C[0], &Cdim);
if (info != 0) {
 printf("blas error in dgemm returning %d\n", info);
 exit(99);
}
...
```

gcc -Ddgemm=dgemm\_ ... -lblas

```
...
stat = cublasDgemm (handle, dev_Atype, dev_Btype, Adim, Bdim, Cdim, &alpha,
 dev_ptr_A, Adim, dev_ptr_B, Bdim, &beta, dev_ptr_C, Cdim);
if (stat != CUBLAS_STATUS_SUCCESS) {
 printf("cublas error in dgemm \n");
 exit(99);
}
}
```

nvcc ... -lcublas

# CUBLAS CONT.

## CUDA SDK CONT.

col-wise  
linearized  
matrices;  
∀ pointers

```
...
DGEMM(TRANSA, TRANSB, M, N, K, ALPHA, A, LDA, B, LDB, BETA, C, LDC)
...
```

gfortran ... -lblas

```
...
Atype = Btype = 'T';
Adim = Bdim = Cdim = n;
alpha = (double) 1;
beta = (double) 0;
info = dgemm(&Atype, &Btype, &Adim, &Bdim, &Cdim, &alpha,
 → &A[0], &Adim, &B[0], &Bdim, &beta, &C[0], &Cdim);
```

```
if (info != 0) {
 printf("blas error in dgemm returning %d\n", info);
 exit(99);
}
...
```

gcc -Ddgemm=dgemm\_ ... -lblas

```
...
stat = cublasDgemm (handle, dev_Atype, dev_Btype, Adim, Bdim, Cdim, &alpha,
 dev_ptr_A, Adim, dev_ptr_B, Bdim, &beta, dev_ptr_C, Cdim);
if (stat != CUBLAS_STATUS_SUCCESS) {
 printf("cublas error in dgemm \n");
 exit(99);
}
```

nvcc ... -lcublas

→ <http://www.netlib.org/blas/>

# CUBLAS CONT.

## CUDA SDK CONT.

col-wise  
linearized  
matrices;  
∀ pointers

```
...
DGEMM(TRANSA, TRANSB, M, N, K, ALPHA, A, LDA, B, LDB, BETA, C, LDC)
...
```

gfortran ... -lblas

```
...
Atype = Btype = 'T';
Adim = Bdim = Cdim = n;
alpha = (double) 1;
beta = (double) 0;
info = dgemm(&Atype, &Btype, &Adim, &Bdim, &Cdim, &alpha,
 → &A[0], &Adim, &B[0], &Bdim, &beta, &C[0], &Cdim);
if (info != 0) {
 printf("blas error in dgemm returning %d\n", info);
 exit(99);
}
...
```

gcc -Ddgemm=dgemm\_ ... -lblas

separate  
cublas  
arg/types

```
...
stat = cublasDgemm (handle, dev_Atype, dev_Btype, Adim, Bdim, Cdim, &alpha,
 dev_ptr_A, Adim, dev_ptr_B, Bdim, &beta, dev_ptr_C, Cdim);
if (stat != CUBLAS_STATUS_SUCCESS) {
 printf("cublas error in dgemm \n");
 exit(99);
}
```

nvcc ... -lcublas

→ <http://www.netlib.org/blas/>

Porting code to CUBLAS requires a more-or-less standard procedure of the following steps:

1. Initiate the CUBLAS context (`cublasCreate()`)
2. Allocate device memory using `cudaMalloc()` !
3. Transfer content of host arrays to the device (`cublasSetMatrix()`)
4. Call a specific CUBLAS routine, e.g. `cublasDgemm()`
5. Transfer back the result from device memory to host (`cublasGetMatrix()`)
6. Free device memory
7. Destroy CUBLAS context

→ <https://docs.nvidia.com/cuda/cublas/index.html>

→ <https://devtalk.nvidia.com/default/topic/1047981/b/t/post/5318441>

# CUBLAS CONT.

## CUDA SDK CONT.

### Example cublasDgemm()

```
#include <stdio.h>
#include <stdlib.h>
#include <cuda_runtime.h>
#include "cublas_v2.h"

int main(int argc, char **argv)
{
 int N, i, j;
 double alpha, beta, *A, *Adev, *B, *Bdev, *C, *Cdev;
 cublasStatus_t stat;
 cublasHandle_t handle;
 cublasOperation_t Atype, Btype;

 // memory allocation and parameter set up
 N = 5;
 alpha = (double) 1;
 beta = (double) 0;
 Atype = CUBLAS_OP_N;
 Btype = CUBLAS_OP_N;
 A = (double *) malloc(N * N * sizeof(double));
 B = (double *) malloc(N * N * sizeof(double));
 C = (double *) malloc(N * N * sizeof(double));

 // fill matrices A[] and B[] with data
```

→ <https://docs.nvidia.com/cuda/cublas/index.html>

# CUBLAS CONT.

## CUDA SDK CONT.

### Example cublasDgemm()

```
#include <stdio.h>
#include <stdlib.h>
#include <cuda_runtime.h>
#include "cublas_v2.h"

int main(int argc, char **argv)
{
 int N, i, j;
 double alpha, beta, *A, *Adev, *B, *Bdev, *C, *Cdev;
 cublasStatus_t stat;
 cublasHandle_t handle;
 cublasOperation_t Atype, Btype;

 // memory allocation and parameter set up
 N = 5;
 alpha = (double) 1;
 beta = (double) 0;
 Atype = CUBLAS_OP_N;
 Btype = CUBLAS_OP_N;
 A = (double *) malloc(N * N * sizeof(double));
 B = (double *) malloc(N * N * sizeof(double));
 C = (double *) malloc(N * N * sizeof(double));

 // fill matrices A[] and B[] with data
```

go for the new  
CUBLAS library API

# CUBLAS CONT.

## CUDA SDK CONT.

### Example cublasDgemm()

```
#include <stdio.h>
#include <stdlib.h>
#include <cuda_runtime.h>
#include "cublas_v2.h"
```

go for the new  
CUBLAS library API

```
int main(int argc, char **argv)
{
```

```
 int N, i, j;
 double alpha, beta, *A, *Adev, *B, *Bdev, *C, *Cdev;
 cublasStatus_t stat;
 cublasHandle_t handle;
 cublasOperation_t Atype, Btype;
```

will establish CUBLAS context

```
 // memory allocation and parameter set up
 N = 5;
 alpha = (double) 1;
 beta = (double) 0;
 Atype = CUBLAS_OP_N;
 Btype = CUBLAS_OP_N;
 A = (double *) malloc(N * N * sizeof(double));
 B = (double *) malloc(N * N * sizeof(double));
 C = (double *) malloc(N * N * sizeof(double));

 // fill matrices A[] and B[] with data
```

→ <https://docs.nvidia.com/cuda/cublas/index.html>

# CUBLAS CONT.

## CUDA SDK CONT.

### Example cublasDgemm()

```
#include <stdio.h>
#include <stdlib.h>
#include <cuda_runtime.h>
#include "cublas_v2.h"
```

go for the new  
CUBLAS library API

```
int main(int argc, char **argv)
{
```

```
 int N, i, j;
 double alpha, beta, *A, *Adev, *B, *Bdev, *C, *Cdev;
 cublasStatus_t stat;
 cublasHandle_t handle;
 cublasOperation_t Atype, Btype;
```

will establish CUBLAS context

```
 // memory allocation and parameter set up
 N = 5;
 alpha = (double) 1;
 beta = (double) 0;
 Atype = CUBLAS_OP_N;
 Btype = CUBLAS_OP_N;
 A = (double *) malloc(N * N * sizeof(double));
 B = (double *) malloc(N * N * sizeof(double));
 C = (double *) malloc(N * N * sizeof(double));
```

CUBLAS way of  
TRANSA/B='T'/'V'/'N'

```
 // fill matrices A[] and B[] with data
```

→ <https://docs.nvidia.com/cuda/cublas/index.html>

# CUBLAS CONT.

## CUDA SDK CONT.

### Example cublasDgemm()

```
#include <stdio.h>
#include <stdlib.h>
#include <cuda_runtime.h>
#include "cublas_v2.h"
```

go for the new  
CUBLAS library API

```
int main(int argc, char **argv)
{
```

```
 int N, i, j;
 double alpha, beta, *A, *Adev, *B, *Bdev, *C, *Cdev;
 cublasStatus_t stat;
 cublasHandle_t handle;
 cublasOperation_t Atype, Btype;
```

will establish CUBLAS context

```
 // memory allocation and parameter set up
 N = 5;
 alpha = (double) 1;
 beta = (double) 0;
 Atype = CUBLAS_OP_N;
 Btype = CUBLAS_OP_N;
```

CUBLAS way of  
TRANSA/B='T'/'V'/'N'

```
 A = (double *) malloc(N * N * sizeof(double));
 B = (double *) malloc(N * N * sizeof(double));
 C = (double *) malloc(N * N * sizeof(double));
```

normal memory  
allocation

```
 // fill matrices A[] and B[] with data
```

→ <https://docs.nvidia.com/cuda/cublas/index.html>

### Example cublasDgemm() cont.

