

AI

Homework

Task ①

Constants :  $B_1 \ B_2 \ B_3 \} \rightarrow B$

$R_1 \ R_2 \ R_3 \} \rightarrow R$

$P_1 \ P_2$

Predicate : move( $R$ ) : move 2 red from  $P_2$  to  $P_1$

move( $B$ ) = move 2 blue from  $P_2$  to  $P_1$

move( $x$ ) : move 1 red and 1 Blue from  $P_1$  to  $P_2$

at( $a, b, c$ ) : a number of  $b$  ball is in  $c$ . bucket

states : at( $3, R, P_1$ ) }

at( $3, B, P_2$ ) }  $\rightarrow$  precondition

action :

move( $R$ )

move( $B$ )

move( $x$ )

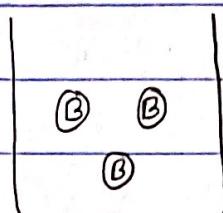
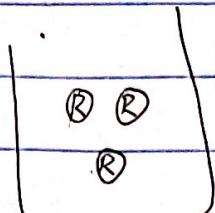
effect

at( $3, B, P_1$ )

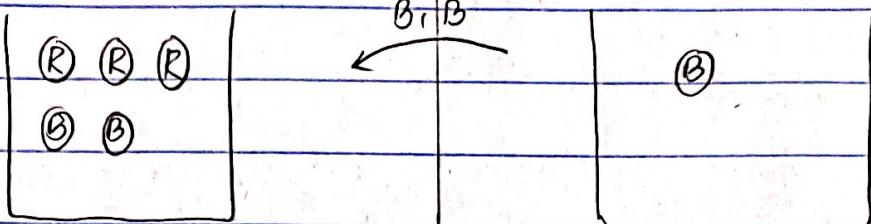
at( $3, R, P_2$ )

BN ①

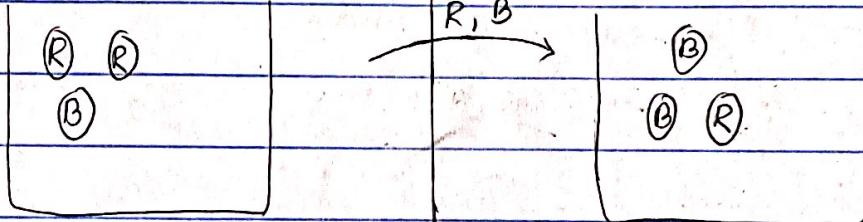
Ans:



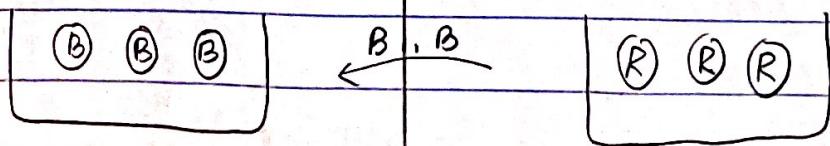
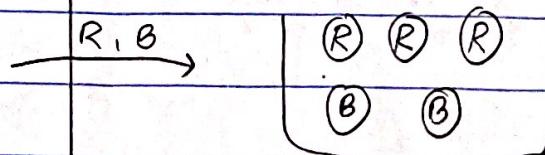
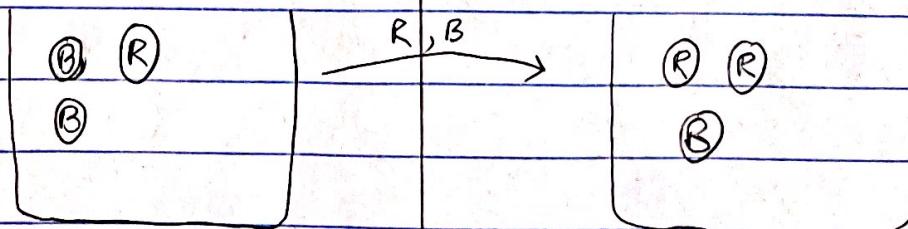
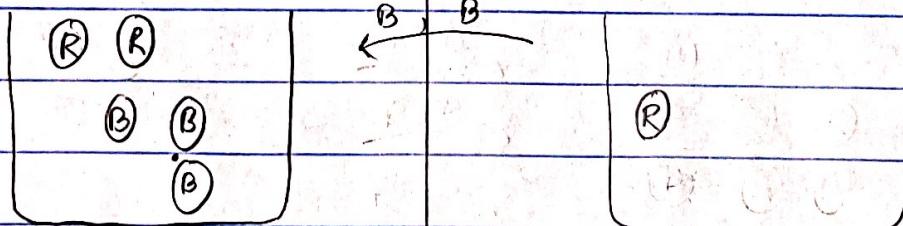
Case 1



