

# Assignment 3

## Task 1

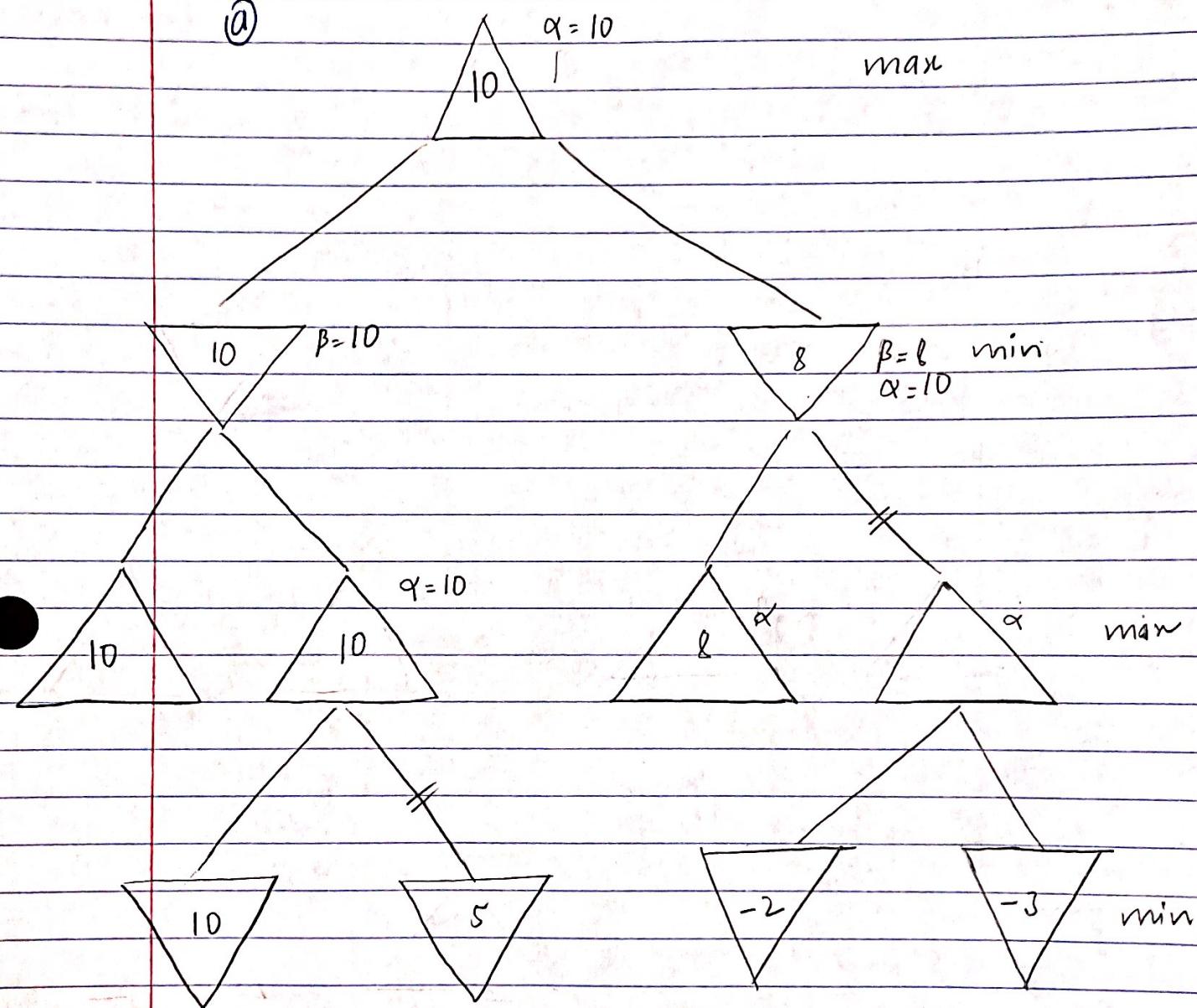
	X	O
max(0)	O	X
X	O	

X		0											
min(0)	0	X	X		X	X	0			X		0	
X	0				0		X			0		X	
					X	0				X	0	X	
					min(0)								
						max				max		max	
max	X	0	0		X		0			X	0	0	
	0	X	X		0	X	X			0	X	0	X
	X	0			X	0	0			X	0	X	
+1					0					+1			0
										max		max	
										X	X	0	X
										0	0	X	0
										X	0		X
											X	0	0
										0			0