```
// initiate the CUBLAS context
cublasCreate(&handle);
// allocate device memory
cudaMalloc(&Adev, N * N * sizeof(double));
cudaMalloc(&Bdev, N * N * sizeof(double));
cudaMalloc(&Cdev, N * N * sizeof(double));
// copy contents of arrays A[], B[] into device memory
cublasSetMatrix(N, N, sizeof(double), &A[0], N, Adev, N);
cublasSetMatrix(N, N, sizeof(double), &B[0], N, Bdev, N);
// carry out CUBLAS operation
cublasDgemm(handle, Atype, Btype, N, N, N, &alpha, Adev, N, Bdev, N, &beta, Cdev, N);
// retrieve results from device memory
cublasGetMatrix(N, N, sizeof(double), Cdev, N, &C[0], N);
// do something with the result
... = C[]
// make clean
cudaFree(Cdev); cudaFree(Bdev); cudaFree(Adev);
cublasDestroy(handle);
// free host memory and return
free(C); free(B); free(A);
return(0);
}
```

### Example cublasDgemm() cont.

Step 1

```
// initiate the CUBLAS context
cublasCreate(&handle); ←
// allocate device memory
cudaMalloc(&Adev, N * N * sizeof(double));
cudaMalloc(&Bdev, N * N * sizeof(double));
cudaMalloc(&Cdev, N * N * sizeof(double));
// copy contents of arrays A[], B[] into device memory
cublasSetMatrix(N, N, sizeof(double), &A[0], N, Adev, N);
cublasSetMatrix(N, N, sizeof(double), &B[0], N, Bdev, N);
// carry out CUBLAS operation
cublasDgemm(handle, Atype, Btype, N, N, N, &alpha, Adev, N, Bdev, N, &beta, Cdev, N);
// retrieve results from device memory
cublasGetMatrix(N, N, sizeof(double), Cdev, N, &C[0], N);
// do something with the result
... = C[]
// make clean
cudaFree(Cdev); cudaFree(Bdev); cudaFree(Adev);
cublasDestroy(handle);
// free host memory and return
free(C); free(B); free(A);
return(0);
}
```

### Example cublasDgemm() cont.

```
// initiate the CUBLAS context
cublasCreate(&handle);
// allocate device memory
cudaMalloc(&Adev, N * N * sizeof(double));
cudaMalloc(&Bdev, N * N * sizeof(double));
cudaMalloc(&Cdev, N * N * sizeof(double));
// copy contents of arrays A[], B[] into device memory
cublasSetMatrix(N, N, sizeof(double), &A[0], N, Adev, N);
cublasSetMatrix(N, N, sizeof(double), &B[0], N, Bdev, N);
// carry out CUBLAS operation
cublasDgemm(handle, Atype, Btype, N, N, N, &alpha, Adev, N, Bdev, N, &beta, Cdev, N);
// retrieve results from device memory
cublasGetMatrix(N, N, sizeof(double), Cdev, N, &C[0], N);
// do something with the result
... = C[]
// make clean
cudaFree(Cdev); cudaFree(Bdev); cudaFree(Adev);
cublasDestroy(handle);
// free host memory and return
free(C); free(B); free(A);
return(0);
}
```

Step 1

Step 2

# CUBLAS CONT.

## CUDA SDK CONT.

### Example cublasDgemm() cont.

```
// initiate the CUBLAS context
cublasCreate(&handle);
// allocate device memory
cudaMalloc(&Adev, N * N * sizeof(double));
cudaMalloc(&Bdev, N * N * sizeof(double));
cudaMalloc(&Cdev, N * N * sizeof(double));
// copy contents of arrays A[], B[] into device memory
cublasSetMatrix(N, N, sizeof(double), &A[0], N, Adev, N);
cublasSetMatrix(N, N, sizeof(double), &B[0], N, Bdev, N);
// carry out CUBLAS operation
cublasDgemm(handle, Atype, Btype, N, N, N, &alpha, Adev, N, Bdev, N, &beta, Cdev, N);
// retrieve results from device memory
cublasGetMatrix(N, N, sizeof(double), Cdev, N, &C[0], N);
// do something with the result
... = C[]
// make clean
cudaFree(Cdev); cudaFree(Bdev); cudaFree(Adev);
cublasDestroy(handle);
// free host memory and return
free(C); free(B); free(A);
return(0);
}
```

Step 1

Step 2

Step 3

→ <https://docs.nvidia.com/cuda/cublas/index.html>

### Example cublasDgemm() cont.

```
// initiate the CUBLAS context
cublasCreate(&handle);
// allocate device memory
cudaMalloc(&Adev, N * N * sizeof(double));
cudaMalloc(&Bdev, N * N * sizeof(double));
cudaMalloc(&Cdev, N * N * sizeof(double));
// copy contents of arrays A[], B[] into device memory
cublasSetMatrix(N, N, sizeof(double), &A[0], N, Adev, N);
cublasSetMatrix(N, N, sizeof(double), &B[0], N, Bdev, N);
// carry out CUBLAS operation
cublasDgemm(handle, Atype, Btype, N, N, N, &alpha, Adev, N, Bdev, N, &beta, Cdev, N);
// retrieve results from device memory
cublasGetMatrix(N, N, sizeof(double), Cdev, N, &C[0], N);
// do something with the result
... = C[]
// make clean
cudaFree(Cdev); cudaFree(Bdev); cudaFree(Adev);
cublasDestroy(handle);
// free host memory and return
free(C); free(B); free(A);
return(0);
}
```

Step 1

Step 2

Step 3

Step 4

### Example cublasDgemm() cont.

```
// initiate the CUBLAS context
```

```
cublasCreate(&handle);
```

```
// allocate device memory
```

```
cudaMalloc(&Adev, N * N * sizeof(double));
```

```
cudaMalloc(&Bdev, N * N * sizeof(double));
```

```
cudaMalloc(&Cdev, N * N * sizeof(double));
```

```
// copy contents of arrays A[], B[] into device memory
```

```
cublasSetMatrix(N, N, sizeof(double), &A[0], N, Adev, N);
```

```
cublasSetMatrix(N, N, sizeof(double), &B[0], N, Bdev, N);
```

```
// carry out CUBLAS operation
```

```
cublasDgemm(handle, Atype, Btype, N, N, N, &alpha, Adev, N, Bdev, N, &beta, Cdev, N);
```

```
// retrieve results from device memory
```

```
cublasGetMatrix(N, N, sizeof(double), Cdev, N, &C[0], N);
```

```
// do something with the result
```

```
... = C[]
```

```
// make clean
```

```
cudaFree(Cdev); cudaFree(Bdev); cudaFree(Adev);
```

```
cublasDestroy(handle);
```

```
// free host memory and return
```

```
free(C); free(B); free(A);
```

```
return(0);
```

```
}
```

Step 1

Step 2

Step 3

Step 4

Step 5

### Example cublasDgemm() cont.

```
// initiate the CUBLAS context
```

```
cublasCreate(&handle);
```

```
// allocate device memory
```

```
cudaMalloc(&Adev, N * N * sizeof(double));
```

```
cudaMalloc(&Bdev, N * N * sizeof(double));
```

```
cudaMalloc(&Cdev, N * N * sizeof(double));
```

```
// copy contents of arrays A[], B[] into device memory
```

```
cublasSetMatrix(N, N, sizeof(double), &A[0], N, Adev, N);
```

```
cublasSetMatrix(N, N, sizeof(double), &B[0], N, Bdev, N);
```

```
// carry out CUBLAS operation
```

```
cublasDgemm(handle, Atype, Btype, N, N, N, &alpha, Adev, N, Bdev, N, &beta, Cdev, N);
```

```
// retrieve results from device memory
```

```
cublasGetMatrix(N, N, sizeof(double), Cdev, N, &C[0], N);
```

```
// do something with the result
```

```
... = C[]
```

```
// make clean
```

```
cudaFree(Cdev); cudaFree(Bdev); cudaFree(Adev);
```

```
cublasDestroy(handle);
```

```
// free host memory and return
```

```
free(C); free(B); free(A);
```

```
return(0);
```

```
}
```

Step 1

Step 2

Step 3

Step 4

Step 5

Step 6

# CUBLAS CONT.

## CUDA SDK CONT.

### Example cublasDgemm() cont.

```
// initiate the CUBLAS context
```

```
cublasCreate(&handle);
```

```
// allocate device memory
```

```
cudaMalloc(&Adev, N * N * sizeof(double));
```

```
cudaMalloc(&Bdev, N * N * sizeof(double));
```

```
cudaMalloc(&Cdev, N * N * sizeof(double));
```

```
// copy contents of arrays A[], B[] into device memory
```

```
cublasSetMatrix(N, N, sizeof(double), &A[0], N, Adev, N);
```

```
cublasSetMatrix(N, N, sizeof(double), &B[0], N, Bdev, N);
```

```
// carry out CUBLAS operation
```

```
cublasDgemm(handle, Atype, Btype, N, N, N, &alpha, Adev, N, Bdev, N, &beta, Cdev, N);
```

```
// retrieve results from device memory
```

```
cublasGetMatrix(N, N, sizeof(double), Cdev, N, &C[0], N);
```

```
// do something with the result
```

```
... = C[]
```

```
// make clean
```

```
cudaFree(Cdev); cudaFree(Bdev); cudaFree(Adev);
```

```
cublasDestroy(handle);
```

```
// free host memory and return
```

```
free(C); free(B); free(A);
```

```
return(0);
```

```
}
```

Step 1

Step 2

Step 3

Step 4

Step 5

Step 6

Step 7

Words of caution:

- Always start with a small explicit example to check/confirm each individual step
- Formats of matrices are crucial ! 1D-representation, column-wise linearized;
- (double) on consumer grade cards is slower by  $\approx 1/64$  than (float)
- Two new APIs, CUBLASXT (for CUDA  $\geq 6.0$ ) and cuBLASLt (for CUDA 10.1)
- Pity that we can't use `cudaMallocManaged()` at this point

→ <https://docs.nvidia.com/cuda/cublas/index.html>

→ <https://devtalk.nvidia.com/default/topic/1047981/b/t/post/5318441>

Next level of problems:

$$\underbrace{\begin{pmatrix} 1.96 & -6.49 & -0.47 & -7.20 & -0.65 \\ -6.49 & 3.80 & -6.39 & 1.50 & -6.34 \\ -0.47 & -6.39 & 4.17 & -1.51 & 2.67 \\ -7.20 & 1.50 & -1.51 & 5.70 & 1.80 \\ -0.65 & -6.34 & 2.67 & 1.80 & -7.10 \end{pmatrix}}_A$$

- For example, what are the eigenvalues and corresponding eigenvectors of  $A$  ?
- $Ax = \lambda x$
- A typical LAPACK problem — usually tightly coupled to BLAS
- Not on the GPU ! CUBLAS is BLAS only !
- However, there are cuSolver and MAGMA

→ <https://docs.nvidia.com/cuda/cusolver>

→ [https://icl.cs.utk.edu/projectsfiles/magma/doxygen/group\\_\\_cublas\\_\\_const.html](https://icl.cs.utk.edu/projectsfiles/magma/doxygen/group__cublas__const.html)

Making use of CUSOLVER is schematically very similar to using CUBLAS:

1. Initiate the CUSOLVER context (`cusolverDnCreate()`)
2. Allocate device memory using `cudaMalloc()` !
3. Transfer content of host arrays to the device (`cudaMemcpy()`)
4. Semi-automatically set up working space required by CUSOLVER routine, e.g. WORK, LWORK in LAPACK jargon
5. Call a specific CUSOLVER routine, e.g. `cusolverDnDsyevd()`
6. Transfer back the result from device memory to host (`cudaMemcpy()`)
7. Free device memory
8. Destroy CUSOLVER context

### Example cusolverDnDsyevd()

```
#include <stdio.h>
#include <stdlib.h>
#include <assert.h>
#include <cuda_runtime.h>
#include "cusolverDn.h"

int main(int argc, char **argv)
{
 int i, j, lwork, info_gpu, *devInfo;
 double *d_A, *d_W, *d_work;
 cusolverDnHandle_t cusolverH;
 cusolverStatus_t cusolver_status;
 cusolverEigMode_t jobz;
 cublasFillMode_t uplo;
 cudaError_t cudaStat;
 const int m = 5;
 const int lda = m;
 double W[m];
 double V[lda*m];
 double A[lda*m] = { 1.96, -6.49, -0.47, -7.20, -0.65,
 -6.49, 3.80, -6.39, 1.50, -6.34,
 -0.47, -6.39, 4.17, -1.51, 2.67,
 -7.20, 1.50, -1.51, 5.70, 1.80,
 -0.65, -6.34, 2.67, 1.80, -7.10};
```

# CUSOLVER CONT.

## CUDA SDK CONT.

### Example cusolverDnDsyevd()

```
#include <stdio.h>
#include <stdlib.h>
#include <assert.h>
#include <cuda_runtime.h>
#include "cusolverDn.h" ←
```

CUSOLVER header  
for 'dense' subset

```
int main(int argc, char **argv)
{
 int i, j, lwork, info_gpu, *devInfo;
 double *d_A, *d_W, *d_work;
 cusolverDnHandle_t cusolverH;
 cusolverStatus_t cusolver_status;
 cusolverEigMode_t jobz;
 cublasFillMode_t uplo;
 cudaError_t cudaStat;
 const int m = 5;
 const int lda = m;
 double W[m];
 double V[lda*m];
 double A[lda*m] = { 1.96, -6.49, -0.47, -7.20, -0.65,
 -6.49, 3.80, -6.39, 1.50, -6.34,
 -0.47, -6.39, 4.17, -1.51, 2.67,
 -7.20, 1.50, -1.51, 5.70, 1.80,
 -0.65, -6.34, 2.67, 1.80, -7.10};
```

# CUSOLVER CONT.

## CUDA SDK CONT.

### Example cusolverDnDsyevd()

```
#include <stdio.h>
#include <stdlib.h>
#include <assert.h>
#include <cuda_runtime.h>
#include "cusolverDn.h" ←
```

CUSOLVER header  
for 'dense' subset

```
int main(int argc, char **argv)
{
```

4 CUSOLVER context

```
 int i, j, lwork, info_gpu, *devInfo;
 double *d_A, *d_W, *d_work;
 cusolverDnHandle_t cusolverH; ←
 cusolverStatus_t cusolver_status;
 cusolverEigMode_t jobz;
 cublasFillMode_t uplo;
 cudaError_t cudaStat;
 const int m = 5;
 const int lda = m;
 double W[m];
 double V[lda*m];
 double A[lda*m] = { 1.96, -6.49, -0.47, -7.20, -0.65,
 -6.49, 3.80, -6.39, 1.50, -6.34,
 -0.47, -6.39, 4.17, -1.51, 2.67,
 -7.20, 1.50, -1.51, 5.70, 1.80,
 -0.65, -6.34, 2.67, 1.80, -7.10};
```

### Example cusolverDnDsyevd()

```
#include <stdio.h>
#include <stdlib.h>
#include <assert.h>
#include <cuda_runtime.h>
#include "cusolverDn.h"

int main(int argc, char **argv)
{
 int i, j, lwork, info_gpu, *devInfo;
 double *d_A, *d_W, *d_work;
 cusolverDnHandle_t cusolverH;
 cusolverStatus_t cusolver_status;
 cusolverEigMode_t jobz;
 cublasFillMode_t uplo;
 cudaError_t cudaStat;
 const int m = 5;
 const int lda = m;
 double W[m];
 double V[lda*m];
 double A[lda*m] = { 1.96, -6.49, -0.47, -7.20, -0.65,
 -6.49, 3.80, -6.39, 1.50, -6.34,
 -0.47, -6.39, 4.17, -1.51, 2.67,
 -7.20, 1.50, -1.51, 5.70, 1.80,
 -0.65, -6.34, 2.67, 1.80, -7.10};
```

CUSOLVER header  
for 'dense' subset

4 CUSOLVER context

CUSOLVER flags 4 LAPACK's

### Example cusolverDnDsyevd() cont.

```

jobz = CUSOLVER_EIG_MODE_VECTOR;
uplo = CUBLAS_FILL_MODE_LOWER;
cusolver_status = cusolverDnCreate(&cusolverH);
assert(CUSOLVER_STATUS_SUCCESS == cusolver_status);
cudaStat = cudaMalloc ((void**)&d_A, sizeof(double) * lda * m);
cudaStat = cudaMalloc ((void**)&d_W, sizeof(double) * m);
cudaStat = cudaMalloc ((void**)&devInfo, sizeof(int));
cudaStat = cudaMemcpy(d_A, A, sizeof(double) * lda * m, cudaMemcpyHostToDevice);

cusolver_status = cusolverDnDsyevd_bufferSize(cusolverH, jobz, uplo, m, d_A, lda, d_W, &lwork);
cudaStat = cudaMalloc((void**)&d_work, sizeof(double)*lwork);
cusolver_status = cusolverDnDsyevd(cusolverH, jobz, uplo, m, d_A, lda, d_W, d_work, lwork, devInfo);
cudaStat = cudaDeviceSynchronize();

cudaStat = cudaMemcpy(W, d_W, sizeof(double)*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(V, d_A, sizeof(double)*lda*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(&info_gpu, devInfo, sizeof(int), cudaMemcpyDeviceToHost);
... do something with W[] and V[] ...
cudaFree(d_A); cudaFree(d_W); cudaFree(devInfo); cudaFree(d_work);
cusolverDnDestroy(cusolverH);
cudaDeviceReset();

return(0);
}

```

### Example cusolverDnDsyevd() cont.

establish CUSOLVER context

```

jobz = CUSOLVER_EIG_MODE_VECTOR;
uplo = CUBLAS_FILL_MODE_LOWER;
cusolver_status = cusolverDnCreate(&cusolverH); ←
assert(CUSOLVER_STATUS_SUCCESS == cusolver_status);
cudaStat = cudaMalloc ((void*)&d_A, sizeof(double) * lda * m);
cudaStat = cudaMalloc ((void*)&d_W, sizeof(double) * m);
cudaStat = cudaMalloc ((void*)&devInfo, sizeof(int));
cudaStat = cudaMemcpy(d_A, A, sizeof(double) * lda * m, cudaMemcpyHostToDevice);

cusolver_status = cusolverDnDsyevd_bufferSize(cusolverH, jobz, uplo, m, d_A, lda, d_W, &lwork);
cudaStat = cudaMalloc((void*)&d_work, sizeof(double)*lwork);
cusolver_status = cusolverDnDsyevd(cusolverH, jobz, uplo, m, d_A, lda, d_W, d_work, lwork, devInfo);
cudaStat = cudaDeviceSynchronize();

cudaStat = cudaMemcpy(W, d_W, sizeof(double)*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(V, d_A, sizeof(double)*lda*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(&info_gpu, devInfo, sizeof(int), cudaMemcpyDeviceToHost);
... do something with W[] and V[] ...
cudaFree(d_A); cudaFree(d_W); cudaFree(devInfo); cudaFree(d_work);
cusolverDnDestroy(cusolverH);
cudaDeviceReset();

return(0);
}

```

### Example cusolverDnDsyevd() cont.

```

jobz = CUSOLVER_EIG_MODE_VECTOR;
uplo = CUBLAS_FILL_MODE_LOWER;
cusolver_status = cusolverDnCreate(&cusolverH);
assert(CUSOLVER_STATUS_SUCCESS == cusolver_status);
cudaStat = cudaMalloc ((void**)&d_A, sizeof(double) * lda * m);
cudaStat = cudaMalloc ((void**)&d_W, sizeof(double) * m);
cudaStat = cudaMalloc ((void**)&devInfo, sizeof(int));
cudaStat = cudaMemcpy(d_A, A, sizeof(double) * lda * m, cudaMemcpyHostToDevice);

cusolver_status = cusolverDnDsyevd_bufferSize(cusolverH, jobz, uplo, m, d_A, lda, d_W, &lwork);
cudaStat = cudaMalloc((void**)&d_work, sizeof(double)*lwork);
cusolver_status = cusolverDnDsyevd(cusolverH, jobz, uplo, m, d_A, lda, d_W, d_work, lwork, devInfo);
cudaStat = cudaDeviceSynchronize();

cudaStat = cudaMemcpy(W, d_W, sizeof(double)*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(V, d_A, sizeof(double)*lda*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(&info_gpu, devInfo, sizeof(int), cudaMemcpyDeviceToHost);
... do something with W[] and V[] ...
cudaFree(d_A); cudaFree(d_W); cudaFree(devInfo); cudaFree(d_work);
cusolverDnDestroy(cusolverH);
cudaDeviceReset();

return(0);
}

```

establish CUSOLVER context

error check

### Example cusolverDnDsyevd() cont.

```

jobz = CUSOLVER_EIG_MODE_VECTOR;
uplo = CUBLAS_FILL_MODE_LOWER;
cusolver_status = cusolverDnCreate(&cusolverH);
assert(CUSOLVER_STATUS_SUCCESS == cusolver_status);
cudaStat = cudaMalloc ((void**)&d_A, sizeof(double) * lda * m);
cudaStat = cudaMalloc ((void**)&d_W, sizeof(double) * m);
cudaStat = cudaMalloc ((void**)&devInfo, sizeof(int));
cudaStat = cudaMemcpy(d_A, A, sizeof(double) * lda * m, cudaMemcpyHostToDevice);

cusolver_status = cusolverDnDsyevd_bufferSize(cusolverH, jobz, uplo, m, d_A, lda, d_W, &lwork);
cudaStat = cudaMalloc((void**)&d_work, sizeof(double)*lwork);
cusolver_status = cusolverDnDsyevd(cusolverH, jobz, uplo, m, d_A, lda, d_W, d_work, lwork, devInfo);
cudaStat = cudaDeviceSynchronize();

cudaStat = cudaMemcpy(W, d_W, sizeof(double)*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(V, d_A, sizeof(double)*lda*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(&info_gpu, devInfo, sizeof(int), cudaMemcpyDeviceToHost);
... do something with W[] and V[] ...
cudaFree(d_A); cudaFree(d_W); cudaFree(devInfo); cudaFree(d_work);
cusolverDnDestroy(cusolverH);
cudaDeviceReset();

return(0);
}

```

establish CUSOLVER context

error check

standard procedure

### Example cusolverDnDsyevd() cont.

adjust  
work  
arrays

establish CUSOLVER context

error check

standard procedure

