Name: Nachiketh Reddy

ID: 2117731

QUESTION 1:

Bloom Filter Consider a Bloom filter with 16 slots that uses 2 hash functions. To define the index position to set in the array, we will use the following procedure: Generate a hash value using SHA256 on your depaulid and a number. For example, to generate hash value of number x, you will need to run: Use the bloomfilter.py file shared in the class: (a) Add the strings '1', '3', '5', . . . , '19' to this Bloom filter and write down which bits have been set. (b) Test the resulting Bloom filter for the values '2', '4', '6', . . . , '20'. Do you get any false positives, and if so, what are they?

QUESTION 1

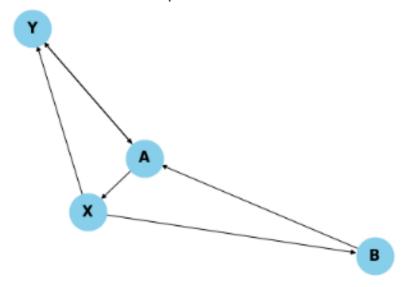
```
In [10]: import hashlib
         class BloomFilter:
             def __init__(self, size, hash_functions):
                 self.size = size # Size of the filter (number of bits)
                 self.hash_functions = hash_functions
                 self.bit_array = [False] * size
             def add(self, element):
                 for i in range(self.hash_functions):
                     index = self._hash(element, i)
                     self.bit_array[index] = True
             def contains(self, element):
                 for i in range(self.hash_functions):
                     index = self._hash(element, i)
                     if not self.bit_array[index]:
                         return False
                 return True
             def _hash(self, element, i):
                  # Generate hash value using SHA256 using DePaul ID and element
                 hash_value = hashlib.sha256(bytes(f"nparamah {element}", encoding='utf-8')).hexdigest()
                     hash_function = int(hash_value[0], 16)
                     hash_function = int(hash_value[1], 16)
                 # Return the hash value modulo the size of the filter
                 return hash_function % self.size
         # Creating a Bloom filter with 16 slots and 2 hash functions
         filter_size = 16
         num_hash_functions = 2
         obj_bloom = BloomFilter(filter_size, num_hash_functions)
         # Add the elements '1', '3', '5', ..., '19' to the Bloom filter
         for i in range(1, 20, 2):
            obi bloom.add(str(i))
             print(f"Bit at index {obj_bloom._hash(str(i), 0)} and {obj_bloom._hash(str(i), 1)} is set for {i}")
         # Test the presence of elements '2', '4', '6', ..., '20' in the Bloom Filter
         values_to_check = list(range(2, 20, 2))
         for value in values_to_check:
             if obj bloom.contains(str(value)):
                 print(f"{value} may be in the set.")
             else:
                 print(f"{value} is definitely not in the set.")
         Bit at index 4 and 8 is set for 1
         Bit at index 7 and 2 is set for 3
         Bit at index 15 and 1 is set for 5
         Bit at index 4 and 8 is set for 7
         Bit at index 10 and 1 is set for 9
         Bit at index 4 and 1 is set for 11
         Bit at index 13 and 5 is set for 13
         Bit at index 5 and 6 is set for 15
         Bit at index 15 and 0 is set for 17
         Bit at index 1 and 0 is set for 19
         2 is definitely not in the set.
         4 is definitely not in the set.
         6 may be in the set.
         8 is definitely not in the set.
         10 may be in the set.
         12 is definitely not in the set.
         14 is definitely not in the set.
         16 is definitely not in the set.
         18 is definitely not in the set.
```