Case 2



Case 3



Task

(2)

Here, JUNGLE

there are 4 predicates, each predicate takes at most 3 arguments [1..3] and 5 constants

Possible arguments is

$$\text{at least} = 4 \times 5^1 = 20$$

$$\text{at most} = 4 \times 5^3 = 500$$

So,

number of possible unique states :

$$\text{at least} = 2^{20}$$

$$\text{at most} = 2^{500}$$

## Task

(3)

a)  $P(\text{Color Green}) = 0.36$

$$P(\text{not Green}) = 1 - 0.36 = 0.64$$

$$P(\text{Truck}) = 0.24$$

$$P(\text{not Green} \mid \text{Truck}) = \frac{0.64 \times 0.24}{0.24} = 0.64$$

b)  $P(\text{Color Green} \mid \text{Truck}) = 1 - 0.64 = 0.36$

$$P(\text{Color Green}) = 0.36$$

Here,

$$P(\text{Color Green} \mid \text{Truck}) = P(\text{Color Green})$$

Therefore, vehicle and color are totally independent from each other.

Task

(4)

a) <u>Variable</u>	<u>Possible values</u>	<u>Number.</u>
A	8	1
B	5	10
C	6	1

$$\text{By Joint distribution} = 8^1 \times 5^{10} \times 6^1 \\ = 468750000$$

But

we need to store =  $(468750000 - 1)$  values

$$b) P(A) = 8-1 = 7 \text{ values}$$

$$P(B) = 10 \times (5-1) = 40 \text{ values}$$

$$P(C) = 6-1 = 5 \text{ values}$$

$$\text{We need to store} = 7 \times 40 \times 5 \\ = 1400 \text{ numbers}$$

(5)

baseball-game-on-TV



George-watches-TV

George-Feeds-Cat

out-of-cat-food



Task

T (6)

$$P(\text{baseball-game-on-TV}) = 0.3041 \quad (4)$$

$$P(\text{out-of-cat-food}) = 0.1699 \quad (D)$$

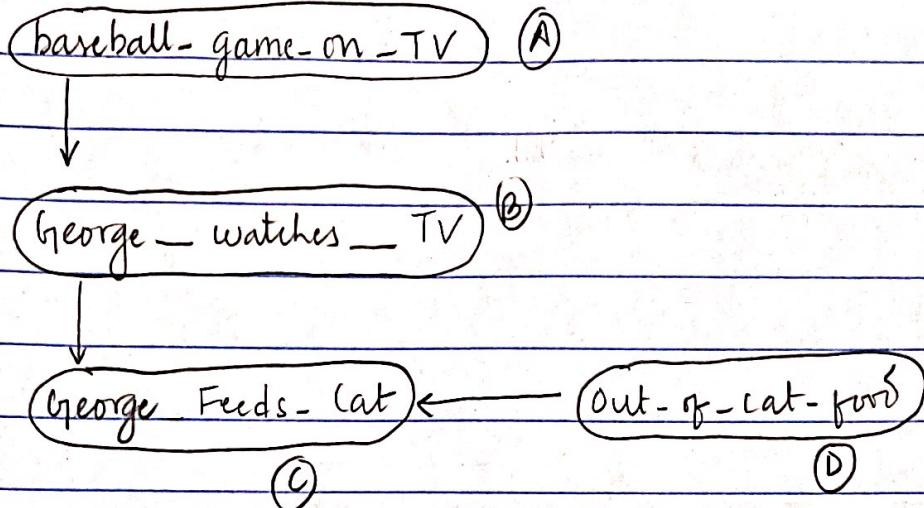
$P(\text{baseball-game-on-TV}) \quad (A)$		$P(\text{George-watches-TV}) \quad (B)$
T		0.9279
F		0.11811

