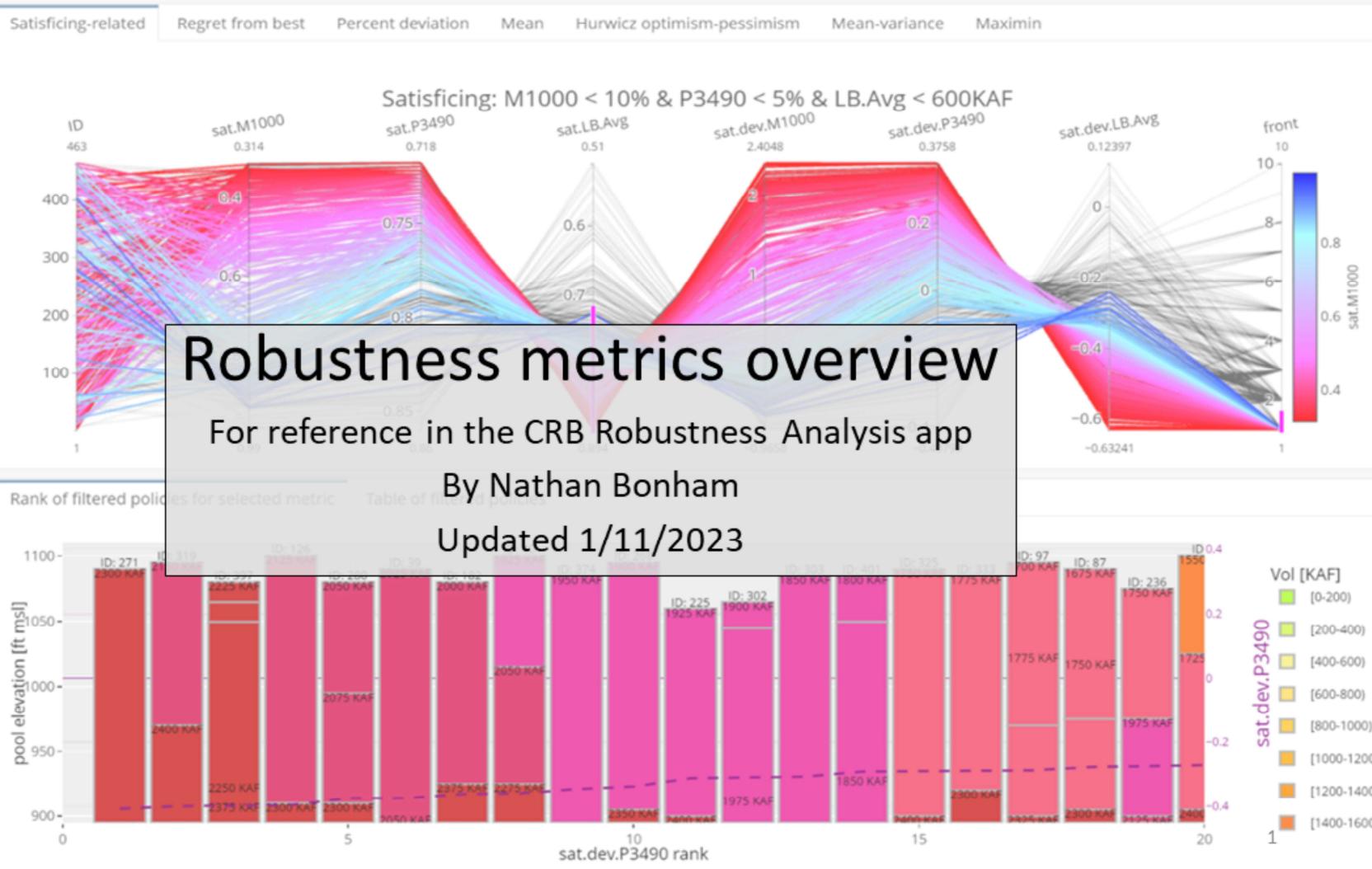


Satisficing calcs ▾



We recommend downloading this document and having it open alongside the app for reference.