QUESTION 2:

```
Link Matrix:
[[0. 1. 0. 1.]
 [0. 0. 0.5 0. ]
 [0.5 0. 0. 0. ]
 [0.5 0. 0.5 0. ]]
Pages: ['A', 'B', 'X', 'Y']
In [15]: import numpy as np
          import networkx as nx
          import matplotlib.pyplot as plt
          def calculate_pagerank(connectivity_matrix, damping_factor=0.85, tolerance=1e-6):
             num_pages = connectivity_matrix.shape[1]
             pagerank_vector = np.ones((num_pages, 1)) / num_pages
             previous_pagerank_vector = np.ones((num_pages, 1)) * 100 # Initialize with a Large difference
             pagerank_iterations = [] # Store PageRank vectors at each iteration
             while np.linalg.norm(pagerank_vector - previous_pagerank_vector, 2) > tolerance:
                 previous_pagerank_vector = pagerank_vector.copy()
                 pagerank_vector = damping_factor * np.dot(connectivity_matrix, pagerank_vector) + (1 - damping_factor) / num_pages
                 pagerank vector += ((1 - np.sum(pagerank vector)) / num pages) # Adding missing probability mass to handle dead-end nod
                 pagerank_vector = pagerank_vector / np.sum(pagerank_vector) # Normalize the PageRank vector
pagerank_iterations.append(pagerank_vector.flatten())
             return pagerank_iterations
          # input matrix representing the connectivity of web pages
         webpage_connectivity = np.array([[0, 1, 0, 1],
                                          [0, 0, 0.5, 0],
                                           [0.5, 0, 0, 0],
                                           [0.5, 0, 0.5, 0]])
         # Running the PageRank algorithm until convergence on the input matrix
         page_rank_iterations = calculate_pagerank(webpage_connectivity)
          # Create a directed graph using NetworkX
         graph = nx.DiGraph()
          # Add edges from the matrix
         edges = [("A", "Y"), ("A", "X"), ("B", "A"), ("X", "B"), ("X", "Y"), ("Y", "A")]
          graph.add_edges_from(edges)
          # Draw the graph
         positions = nx.spring_layout(graph)
          nx.draw(graph, positions, with_labels=True, node_size=1500, node_color="skyblue", font_size=15, font_weight="bold", arrows=True)
         plt.title("Graph Visualization")
         plt.show()
          # Print all iterations until convergence
         for i, page_rank in enumerate(page_rank_iterations):
             print("Iteration", i+1, "Page ranks:", page_rank)
         # Print the final iteration in the respective page rank order
         final_page_ranks = page_rank_iterations[-1]
          page_ranks_with_labels = [(page, rank) for page, rank in zip(['A', 'B', 'X', 'Y'], final_page_ranks)]
         page_ranks_with_labels.sort(key=lambda x: x[1], reverse=True)
          print("Final Page Ranks:")
          for page, rank in page_ranks_with_labels:
             print(f"{page}: {rank}")
```

. . . .

Graph Visualization



```
Iteration 1 Page ranks: [0.4625 0.14375 0.14375 0.25 ]
Iteration 2 Page ranks: [0.3721875 0.09859375 0.2340625 0.29515625]
Iteration 3 Page ranks: [0.3721875 0.13697656 0.19567969 0.29515625]
Iteration 4 Page ranks: [0.40481289 0.12066387 0.19567969 0.27884355]
Iteration 5 Page ranks: [0.37708131 0.12066387 0.20954548 0.29270935]
Iteration 6 Page ranks: [0.38886723 0.12655683 0.19775956 0.28681638]
Iteration 7 Page ranks: [0.38886723 0.12154781 0.20276857 0.28681638]
Iteration 8 Page ranks: [0.38460957 0.12367664 0.20276857 0.28894522]
Iteration 9 Page ranks: [0.38822858 0.12367664 0.20095907 0.28713571]
Iteration 10 Page ranks: [0.3866905 0.1229076 0.20249715 0.28790475]
Iteration 11 Page ranks: [0.3866905 0.12356129 0.20184346 0.28790475]
Iteration 12 Page ranks: [0.38724613 0.12328347 0.20184346 0.28762693]
Iteration 13 Page ranks: [0.38677384 0.12328347 0.20207961 0.28786308]
Iteration 14 Page ranks: [0.38697457 0.12338383 0.20187888 0.28776272]
Iteration 15 Page ranks: [0.38697457 0.12329853 0.20196419 0.28776272]
Iteration 16 Page ranks: [0.38690206 0.12333478 0.20196419 0.28779897]
Iteration 17 Page ranks: [0.38696369 0.12333478 0.20193337 0.28776815]
Iteration 18 Page ranks: [0.3869375 0.12332168 0.20195957 0.28778125]
Iteration 19 Page ranks: [0.3869375 0.12333282 0.20194844 0.28778125]
Iteration 20 Page ranks: [0.38694696 0.12332809 0.20194844 0.28777652]
Iteration 21 Page ranks: [0.38693892 0.12332809 0.20195246 0.28778054]
Iteration 22 Page ranks: [0.38694233 0.12332979 0.20194904 0.28777883]
Iteration 23 Page ranks: [0.38694233 0.12332834 0.20195049 0.28777883]
Iteration 24 Page ranks: [0.3869411 0.12332896 0.20195049 0.28777945]
Iteration 25 Page ranks: [0.38694215 0.12332896 0.20194997 0.28777893]
Iteration 26 Page ranks: [0.3869417 0.12332874 0.20195041 0.28777915]
Final Page Ranks:
```