$P(\text{George-watches-TV}) \quad (B)$	$P(\text{out-of-cat-food}) \quad (D)$	$P(\text{George-feeds-cat}) \quad (C)$
T	T	0.0416
T	F	0.7064
F	T	0.31576
F	F	0.95876

Task

(7)

let



$$P(A | \neg C)$$

$$= P(A, \neg C)$$

$P(C)$  Taking Numerator

$$\begin{aligned} &= P(A, \neg C, B, D) + P(A, \neg C, \neg B, D) + \\ &\quad P(A, \neg C, \neg B, \neg D) + P(A, \neg C, B, \neg D) \\ &= P(A) \times P(\neg C | B, D) \times P(B | A) \times P(D) + \\ &\quad P(A) \times P(\neg C | \neg B, D) \times P(\neg B | A) \times P(D) + \\ &\quad P(A) \times P(\neg C | \neg B, \neg D) \times P(\neg B | A) \times P(\neg D) + \\ &\quad P(A) \times P(\neg C | B, \neg D) \times P(B | A) \times P(\neg D) \\ &= 0.3041 \times (1 - 0.0416) \times (0.9279) \times 0.1699 + \\ &\quad 0.3041 \times (1 - 0.95876) \times (1 - 0.9279) \times (1 - 0.1699) + \\ &\quad 0.3041 \times (1 - 0.31576) \times (1 - 0.9279) \times 0.1699 + \\ &\quad 0.3041 \times (1 - 0.7064) \times (0.9279) \times (1 - 0.1699) \\ &= 0.1111 \end{aligned}$$

Taking denominator

$$\begin{aligned} P(C) &= P(C, B, D, A) + P(C, B, \neg D, A) + P(C, B, D, \neg A) \\ &\quad P(C, \neg B, \neg D, A) + P(C, B, \neg D, \neg A) + P(C, \neg B, D, A) \\ &\quad P(C, \neg B, \neg D, A) + P(C, \neg B, D, \neg A) \\ \\ &= P(C) \times P(B|A) \times P(D) \times P(A) + \\ &\quad P(C) \times P(B|A) \times P(\neg D) \times P(A) + \\ &\quad P(C) \times P(B|A) \times P(D) \times P(\neg A) + \\ &\quad P(C) \times P(\neg B|A) \times P(\neg D) \times P(\neg A) + \\ &\quad P(C) \times P(\neg B|A) \times P(\neg D) \times P(A) + \\ &\quad P(C) \times P(\neg B|A) \times P(\neg D) \times P(A) + \\ &\quad P(C) \times P(\neg B|A) \times P(D) \times P(\neg A) \\ \\ &= x \text{ (say)} \end{aligned}$$

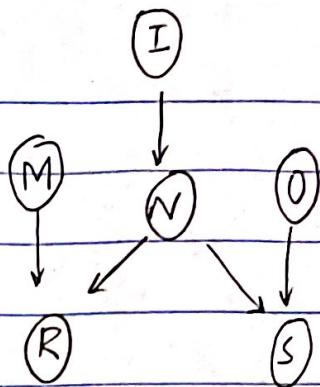
Now,

Finally

$$= \frac{0.1111}{x}$$

Task 8

a) For Node N



Parents	I
Children	R, S
Children other Parents	M, O

So,

Markov blanket of Node N = I, R, S, M, O

b)

$$P(I, D)$$

$$= P(I, D) \times P(D)$$

$$= 0.5 \times 0.5$$

$$= 0.25$$

c)

$$P(M, \text{not}(C), H)$$

$$= \frac{P(M, \neg C, H)}{P(H)}$$

$$= \frac{P(M|H) \times P(\neg C) \times P(H|\neg C)}{P(H, C) + P(H, \neg C)}$$

$$= \frac{0.1 \times 0.4 \times 0.1}{0.6 \times 0.6 + 0.1 \times 0.4} = \frac{0.004}{0.36 + 0.04} = 0.01$$