# Contents

- Define robustness
- How robustness is assessed in the Colorado River Basin with Many Objective Robust Decision Making
- How robustness metrics are calculated

# What is robustness?

- A robust solution “perform(s) well under a range of plausible conditions” (McPhail et al. 2018)
- In the Colorado River Basin (CRB) context, we desire operation policies that perform ‘well’ in water supply and storage objectives when tested in many plausible realizations of streamflow and demand.

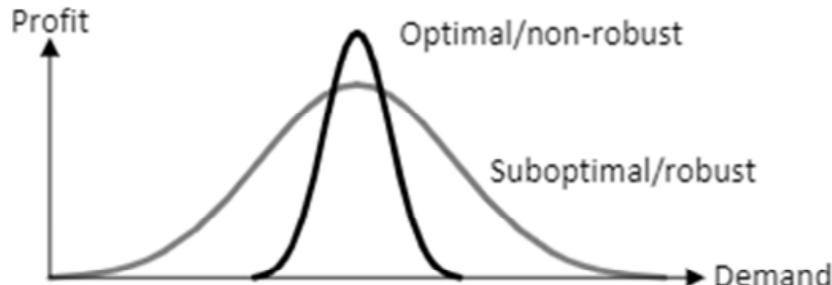


Fig. 1. Illustration of robustness.