A: 0.3869417021334981 Y: 0.28777914893325096 X: 0.20195041300356312 B: 0.12332873592968788

QUESTION 3

Link Matrix:

```
0.
                                     0.5
                                                      0.33333333 0.
                                                                                        ]
[[0.
 [0.
                    0.
                                     0.5
                                                      0.33333333 0.
                                                                                        1
 [0.
                                     0.
                                                      0.33333333 0.
                                                                                        1
                    0.
 [1.
                    0.
                                     0.
                                                      0.
                                                                        0.
                                                                                        1
                                                      0.
                                                                        0.
 ΓΟ.
                   1.
                                     Ω
                                                                                       11
Pages: ['A', 'O', 'X', 'Y', 'Z']
In [16]: import numpy as np
          import networkx as nx
          import matplotlib.pyplot as plt
          def calculate_pagerank(connectivity_matrix, damping_factor=0.85, tolerance=1e-6):
             num_pages = connectivity_matrix.shape[1]
              pagerank_vector = np.ones((num_pages, 1)) / num_pages
              previous_pagerank_vector = np.ones((num_pages, 1)) * 100 # Initialize with a large difference pagerank_iterations = [] # Store PageRank vectors at each iteration
              while np.linalg.norm(pagerank_vector - previous_pagerank_vector, 2) > tolerance:
                  previous_pagerank_vector = pagerank_vector.copy()
                  pagerank_vector = damping_factor * np.dot(connectivity_matrix, pagerank_vector) + (1 - damping_factor) / num_pages
                  pagerank_vector += ((1 - np.sum(pagerank_vector)) / num_pages) # Adding missing probability mass to handle dead-end node
                  pagerank_vector = pagerank_vector / np.sum(pagerank_vector) # Normalize the PageRank vector
                  pagerank_iterations.append(pagerank_vector.flatten())
              return pagerank_iterations
          # input matrix representing the connectivity of web pages
          webpage_connectivity = np.array([[0.0,0.0,0.5,0.33333333,0.0],
           [0.0,0.0,0.5,0.33333333,0.0],
           [0.0,0.0,0.0,0.33333333,0.0],
           [1.0,0.0,0.0,0.0,0.0],
           [0.0,1.0,0.0,0.0,0.0]])
          # Running the PageRank algorithm until convergence on the input matrix
          page_rank_iterations = calculate_pagerank(webpage_connectivity)
          # Create a directed graph using NetworkX
          graph = nx.DiGraph()
          # Add edges from the matrix
          edges = [
              ('A', 'Y'),
('Y', 'A'),
('Y', 'X'),
              ('Y', 'Q'),
('X', 'A'),
('X', 'Q'),
('Q', 'Z')
          graph.add_edges_from(edges)
          # Draw the graph
          positions = nx.spring layout(graph)
          nx.draw(graph, positions, with_labels=True, node_size=1500, node_color="skyblue", font_size=15, font_weight="bold", arrows=True)
          plt.title("Graph Visualization")
          plt.show()
          # Print all iterations until convergence
          for i, page_rank in enumerate(page_rank_iterations):
              print("Iteration", i+1, "Page ranks:", page_rank)
          # Print the final iteration in the respective page rank order
          final_page_ranks = page_rank_iterations[-1]
          page_ranks_with_labels = [(page, rank) for page, rank in zip(['A','Q','X','Y','Z'], final_page_ranks)]
          page_ranks_with_labels.sort(key=lambda x: x[1], reverse=True)
          print("Final Page Ranks:")
          for page, rank in page_ranks_with_labels:
              print(f"{page}: {rank}")
```