$$\begin{array}{c} \alpha \uparrow \\ \beta \downarrow \\ \alpha \geq \beta \end{array}$$

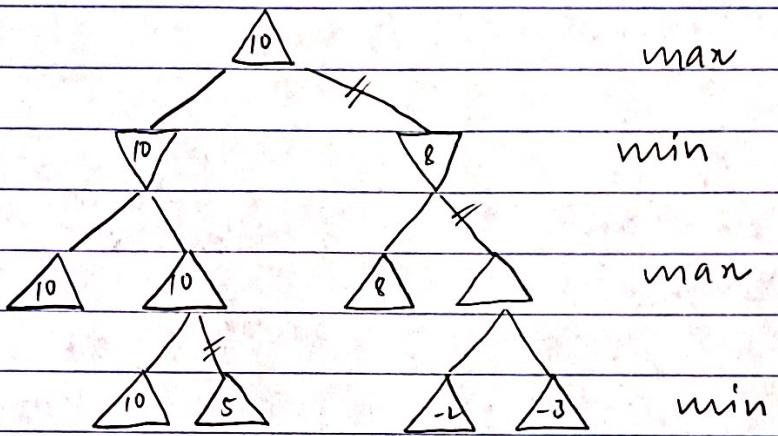
Task 2

(a)



## Task 2 (b)

Ans If we know that max utility value is 10, then any max node can stop exploring after it finds a Max value of 10



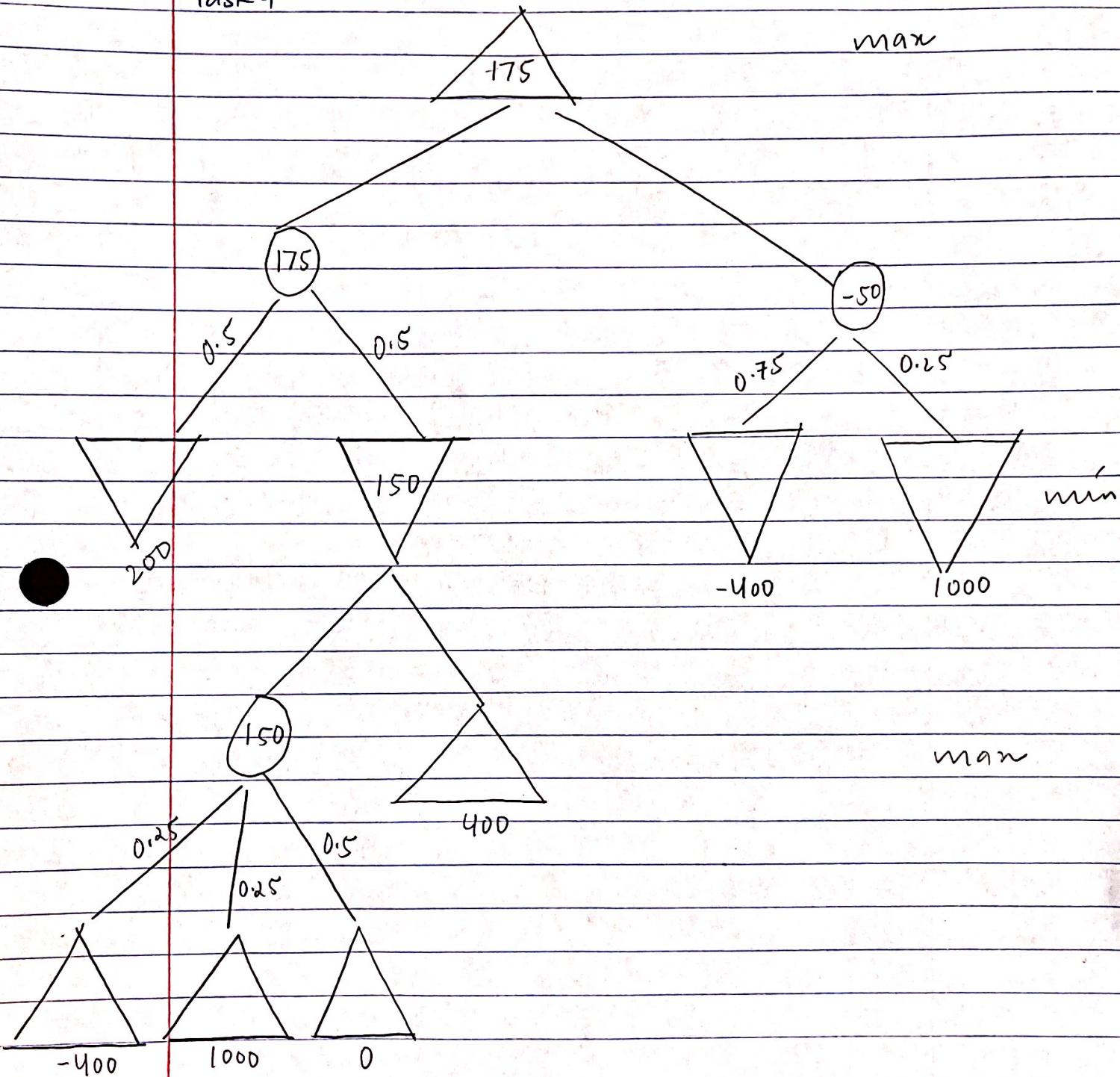
Here, maximum utility is 10, all the other value on the right side will be pruned.