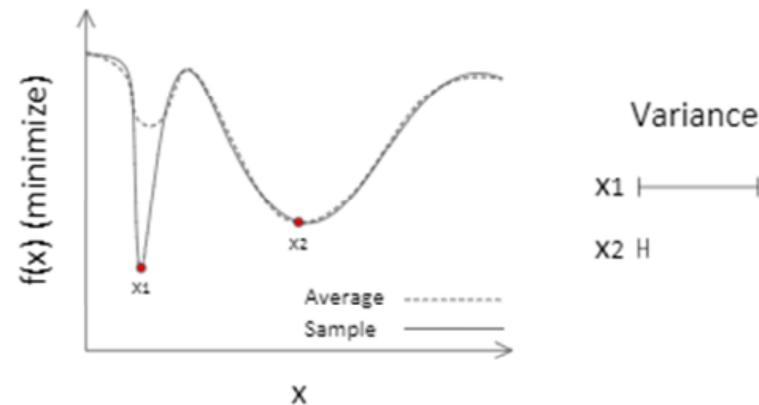


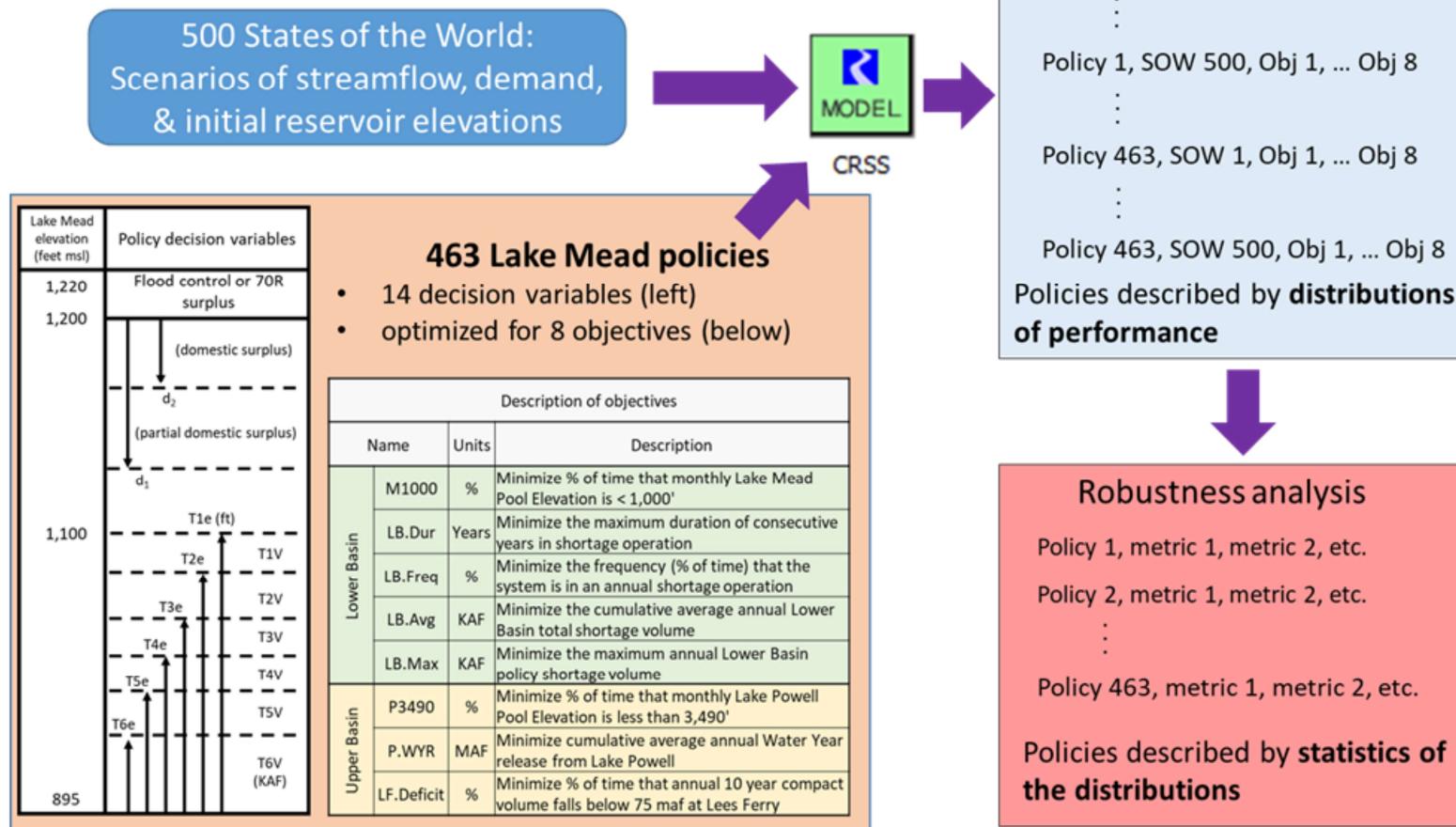
Fig. 2. Example of a sample versus a robust optimal solution for a function  $f(x)$ .

Figures from Syberfeldt and Gustavsson 2014

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Both figures are examples where the globally optimal solution is highly sensitive to changes in another variable. In contrast, the performance of the robust solution suffers less when the uncertain variable changes.

# How is robustness calculated in Many Objective Robust Decision Making?



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We provide an example of how robustness is assessed in the Many Objective Robust Decision Making framework using our Colorado River Basin (CRB) case study. 463 operation policies are each simulated in 500 plausible states of the world (SOW) using the Colorado River Simulation System (CRSS). The operation policies were identified in previous research using the Borg Many Objective Evolutionary Algorithm coupled with CRSS. The result of simulating all policies in all SOW is that each policy is described by distributions of performance in the objectives. Robustness analysis is the process of summarizing the distributions of performance as scalar values by applying one or more statistical functions. The statistical functions are called robustness metrics. The figure describes the process of evaluating policy robustness, but keep in mind that copious robustness metrics exist and the analyst should consider how they are calculated and what the implications might be on robustness magnitude and ranking of the policies.