Q X

```
Iteration 1 Page ranks: [0.20566667 0.20566667 0.12066667 0.234
                                                                     0.234
Iteration 2 Page ranks: [0.18736333 0.18736333 0.13608
                                                          0.24459667 0.244596671
Iteration 3 Page ranks: [0.19871782 0.19871782 0.14088382 0.23084027 0.23084027]
Iteration 4 Page ranks: [0.19452321 0.19452321 0.13464759 0.23815299 0.23815299]
Iteration 5 Page ranks: [0.19518792 0.19518792 0.13796269 0.23583074 0.23583074]
Iteration 6 Page ranks: [0.19554408 0.19554408 0.13690993 0.23600095 0.23600095]
Iteration 7 Page ranks: [0.19517382 0.19517382 0.1369871 0.23633263 0.23633263]
Iteration 8 Page ranks: [0,19535698 0,19535698 0,13713746 0,2360743 0,2360743 ]
Iteration 9 Page ranks: [0.19530377 0.19530377 0.13702035 0.23618606 0.23618606]
Iteration 10 Page ranks: [0.19530466 0.19530466 0.13707101 0.23615983 0.23615983]
Iteration 11 Page ranks: [0.1953143 0.1953143 0.13705912 0.23615613 0.23615613]
Iteration 12 Page ranks: [0.19530757 0.19530757 0.13705745 0.2361637 0.2361637 ]
Iteration 13 Page ranks: [0.19531029 0.19531029 0.13706088 0.23615927 0.23615927]
Iteration 14 Page ranks: [0.19530974 0.19530974 0.13705887 0.23616082 0.23616082]
Iteration 15 Page ranks: [0.19530959 0.19530959 0.13705957 0.23616062 0.23616062]
Final Page Ranks:
Y: 0.23616062055337508
Z: 0.23616062055337508
A: 0.1953095925906417
```

Q: 0.1953095925906417 X: 0.13705957371196648

QUESTION 4

Suppose we recursively eliminate dead ends from the graph, solve the remaining graph, and estimate the PageRank for the dead-end pages as described in Section 5.1.4. Suppose the graph is a chain of dead ends, headed by a node with a self-loop, as suggested in Fig. 5.9. What would be the Page Rank assigned to each of the nodes?

The scenario outlined consists of a series of dead-end sites, where the initial node (Node 1) has a self-loop and each page links to the next. This is how each node's PageRank would be calculated:

Node 1: Self-Looping Root Node Node 1 keeps all of its significance and transfers its entire PageRank to itself because it has a self-loop. As a result, Node 1's PageRank stays at 1.

Dead-End Nodes That Follow (Node 2 to Node n): There is only one inbound link from each preceding node (Node 2 to Node n).

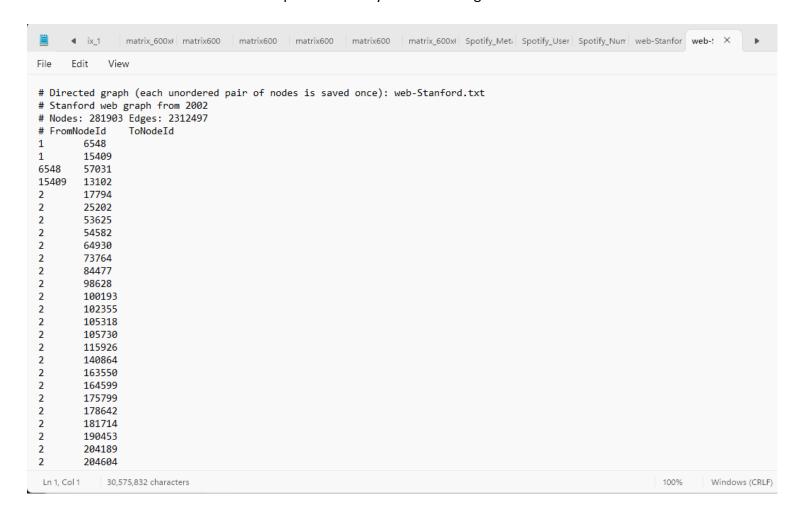
Hence, node 1, the root node with a self-loop, continues to have a PageRank of 1. Because each successive deadend node (Node 2 to Node n) receives half of its PageRank from its predecessors, their PageRank is 1/2. As a result, each node in the chain of dead ends, which is led by a node with a self-loop, would have the following PageRank assigned to it:

Node 1: 1

Node 2 to Node n: 1/2

QUESTION 5:

a. Take a look at the file and report how many nodes and edges the web-Stanford.txt contains.