## Task 3

Ans → Regular minmax will give the optimal decision. However, we can use DeepGreenMove(s) to reduce the amount of work we have to do.

function MinValue(state) returns a utility value  
if TerminalTest(state) then return Utility(state)  
else  
return MaxValue(DeepGreenMove(s))

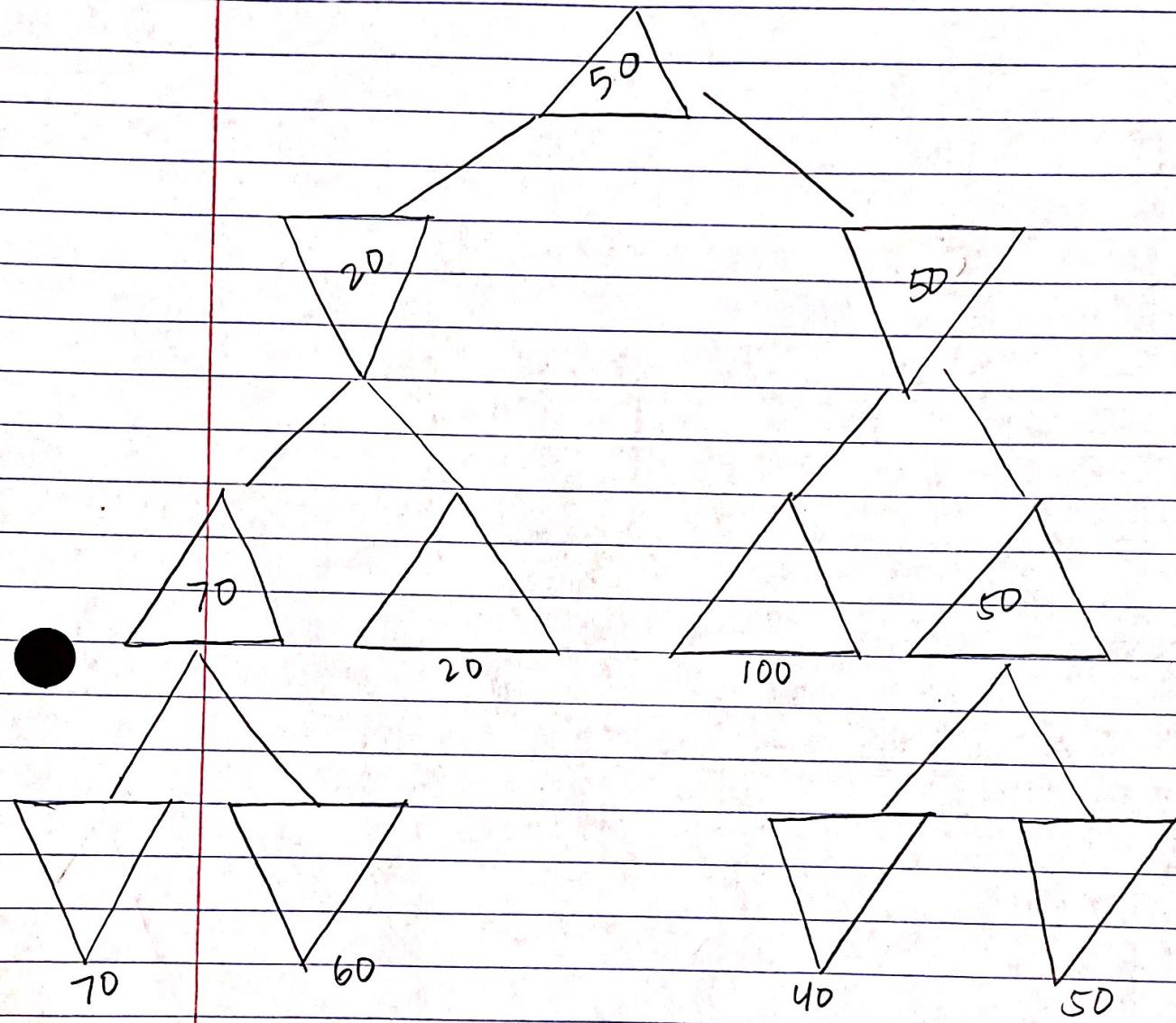
### Task 4



lowest possible outcome = -50

highest possible outcome = 175

### Task 5



The best possible outcome for MAX player is 100 if opponent does not try to minimize.

The worst possible outcome for MAX player is 50 if the opponent tries to minimize.

## Task 6

Ans: function CHECK-EQUIVALENCE( $KB_1, KB_2$ )

    returns true or false

{

        if TT-Entails( $KB_1, KB_2$ ) and TT-Entails( $KB_2, KB_1$ )

            return true

        else

            return false

}

## Task 7

- a. Yes,  $K_B$  entail  $S_1$  because for all the values where  $K_B$  is true,  $S_1$  is also true  
(Rows: 1, 3, 7)
- b. There are certain rows where  $\text{NOT}(K_B)$  is true but  $\text{NOT}(S_1)$  is not true. So,  $\text{NOT}(K_B)$  does not entail statement  $\text{NOT}(S_1)$ . (Rows: 2, 4)

### Task 8

Cases	A	B	C	D	$\neg B$
1	T	F	T	T	F
2	F	F	T	F	F

In other cases, where  $\neg B$  is true

1 Cases	A	B	C	D	$\neg B$
1 <sup>st</sup>	F	T	F	F	T
2 <sup>nd</sup>	T	T	F	T	T

Conjunctive Normal Form (CNF)