\*\*\*Note: LB stands for Lower Basin

# Robustness metric summary table

Category	Name	Definition	Interpretation	Transformation of objective	SOW used	Normalization factor	Summary statistic
threshold	Satisficing	The fraction of SOW where a given policy satisfies user-defined performance thresholds.	1 indicates the performance thresholds have been satisfied in every SOW, whereas 0 indicates the thresholds are violated in every SOW.	Satisfactory (1) or Not Satisfactory (0)	All	None	mean
threshold & regret	Satisficing deviation	The average percent by which a policy satisfies a user-defined performance threshold.	Negative percentages indicate performance better than the threshold, and positive indicates performance worse than the threshold.	Deviation from satisficing threshold	All	Threshold	mean
regret	Regret from best	The average deviation of a solution's performance in each SOW from the best performance obtained by any policy in each SOW.	0 percent indicates the policy is the best performing policy in every SOW, and greater positive values indicate larger average regret compared to the best performing policies.	Deviation from best performance by any policy in each SOW	All	None	mean
	Percent deviation from optimization	The percent by which the 90th percentile performance of a solution deviates from its performance during optimization.	Positive percentages indicate the policy performs worse during robustness simulations compared to optimization simulations, whereas negative values means the policy performs better (mathematically possible, but doesn't occur in our analysis).	Deviation from optimization performance	90th percentile	Optimization performance	None
No objective transform	Mean (Laplace's Principle of Insufficient Reason)	The performance averaged over the SOW ensemble.	The units and interpretation of each performance objective are maintained (e.g. smaller values are desired for minimization objectives)	None	All	None	mean
	Hurwicz optimism-pessimism	The weighted average of the best and worst case performance.	The units and interpretation of each performance objective are maintained (e.g. smaller values are desired for minimization objectives)	None	Best and worst-cases	None	weighted mean
	Mean-variance	The average performance multiplied by the standard deviation (in the case of minimization objectives).	The units are that of the objective squared. Small values are desirable, indicating small (good) performance that is consistent (low standard deviation) across the SOW	None	All	None	mean x standard deviation
	Maximin	The worst performance obtained by a solution in the SOW ensemble. Alternatively, other percentiles can be used (95th or 90th percentile performance, for example).	The units and interpretation of each performance objective are maintained (e.g. smaller values are desired for minimization objectives)	None	Worst-case (or user-defined percentile)	None	None

See the app's "Example calculations" tab for example calculations for each metric in Google Sheets

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This table serves as a "cheat sheet" for interpreting the robustness metrics supported in the app. The table is divided into the blue section (left), which provides practical information for understanding what each robustness metric is telling you, and the green section (right), which provides details about how the metrics are calculated. The "Transformation of objective" column indicates what, if any, mathematical transformation is performed to the performance objectives. Then, "SOW used" explains if all or a subset of the States of the World (SOW) are used in the calculation. Next, "Normalization factor" defines the denominator used to convert the metric to a percentage or fraction. Lastly, "Summary statistic" lists the statistical moment used to describe the distribution of performance as a scalar value, in the case more than one SOW is used. The app's "Example calculations" tab provides example calculations for each metric in Google Sheets, and it is helpful for understanding what each of the columns in the "Calculation" section means.

# References

- McPhail, C., Maier, H.R., Kwakkel, J.H., Giuliani, M., Castelletti, A., Westra, S., 2018. Robustness Metrics: How Are They Calculated, When Should They Be Used and Why Do They Give Different Results? *Earths Future* 6, 169–191. <https://doi.org/10.1002/2017EF000649>
- McPhail, C., Maier, H.R., Westra, S., van der Linden, L., Kwakkel, J.H., 2021. Guidance framework and software for understanding and achieving system robustness. *Environ. Model. Softw.* 142, 105059. <https://doi.org/10.1016/j.envsoft.2021.105059>
- Syberfeldt, A., Gustavsson, P., 2014. Increased Robustness of Product Sequencing Using Multi-objective Optimization. *Procedia CIRP* 17, 434–439. <https://doi.org/10.1016/j.procir.2014.01.141>

Please email me with questions and comments

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