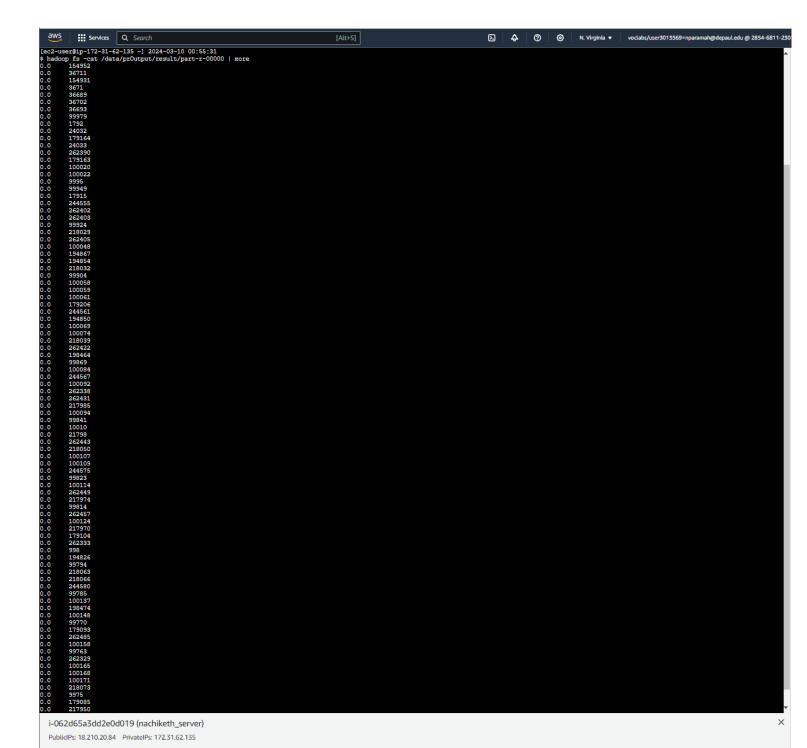
b. Report the runtime (took about 5 minutes to run when I tested it)

SINGLE NODE:

Real 1m47.097S User 1m49.754s

Sys 0m3.330s

```
| March | Color | Colo
                                                       Services Q Search
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          (3)
                                                                                  uce Framework
Map input records=281904
Map output records=281904
Map output records=281904
Map output bytes=4117449
Map output materialized bytes=4681263
Input split bytes=15
Combine input records=0
Reduce input groups=125896
                                                                                     Failed Shuffles=0
Merged Map outputs=1
GC time elapsed (ms)=8
GC time elapsed (ms)=8
GCPU time spent (ms)=0
Fhysical memory (bytes) snapshot=0
Virtual memory (bytes) snapshot=0
Total committed heap usage (bytes)=908066816
                                            Shuffle Errors
BAD_ID=0
                                           File Input Format Counters
Bytes Read=22808184
File Output Format Counters
                                       0m3.330s
ser@ip-172-31-62-135 src] 2024-03-10 00:44:46
                 i-062d65a3dd2e0d019 (nachiketh server)
                 PublicIPs: 18.210.20.84 PrivateIPs: 172.31.62.135
```



MULTI NODE:

Real 4m37.678S User 0m6.563s Sys 0m0.476s

PublicIPs: 54.90.40.172 PrivateIPs: 172.31.57.221

```
aws Services Q Search
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  N. Virginia ▼
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         voclabs/user3013569=nparamah@depaul.edu @ 2854-6811-23
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             0
                                                                                       GC time elapsed (ms)=226

CPU time spent (ms)=16110

Physical memory (bytes) snapshot=717959168

Virtual memory (bytes) snapshot=6141054976

Total committed heap usage (bytes)=603455488
HUFS: Number of write operations there's there's there's Launched map tasks=1
Launched reduce tasks=1
Data-local map tasks=1
Total time spent by all maps in occupied slots (ms)=14448
Total time spent by all reduces in occupied slots (ms)=12680
Total time spent by all map tasks (ms)=3612
Total time spent by all reduce tasks (ms)=3170
Total vcore-milliseconds taken by all map tasks=3612
Total vcore-milliseconds taken by all reduce tasks=12448000
Total megabyte-milliseconds taken by all reduce tasks=12680000
dides framework
Map input records=281904
                                   Map-Reduce Framework
Map input records=281904
Map input records=281904
Map output preserved
Map output Map ou
                                                                                        IO_ERROR=0
WRONG_LENGTH=0
                                           File Input Format Counters
Bytes Read=22629726
File Output Format Counters
                                                                                        Bytes Written=7333875
             CIVID
                                           4m37.678s

0m6.563s

0m0.476s

4min-172-31-57-221 sxc]$ [
                 i-06fafa7fc816ec90a (Master_1)
```

c. Submit a screenshot of the first page of nodes, e.g., by running:

