

ECON GA 2101: Econometrics II

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An econometric model is a probability distribution over observables indexed by parameters. The model imposes restrictions on the distribution of observables. This half of the course introduces methods which use these restrictions to estimate model parameters and perform statistical inference. The first part introduces extremum estimation as a general framework, and discusses M-estimation (which includes Maximum Likelihood estimation, quantile regression and nonlinear regression as special cases), generalized method of moments (GMM), simulated method of moments (SMM), and minimum distance (MD) procedures in some detail. The second part deals with inference and implementation issues, including using the bootstrap and quasi-Bayesian methods.

Contents

1	Introduction	4
1.1	Structural estimation	4
1.2	Motivating examples	4
1.3	General approach to structural estimation	8
1.4	Preliminaries	8
1.5	Identification	11
2	Extremum estimation	12
2.1	Introduction	12
2.2	Consistency	19
2.3	Asymptotic normality	30
3	M-estimation	32
3.1	Additional details for asymptotic normality	32
3.2	Estimating standard errors	35
3.3	Maximum likelihood in more detail	37
4	GMM	43
4.1	Additional details for asymptotic normality	43
4.2	Estimating standard errors	46
4.3	One-step correction	48
4.4	Testing over-identifying restrictions	49
4.5	Continuously-updated GMM	50
5	Simulated Method of Moments	52
5.1	Relation with calibration	52
5.2	Additional details for asymptotic normality	53
5.3	Estimating standard errors	56
5.4	Boosting precision without increasing the number of draws	57
6	Minimum distance	59
6.1	Additional details for asymptotic normality	59
6.2	Estimating standard errors	60
7	Hypothesis testing	61
7.1	Introduction	61
7.2	Wald, LM, and QLR tests	62

7.3	Asymptotic theory	65
8	Quasi-Bayesian estimation	68
8.1	Bayesian estimation	68
8.2	Quasi-Bayesian estimation	69
8.3	Inference under partial identification	71
8.4	Penalization via priors	72
8.5	Being more Bayesian: Bayesian bootstrap	74
9	Bootstrap	77
9.1	Introduction	77
9.2	Types of bootstrap	79
9.3	Consistency of the bootstrap	81
9.4	Bootstrap confidence intervals	85
9.5	Bootstrapping test statistics	89
9.6	Where do refinements come from?	91
10	Sieve estimation	92
10.1	Introduction	92
10.2	Bias-variance tradeoff	97
10.3	Identification	97
10.4	Consistency	97
10.5	Inference	99
11	Nonparametric Bayes procedures	101
11.1	Introduction	101
11.2	Negative results	101
11.3	Somewhat positive results	103
11.4	Positive results	104
A	Supplemental results	107
A.1	Useful results	107
A.2	Asymptotic normality of extremum estimators with non-differentiable objective function	107
	Bibliography	112