Problem 1

The convolution of a delta function with any other function generates a shift;

$$\delta(x - m) \circledast f(x) = \sum_{\chi} f(x - \chi)\delta(\chi - m) = f(x - m) \tag{1}$$

then, the shifted Gaussian looks like: