

Q N ①

#

1

left

Right

3 children (boat) →

3 adult

Planning Problem

PDOL description

Constants: $c_1 c_2 c_3 A_1 A_2 A_3$

Predicates:

ischild(x) = x is a child

isadult(x) = x is an adult

onleft(x) = x is on left side of river

onright(x) = x is on right side of river

moveleft(x, y) = x and y moves to left side of river

moveright(x, y) = x and y moves to right side of river

boat(x) = x is a boat

initial state

ischild(c_1) \wedge ischild(c_2) \wedge ischild(c_3) \wedge

isadult(A_1) \wedge isadult(A_2) \wedge isadult(A_3) \wedge

onleft(c_1) \wedge onleft(c_2) \wedge onleft(c_3) \wedge

onleft(A_1) \wedge onleft(A_2) \wedge onleft(A_3) \wedge

Initial state:

onRight(c_1) \wedge onRight(c_2) \wedge onRight(c_3) \wedge onRight(A_1) \wedge
onRight(A_2) \wedge onRight(A_3)

Action:

move A-C from L to R (x, y)

Preccond:

onLeft(x) \wedge onLeft(y) \wedge onLeft(boat) \wedge isChild(x) \wedge isAdult(y)

effect:

onRight(x) \wedge onRight(y) \wedge \neg onLeft(x) \wedge \neg onLeft(y)

Action:

move A-C from R to L (x, y)

Preccond:

onRight(x) \wedge onRight(y) \wedge onRight(boat) \wedge isChild(x) \wedge
isAdult(y)

effect:

onLeft(x) \wedge onLeft(y) \wedge \neg onRight(x) \wedge \neg onRight(y)

Action:

move C-C from L to R (x, y)

Preccond:

onLeft(x) \wedge onLeft(y) \wedge onLeft(boat) \wedge isChild(x) \wedge isAdult(y)

effect:

onRight(x) \wedge onRight(y) \wedge \neg onLeft(x) \wedge \neg onLeft(y)

1 ✓
2
3
4
5 ✓
6

action:

move C-C-R to L (n,y)

precond:

onright(x) \wedge onright(y) \wedge onright(boat) \wedge ischild(x) \wedge ischild(y)

effect:

onleft(n) \wedge onleft(y) \wedge \neg onright(x) \wedge \neg onright(y)

action:

move adult - L to R (n)

precond:

onleft(x) \wedge onleft(boat) \wedge isadult(x)

effect:

onright(x) \wedge \neg onleft(x)

action:

move adult - R to L (n)

precond:

onright(x) \wedge onright(boat) \wedge isadult(x)

effect:

onleft(x) \wedge \neg onright(x)

action:

move child - L to - R (n)

precond:

onleft(x) \wedge onleft(boat) \wedge ischild(x)

effect:

onright(x) \wedge \neg onleft(x)

action: move child - R to - L (n)

precond: onright(x) \wedge onright(boat) \wedge ischild(x)

effect: onleft(x) \wedge \neg onright(x)

Q N(2)

② ⑥

$$P(A=2 \vee B=4)$$

$$P(A=2) + P(B=4) - P(P(A)=2 \wedge P(B=4))$$

Now,

$$\begin{aligned} P(A=2) &= 0.0061 + 0.0174 + 0.0342 + 0.0599 + 0.0603 \\ &= 0.1779 \end{aligned}$$

$$\begin{aligned} P(B=4) &= 0.0571 + 0.0599 + 0.0303 + 0.0497 + 0.0524 \\ &= 0.2554 \end{aligned}$$

Now,

$$\begin{aligned} P &= 0.1779 + 0.2554 - 0.0599 \\ &= 0.3734 \end{aligned}$$

⑦ $P(A \neq B)$

$$= 1 - P(A=B)$$

$$= 1 - (0.0509 + 0.0174 + 0.0598 + 0.0497 + 0.0424)$$

$$= 1 - 0.2202$$

$$= 0.7798$$

(d) $P(A|B) = P(A)$ for totally independent
let

$$A = (A=1), B = (B=1)$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{0.0509}{0.1168} = 0.4358$$

$$P(A) = P(A=1) = \frac{0.0509 + 0.0566 + 0.0079 + 0.0571}{0.0395} = 0.212$$

Therefore,

$P(A|B) \neq P(A)$ so they are totally independent

RN(5)