```

jobz = CUSOLVER_EIG_MODE_VECTOR;
uplo = CUBLAS_FILL_MODE_LOWER;
cusolver_status = cusolverDnCreate(&cusolverH);
assert(CUSOLVER_STATUS_SUCCESS == cusolver_status);
cudaStat = cudaMalloc ((void**)&d_A, sizeof(double) * lda * m);
cudaStat = cudaMalloc ((void**)&d_W, sizeof(double) * m);
cudaStat = cudaMalloc ((void**)&devInfo, sizeof(int));
cudaStat = cudaMemcpy(d_A, A, sizeof(double) * lda * m, cudaMemcpyHostToDevice);

cusolver_status = cusolverDnDsyevd_bufferSize(cusolverH, jobz, uplo, m, d_A, lda, d_W, &lwork);
cudaStat = cudaMalloc((void**)&d_work, sizeof(double)*lwork);
cusolver_status = cusolverDnDsyevd(cusolverH, jobz, uplo, m, d_A, lda, d_W, d_work, lwork, devInfo);
cudaStat = cudaDeviceSynchronize();

cudaStat = cudaMemcpy(W, d_W, sizeof(double)*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(V, d_A, sizeof(double)*lda*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(&info_gpu, devInfo, sizeof(int), cudaMemcpyDeviceToHost);
... do something with W[] and V[] ...
cudaFree(d_A); cudaFree(d_W); cudaFree(devInfo); cudaFree(d_work);
cusolverDnDestroy(cusolverH);
cudaDeviceReset();

return(0);
}

```

### Example cusolverDnDsyevd() cont.

adjust  
work  
ar-  
rays

establish CUSOLVER context

error check

standard procedure

call  
solver

```

jobz = CUSOLVER_EIG_MODE_VECTOR;
uplo = CUBLAS_FILL_MODE_LOWER;
cusolver_status = cusolverDnCreate(&cusolverH);
assert(CUSOLVER_STATUS_SUCCESS == cusolver_status);
cudaStat = cudaMalloc ((void**)&d_A, sizeof(double) * lda * m);
cudaStat = cudaMalloc ((void**)&d_W, sizeof(double) * m);
cudaStat = cudaMalloc ((void**)&devInfo, sizeof(int));
cudaStat = cudaMemcpy(d_A, A, sizeof(double) * lda * m, cudaMemcpyHostToDevice);

cusolver_status = cusolverDnDsyevd_bufferSize(cusolverH, jobz, uplo, m, d_A, lda, d_W, &lwork);
cudaStat = cudaMalloc((void**)&d_work, sizeof(double)*lwork);
cusolver_status = cusolverDnDsyevd(cusolverH, jobz, uplo, m, d_A, lda, d_W, d_work, lwork, devInfo);
cudaStat = cudaDeviceSynchronize();

cudaStat = cudaMemcpy(W, d_W, sizeof(double)*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(V, d_A, sizeof(double)*lda*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(&info_gpu, devInfo, sizeof(int), cudaMemcpyDeviceToHost);
... do something with W[] and V[] ...
cudaFree(d_A); cudaFree(d_W); cudaFree(devInfo); cudaFree(d_work);
cusolverDnDestroy(cusolverH);
cudaDeviceReset();

return(0);
}

```

# CUSOLVER CONT.

## CUDA SDK CONT.

### Example cusolverDnDsyevd() cont.

adjust  
work  
arrays

establish CUSOLVER context

error check

standard procedure

call  
solver

back copy results

```
jobz = CUSOLVER_EIG_MODE_VECTOR;
uplo = CUBLAS_FILL_MODE_LOWER;
cusolver_status = cusolverDnCreate(&cusolverH);
assert(CUSOLVER_STATUS_SUCCESS == cusolver_status);
cudaStat = cudaMalloc ((void**)&d_A, sizeof(double) * lda * m);
cudaStat = cudaMalloc ((void**)&d_W, sizeof(double) * m);
cudaStat = cudaMalloc ((void**)&devInfo, sizeof(int));
cudaStat = cudaMemcpy(d_A, A, sizeof(double) * lda * m, cudaMemcpyHostToDevice);

cusolver_status = cusolverDnDsyevd_bufferSize(cusolverH, jobz, uplo, m, d_A, lda, d_W, &lwork);
cudaStat = cudaMalloc((void**)&d_work, sizeof(double)*lwork);
cusolver_status = cusolverDnDsyevd(cusolverH, jobz, uplo, m, d_A, lda, d_W, d_work, lwork, devInfo);
cudaStat = cudaDeviceSynchronize();

cudaStat = cudaMemcpy(W, d_W, sizeof(double)*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(V, d_A, sizeof(double)*lda*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(&info_gpu, devInfo, sizeof(int), cudaMemcpyDeviceToHost);
... do something with W[] and V[] ...
cudaFree(d_A); cudaFree(d_W); cudaFree(devInfo); cudaFree(d_work);
cusolverDnDestroy(cusolverH);
cudaDeviceReset();

return(0);
}
```

# CUSOLVER CONT.

## CUDA SDK CONT.

### Example cusolverDnDsyevd() cont.

adjust  
work  
arrays

establish CUSOLVER context

error check

standard procedure

call  
solver

back copy results

finalize

```
jobz = CUSOLVER_EIG_MODE_VECTOR;
uplo = CUBLAS_FILL_MODE_LOWER;
cusolver_status = cusolverDnCreate(&cusolverH);
assert(CUSOLVER_STATUS_SUCCESS == cusolver_status);
cudaStat = cudaMalloc ((void**)&d_A, sizeof(double) * lda * m);
cudaStat = cudaMalloc ((void**)&d_W, sizeof(double) * m);
cudaStat = cudaMalloc ((void**)&devInfo, sizeof(int));
cudaStat = cudaMemcpy(d_A, A, sizeof(double) * lda * m, cudaMemcpyHostToDevice);

cusolver_status = cusolverDnDsyevd_bufferSize(cusolverH, jobz, uplo, m, d_A, lda, d_W, &lwork);
cudaStat = cudaMalloc((void**)&d_work, sizeof(double)*lwork);
cusolver_status = cusolverDnDsyevd(cusolverH, jobz, uplo, m, d_A, lda, d_W, d_work, lwork, devInfo);
cudaStat = cudaDeviceSynchronize();

cudaStat = cudaMemcpy(W, d_W, sizeof(double)*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(V, d_A, sizeof(double)*lda*m, cudaMemcpyDeviceToHost);
cudaStat = cudaMemcpy(&info_gpu, devInfo, sizeof(int), cudaMemcpyDeviceToHost);
... do something with W[] and V[] ...
cudaFree(d_A); cudaFree(d_W); cudaFree(devInfo); cudaFree(d_work);
cusolverDnDestroy(cusolverH);
cudaDeviceReset();