Applying De-Morgan's law  
for

1<sup>st</sup> case:  $\neg A \vee B \vee \neg C \vee \neg D$

2<sup>nd</sup> case:  $A \vee B \vee \neg C \vee D$

### Task 9

$$A \Rightarrow B$$

$$B \Leftrightarrow C$$

$$D \Leftrightarrow A$$

$$E \Rightarrow D$$

$$C \text{ AND } E \Rightarrow F$$

E

i) Forward chaining

$$\begin{array}{c} i) \underline{E} \\ \qquad \underline{E \Rightarrow D} \\ \qquad \qquad D \end{array}$$

$$\begin{array}{c} ii) \underline{D} \\ \qquad \underline{D \Rightarrow A} \\ \qquad \qquad A \end{array}$$

$$\begin{array}{c} iii) \underline{A} \\ \qquad \underline{A \Rightarrow B} \\ \qquad \qquad B \end{array}$$

$$\begin{array}{c} iv) \underline{B} \\ \qquad \underline{B \Leftrightarrow C} \\ \qquad \qquad C \end{array}$$

$$\begin{array}{c} v) \underline{(C \wedge E) \Rightarrow F} \\ \qquad \qquad \qquad F \end{array}$$

ii) Backwards chaining

$$\begin{array}{c} i) \underline{(C \wedge E) \Rightarrow F} \\ \qquad \qquad \qquad F \end{array}$$

$$\begin{array}{c} ii) \underline{B} \\ \qquad \underline{B \Leftrightarrow C} \\ \qquad \qquad C \end{array}$$

$$\begin{array}{c} iii) \underline{A} \\ \qquad \underline{A \Rightarrow B} \\ \qquad \qquad B \end{array}$$

$$\begin{array}{c} iv) \underline{D} \\ \qquad \underline{D \Rightarrow A} \\ \qquad \qquad A \end{array}$$

$$\begin{array}{c} v) \underline{E} \\ \qquad \underline{E \Rightarrow D} \\ \qquad \qquad D \end{array}$$

By using  
Modus Ponens

## Task 9

### 3) Resolution

$(A \Rightarrow B) \wedge (B \Rightarrow C) \wedge (D \Rightarrow A) \wedge (\varepsilon \Rightarrow D) \wedge (C \wedge \varepsilon \Rightarrow F) \wedge \varepsilon$   
using implication elimination

$$(\neg A \vee B) \wedge (\neg B \vee C) \wedge (\neg C \vee D) \wedge (\neg D \vee A) \wedge (\neg \varepsilon \vee D) \\ \wedge (\neg C \vee \neg \varepsilon \vee F) \wedge \varepsilon$$

Add  $\neg F$   
resolving

$$\neg F \quad \neg C \vee \neg \varepsilon \vee \neg F$$

$$\rightarrow \neg C \vee \neg \varepsilon$$

$$\neg F \vee \neg \varepsilon \quad \underline{\neg B \vee \neg F}$$

$$\rightarrow \neg \varepsilon \vee \neg B$$

$$\neg \varepsilon \vee \neg B \quad \underline{\neg \varepsilon \vee B}$$

$$\rightarrow \neg \varepsilon$$

$$\neg \varepsilon \quad \varepsilon$$

$\square \rightarrow \text{empty}$

$K_B \neq F$  (false)

Task 10,

constants : John, Mary , April , May , 10,000 check

Predicates :

$\text{rain}(x)$  = it rains in  $x$

$\text{gave}(x, y, z)$  =  $x$  gave  $y$  a check of  $z$

$\text{mow}(x)$  =  $x$  mows the lawn

a. Contract :

$\text{rain}(\text{May}) \Rightarrow \text{gave}(\text{John}, \text{Mary}, 10000)$

$\text{gave}(\text{John}, \text{Mary}, 10000) \Rightarrow \text{mow}(\text{Mary})$

b.

$\neg \text{rain}(\text{May})$

$\text{gave}(\text{John}, \text{Mary}, 10000)$

$\text{mow}(\text{Mary})$

c.

- The contract is not violated because  
 $A \Rightarrow B$  is true always if  $A$  is false.

It means if it rains then John must give the cheque to Mary. But, if it doesn't rain then its upto John whether he gives cheque to Mary or not.

## Task 10

c) Symbols involved are

rain-May

gave-John-Mary-10000

mow-Mary

d) rain-May  $\Rightarrow$  gave-John-Mary-10000

gave-John-Mary-10000  $\Rightarrow$  mow-Mary