① Patrons → WaitEstimate → Hungry → Alternate

Rainy
↓

T

output will
wait

② Patrons → leftmost child (None)

output will not wait

③ Patrons → WaitEstimate → Alternate

Fri|sat ?
↓

T

output will wait

initial entropy

Q.N(6)

$$= -\frac{6}{12} \log \frac{6}{12} - \frac{6}{12} \log \frac{6}{12}$$
$$= 1$$

(6)

A	total	1	2	3
X	6	2	2	2
Y	6	2	2	2

For A,

$$I = 1 - \frac{4}{12} H\left(\frac{2}{4}, \frac{2}{4}\right) - \frac{4}{12} H\left(\frac{2}{4}, \frac{2}{4}\right) - \frac{4}{12} H\left(\frac{2}{4}, \frac{2}{4}\right)$$

$$= 1 - \frac{2}{3} \left(-\log_2 \frac{2}{4} - \log_2 \frac{2}{4} \right) - \frac{2}{3} \left(-\log_2 \frac{2}{4} - \log_2 \frac{2}{4} \right)$$

$$- \frac{2}{3} \left(-\log_2 \frac{2}{4} - \log_2 \frac{2}{4} \right)$$

$$= 1 - \frac{2}{3} \left(2 \right) \cdot \frac{2}{3} \left(2 \right) - \frac{2}{3} \left(2 \right)$$

$$= 1 - \frac{1}{3} - \frac{1}{3} - \frac{1}{3}$$

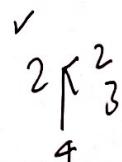
$$= 0 \quad (\text{Information gained})$$

For b,

B	total	1	2	3
X	6	1	2	3
Y	6	1	3	2

$$\begin{aligned}
 I &= 1 - \frac{2}{12} H\left(\frac{1}{2}, \frac{1}{2}\right) - \frac{5}{12} H\left(\frac{2}{5}, \frac{3}{5}\right) - \frac{5}{12} H\left(\frac{3}{5}, \frac{2}{5}\right) \\
 &= 1 - \frac{1}{6} \left(1 \times -\log_2 \frac{1}{2} - 1 \log_2 \frac{1}{2} \right) - \frac{5}{12} \left(-\log_2 \frac{2}{5} \times \frac{2}{5} - \frac{3}{5} \log_2 \frac{3}{5} \right) \\
 &\quad - \frac{5}{12} \left(\frac{3}{5} \times -\log_2 \frac{3}{5} - \frac{2}{5} \log_2 \frac{2}{5} \right) \\
 &= 1 - \frac{1}{6} - \frac{5}{12} (0.9709) - \frac{5}{12} (0.9709) \\
 &= 0.0243
 \end{aligned}$$

1V 5V



①

For C,

C	total	1	2	3
X	6	4	2	0
Y	6	0	2	4

$$I = 1 - \frac{4}{12} H\left(\frac{4}{4}, \frac{0}{4}\right) - \frac{4}{12} \left(\frac{2}{4}, \frac{2}{4}\right) - \frac{4}{12} \left(0, \frac{4}{4}\right)$$

$$= 1 - \frac{4}{12} \left(-1 \log_2 \frac{4}{4} - 0 \log_2 0\right) - \frac{4}{12} \left(-\frac{2}{4} \times \log_2 \frac{2}{4} - \frac{2}{4} \times \log_2 \frac{2}{4}\right) \\ - \frac{4}{12} \left(0 - 1 \log_2 \frac{4}{4}\right)$$

$$= 1 - \frac{4}{12} \times 0 - \frac{4}{12} \times 1 - \frac{4}{12} \times 0$$

$$= 1 - \frac{4}{12} \times \frac{1}{3}$$

$$= 0.6667$$

Therefore, information gained of C is greater than A and B
so, attribute C is best to use as a test in the root of the tree.