return(0);
}
```

- Very straightforward procedure offering significant speed-up for large scale problems at very minor porting effort
- Again, (float)  $\leftrightarrow$  (double) gap in terms of performance,  $\approx 1/64$  on consumer cards !
- A related problem of considerable interest may be addressed via `cusolverEigType_t` — generalized symmetric-definite eigenvalue problem (section 2.2.1.4)  
 $A x = \lambda B x$
- Sparse problems covered too — `cuSolverSP`

# MORE LIBRARIES

## CUDA SDK CONT.

- CUFFT — CUDA Fast Fourier Transform
- CURAND — CUDA random number generation library
- CUDNN & TENSORRT — Deep Learning, training & inference
- CUSPARSE — Basic linear algebra for sparse matrices
- NVBLAS — Another replacement for BLAS calls with little effort of porting (re-linking or LD\_PRELOAD)
- NVGRAPH — Big Data analytics via graph problems

→ <https://docs.nvidia.com/cuda/cufft/index.html>

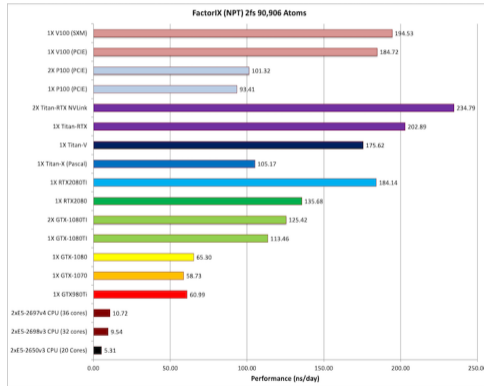
→ <https://docs.nvidia.com/cuda/curand/index.html>

→ <https://docs.nvidia.com/deeplearning/sdk/index.html>

# NUMERICAL ACCURACY & PERFORMANCE

## CUDA SDK CONT.

How come that scientific apps, e.g. AMBER's pmemd.cuda are doing so well on consumer grade GPUs ?



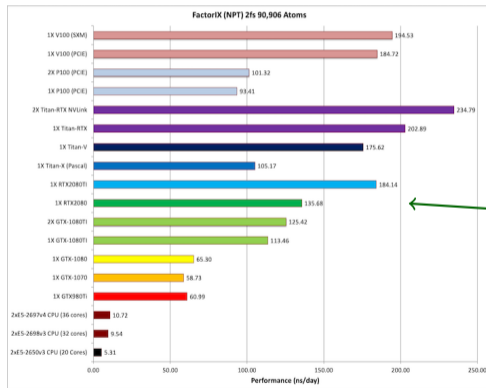
→ <http://ambermd.org/GPUPerformance.php>

→ <https://www.sciencedirect.com/science/article/pii/S0010465512003098>

# NUMERICAL ACCURACY & PERFORMANCE

## CUDA SDK CONT.

How come that scientific apps, e.g. AMBER's pmemd.cuda are doing so well on consumer grade GPUs ?



Combine several 32bit types (float, int) to approximate double

→ <http://ambermd.org/GPUPerformance.php>

→ <https://www.sciencedirect.com/science/article/pii/S0010465512003098>

Dekker (1971) and Knuth (1969)

### Quasi-double precision method

- Combine two floating-point numbers to express one variable

|                               |                                        |
|-------------------------------|----------------------------------------|
| $x + y = z + zz$              | $x = 10.2, y = 0.345$                  |
| (where $ z / zz  < 2^{-24}$ ) | (three significant digits)             |
| $z = \text{fl}(x + y)$        | $z = 10.5$                             |
| $w = \text{fl}(z - x)$        | $w = 0.3$                              |
| $zz = \text{fl}(y - w)$       | $zz = 0.045$                           |
|                               | ( $z + zz = 10.545$ , no cancellation) |

$x, y, z, zz$  : FP32 variable

$\text{fl}(\text{operation})$  : FP32 arithmetic operation

- More than twice operations are needed for similar accuracy to double-precision

⇒ Only works for consumer GPUs

(slide courtesy of Prof Tetsu Narumi, UEC, Tokyo)

→ <https://link.springer.com/article/10.1007/BF01397083>

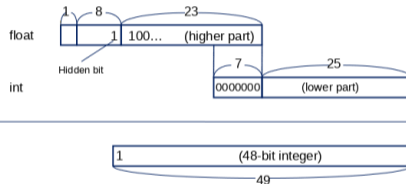
→ [https://en.wikipedia.org/wiki/The\\_Art\\_of\\_Computer\\_Programming](https://en.wikipedia.org/wiki/The_Art_of_Computer_Programming)

# NUMERICAL ACCURACY & PERFORMANCE CONT.

## CUDA SDK CONT.

### Combine floating- and fixed-point

- and INT32 for one variable
- Initialized with a large number beforehand
- Similar to 48-bit integer



*Tetsu Narumi et al., International Journal of Computational Methods, vol. 8, No. 3, pp. 561-581 (2011)*

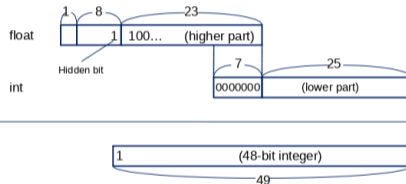
(slide courtesy of Prof Tetsu Narumi, UEC, Tokyo)

→ [doi:10.1142/S0219876211002708](https://doi.org/10.1142/S0219876211002708)

→ [doi:10.1016/j.cpc.2012.09.022](https://doi.org/10.1016/j.cpc.2012.09.022)

### Combine floating- and fixed-point

- and INT32 for one variable
- Initialized with a large number beforehand
- Similar to 48-bit integer



*Tetsu Narumi et al., International Journal of Computational Methods, vol. 8, No. 3, pp. 561-581 (2011)*

All elementary  
operations, +,  
-, \*

(slide courtesy of Prof Tetsu Narumi, UEC, Tokyo)

→ [doi:10.1142/S0219876211002708](https://doi.org/10.1142/S0219876211002708)

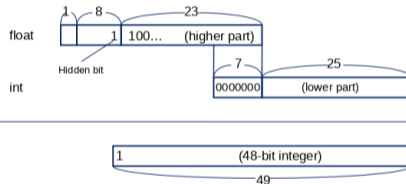
→ [doi:10.1016/j.cpc.2012.09.022](https://doi.org/10.1016/j.cpc.2012.09.022)

# NUMERICAL ACCURACY & PERFORMANCE CONT.

## CUDA SDK CONT.

### Combine floating- and fixed-point

- and INT32 for one variable
- Initialized with a large number beforehand
- Similar to 48-bit integer



All elementary operations, +, -, \*

*Tetsu Narumi et al., International Journal of Computational Methods, vol. 8, No. 3, pp. 561-581 (2011)*

(slide courtesy of Prof Tetsu Narumi, UEC, Tokyo)

Similar strategy in AMBER's pmemd.cuda

→ [doi:10.1142/S0219876211002708](https://doi.org/10.1142/S0219876211002708)

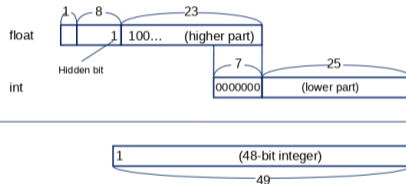
→ [doi:10.1016/j.cpc.2012.09.022](https://doi.org/10.1016/j.cpc.2012.09.022)

# NUMERICAL ACCURACY & PERFORMANCE CONT.

## CUDA SDK CONT.

### Combine floating- and fixed-point

- and INT32 for one variable
- Initialized with a large number beforehand
- Similar to 48-bit integer



Also see Mandel-  
brot example in SDK,  
5\_Domain\_Specific

All elementary  
operations, +,  
-, \*

*Tetsu Narumi et al., International Journal of Computational Methods, vol. 8,  
No. 3, pp. 561-581 (2011)*

(slide courtesy of Prof Tetsu Narumi, UEC, Tokyo)

Similar  
strategy in  
AMBER's  
pmemd.cuda

→ [doi:10.1142/S0219876211002708](https://doi.org/10.1142/S0219876211002708)

→ [doi:10.1016/j.cpc.2012.09.022](https://doi.org/10.1016/j.cpc.2012.09.022)

# 5\_DOMAIN\_SPECIFIC/MARCHINGCUBES

CUDA SDK CONT.

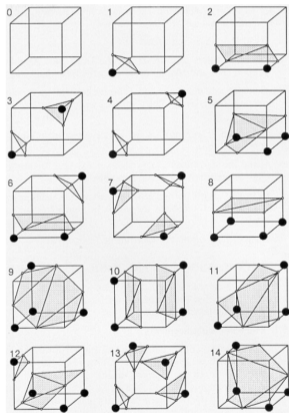
Practical example, of frequent use in biophysical chemistry

- Extracts an isosurface from a volumetric dataset using the 'marching cubes algorithm'
- OpenGL interoperation
- Chosen example is the electron density of  $C_{60}$

→ `./run_marchingCubes.sh`

# 5\_DOMAIN\_SPECIFIC/MARCHINGCUBES CONT.

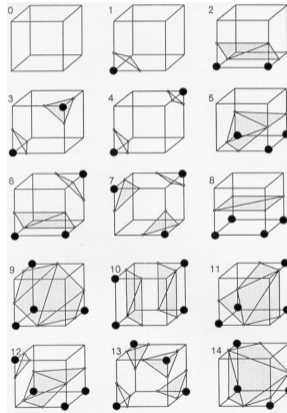
## CUDA SDK CONT.



→ <https://dl.acm.org/citation.cfm?doid=37402.37422>

# 5\_DOMAIN\_SPECIFIC/MARCHINGCUBES CONT.

CUDA SDK CONT.



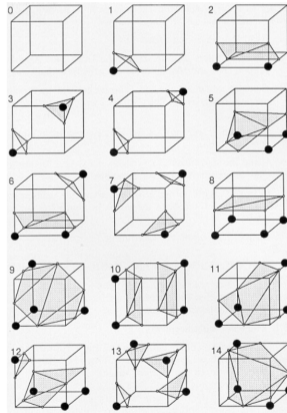
Assign vertices 0 if below iso-value, 1 if above

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CUDA SDK CONT.

Neighbouring  
vertices of 0,  
1 assignment  
determine iso-  
surface edges



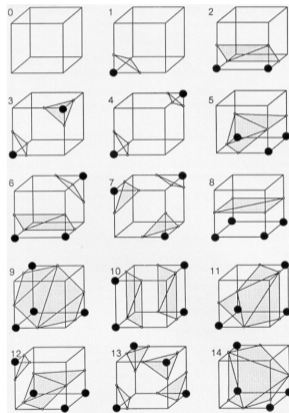
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# 5\_DOMAIN\_SPECIFIC/MARCHINGCUBES CONT.

CUDA SDK CONT.

Neighbouring  
vertices of 0,  
1 assignment  
determine iso-  
surface edges



14 elementary  
cases, the rest  
(256) from  
symmetry

Assign ver-  
tices 0 if below  
iso-value, 1 if  
above

→ <https://dl.acm.org/citation.cfm?doid=37402.37422>

## 5\_DOMAIN\_SPECIFIC/MARCHINGCUBES CONT.

### CUDA SDK CONT.

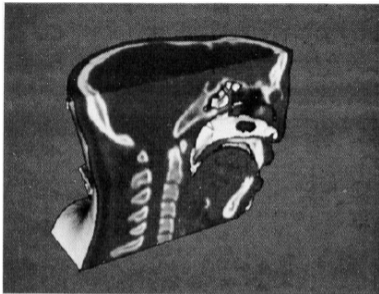


Figure 11. Sagittal Cut with Texture Mapping.

CT data, shows the slice data in relation to the constructed

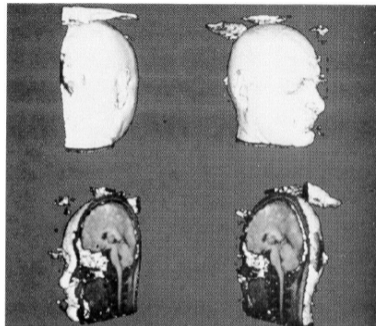


Figure 12. Rotated Sequence of Cut MR Brain.

Interesting for medical  
images (CT,MR)

→ <https://dl.acm.org/citation.cfm?doid=37402.37422>

# PROFILING CUDA CODE

CUDA SDK CONT.

The main profiling tool in CUDA nowadays is NVIDIA Nsight Compute

- nsys nvprof (quick and easy)
- nsys/nsys-ui (for system traces and timeline analysis – streams)
- ncu/ncu-ui (for detailed kernel optimization)

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cuda-zen sh@n3073-004:~$ ncu -f -set full -o profile ./a.out
cuda-zen sh@gui3068-009:~$ ncu-ui ./profile.ncu-rep
```

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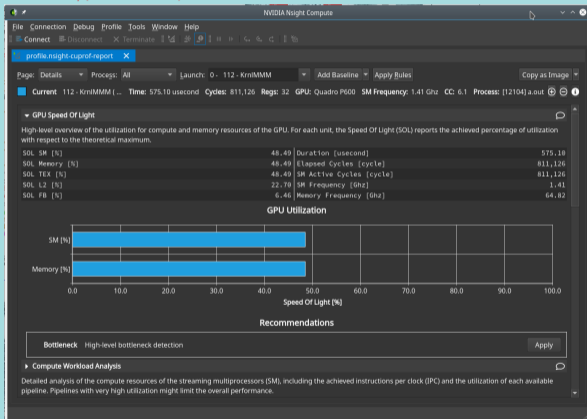
### 3. Visualize profile

→ <https://docs.nvidia.com/nsight-compute/NsightComputeCli/index.html>

# PROFILING CUDA CODE CONT.

## CUDA SDK CONT.

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cuda-zen sh@gui3068-009:~$ ncu-ui ./profile.ncu-rep
```

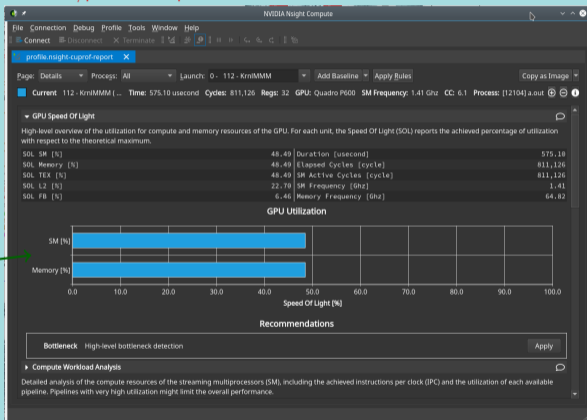


# PROFILING CUDA CODE CONT.

## CUDA SDK CONT.

```
cuda-zen sh@gui3068-009:~$ ncu-ui ./profile.ncu-rep
```

GPU features evaluated w.r.2 theoretical max (SOL)



# PROFILING CUDA CODE CONT.

## CUDA SDK CONT.

```
cuda-zen sh@gui3068-009:~$ ncu-ui ./profile.ncu-rep
```

The screenshot displays the NVIDIA Night Compute application window. The title bar reads "NVIDIA Night Compute". The menu bar includes "File", "Connection", "Debug", "Profile", "Tools", "Window", and "Help". The toolbar contains buttons for "Connect", "Disconnect", "Terminate", and a search icon. Below the toolbar, a tab labeled "profile.night-cuprof-report" is active. The main interface shows a summary of the current profile: "Current: 112 - KrnlMM ( ... Time: 575.10 usecond Cycles: 811,126 Regs: 32 GPU: Quadro P600 SM Frequency: 1.41 Ghz CC: 6.1 Process: [12104] a.out".

Below the summary, there are three expandable sections:

- Compute Workload Analysis**: Detailed analysis of the compute resources of the streaming multiprocessors (SM), including the achieved instructions per clock (IPC) and the utilization of each available pipeline. Pipelines with very high utilization might limit the overall performance.

| Executed Ipc Elapsed [1inst/cycle] | 0.91 | SM Busy [%]          | 48.49 |
|------------------------------------|------|----------------------|-------|
| Executed Ipc Active [1inst/cycle]  | 0.92 | Issue Slots Busy [%] | 15.37 |
| Issued Ipc Active [1inst/cycle]    | 0.92 | -                    | -     |
- Memory Workload Analysis**: Detailed analysis of the memory resources of the GPU. Memory can become a limiting factor for the overall kernel performance when fully utilizing the involved hardware units (Mem Busy), exhausting the available communication bandwidth between those units (Max Bandwidth), or by reaching the maximum throughput of issuing memory instructions (Mem Pipes Busy). Depending on the limiting factor, the memory chart and tables allow to identify the exact bottleneck in the memory system.

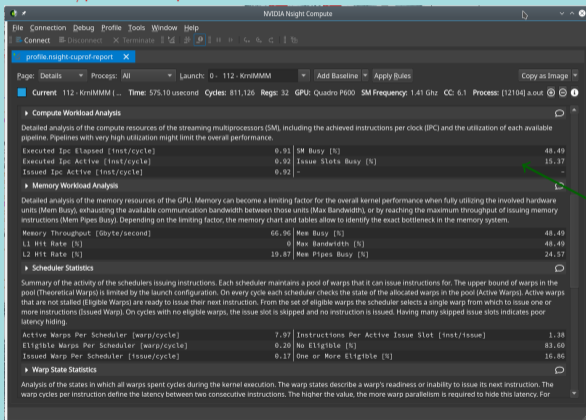
| Memory Throughput [Gbyte/second] | 66.96 | Mem Busy [%]       | 48.49 |
|----------------------------------|-------|--------------------|-------|
| L1 Hit Rate [%]                  | 0     | Max Bandwidth [%]  | 48.49 |
| L2 Hit Rate [%]                  | 19.87 | Mem Pipes Busy [%] | 24.57 |
- Scheduler Statistics**: Summary of the activity of the schedulers issuing instructions. Each scheduler maintains a pool of warps that it can issue instructions for. The upper bound of warps in the pool (Theoretical Warps) is limited by the launch configuration. On every cycle each scheduler checks the state of the allocated warps in the pool (Active Warps). Active warps that are not stalled (Eligible Warps) are ready to issue their next instruction. From the set of eligible warps the scheduler selects a single warp from which to issue one or more instructions (Issued Warp). On cycles with no eligible warps, the issue slot is skipped and no instruction is issued. Having many skipped issue slots indicates poor latency hiding.

| Active Warps Per Scheduler [warp/cycle]   | 7.97 | Instructions Per Active Issue Slot [1inst/issue] | 1.38  |
|-------------------------------------------|------|--------------------------------------------------|-------|
| Eligible Warps Per Scheduler [warp/cycle] | 0.20 | No Eligible [%]                                  | 83.60 |
| Issued Warp Per Scheduler [1issue/cycle]  | 0.17 | One or More Eligible [%]                         | 16.86 |
- Warp State Statistics**: Analysis of the states in which all warps spent cycles during the kernel execution. The warp states describe a warp's readiness or inability to issue its next instruction. The warp cycles per instruction define the latency between two consecutive instructions. The higher the value, the more warp parallelism is required to hide this latency. For

# PROFILING CUDA CODE CONT.

## CUDA SDK CONT.

```
cuda-zen sh@gui3068-009:~$ ncu-ui ./profile.ncu-rep
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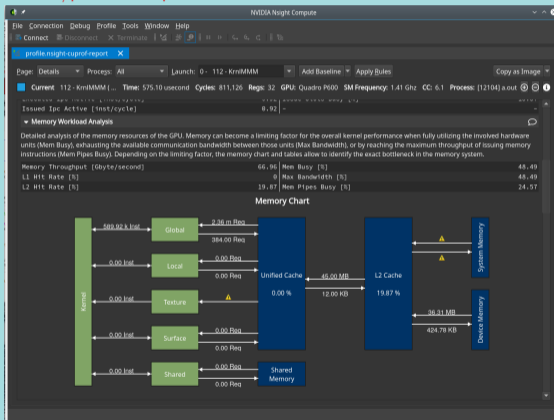


Different categories' evaluation

# PROFILING CUDA CODE CONT.

## CUDA SDK CONT.

```
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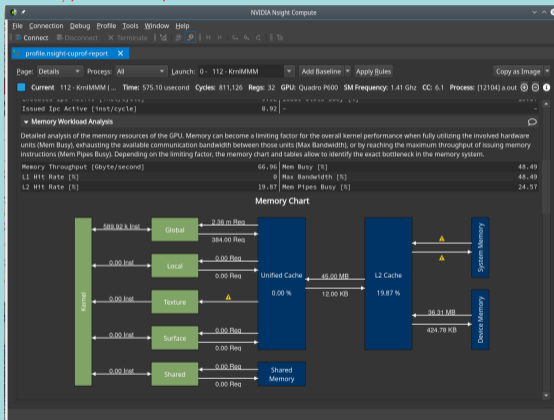
# PROFILING CUDA CODE CONT.

## CUDA SDK CONT.

```
cuda-zen sh@gui3068-009:~$
```

```
ncu-ui ./profile.ncu-rep
```

Expandable  
detail  
sections



- The Heterogeneous Interface for Portability (HIP) is AMD's dedicated GPU programming environment (e.g. to program MI250X/MI300X devices)
- Very similar to CUDA
- HIP code will also run on NVIDIA platforms
- HIP forms another ecosystem with tools, libraries, etc
- Every basic CUDA construct has a direct counterpart in HIP

# HIP CONT.

## HIP EXAMPLE

### Vector Addition with HIP

```
// HIP kernel. Each thread takes care of one element of c;
__global__ void vecAdd(double *a, double *b, double *c, int n)
{
 // Get our global thread ID
 int id = (blockIdx.x * blockDim.x) + threadIdx.x;
 // Make sure we do not go beyond bounds
 if (id < n)
 c[id] = a[id] + b[id];
}

int main()
{
 ...
 // Execute the kernel with n threads
 hipLaunchKernelGGL(vecAdd, dim3(gridSize), dim3(blockSize), 0, 0, d_a, d_b, d_c, n);
 hipDeviceSynchronize();
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```

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same kernel  
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same kernel  
declaration  
specifiers

same built-in  
variables,  
e.g. threadIdx.x=0,1,2...

different kernel  
execution  
configuration

# HIP CONT.

## COMPILE AND RUN AND MONITOR

```
(zen3) [sh@some - mi250x ~]$ hipcc vadd_hip.cpp
(zen3) [sh@some - mi250x ~]$./a.out

0 100.000000
1 100.000000
2 100.000000
3 100.000000
4 100.000000
5 100.000000
6 100.000000
7 100.000000
8 100.000000
9 100.000000
10 100.000000
11 100.000000
...
99 100.000000
```

- <https://developer.amd.com/wp-content/resources/ROCm%20Learning%20Centre/chapter3/HIP-Coding-3.pdf>
- [https://rocm.docs.amd.com/en/latest/Programming\\_Guides/HIP-porting-guide.html](https://rocm.docs.amd.com/en/latest/Programming_Guides/HIP-porting-guide.html)
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```

```
0 100.000000
1 100.000000
2 100.000000
3 100.000000
4 100.000000
5 100.000000
6 100.000000
7 100.000000
8 100.000000
9 100.000000
10 100.000000
11 100.000000
...
99 100.000000
```

```
tictoc@TickTockArch $ rocm-smi

=====ROCM System Management Interface=====
GPU Temp AvgPwr SCLK MCLK Fan Perf PwrCap VRAM% GPU%
0 42.0c 294.0W 1925Mhz 1000Mhz 0.0% high 450.0W 17% 100%
1 50.0c 219.0W 1772Mhz 1000Mhz 0.0% high 220.0W 4% 100%
2 45.0c 273.0W 1925Mhz 1000Mhz 0.0% high 300.0W 4% 100%
3 55.0c 163.0W 1700Mhz 1000Mhz 0.0% high 170.0W 4% 100%
=====End of ROCm SMI Log =====

tictoc@TickTockArch $ _
```

- <https://developer.amd.com/wp-content/resources/ROCM%20Learning%20Centre/chapter3/HIP-Coding-3.pdf>
- [https://rocmdocs.amd.com/en/latest/Programming\\_Guides/HIP-porting-guide.html](https://rocmdocs.amd.com/en/latest/Programming_Guides/HIP-porting-guide.html)
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- Taking advantage of fast FP32 operations with quasi-FP64 accuracy on consumer grade cards requires a couple of algorithmic changes
- NVIDIA's NSIGHT compute is an advanced profiling tool for in-depth kernel optimization
- AMD's HIP is very similar to CUDA and kernel code can be directly interchanged