

(8) Recordar los vectores  $e_1$ ,  $e_2$  y  $e_3$  dados en la página 12 del apunte. Sea  $v = (x_1, x_2, x_3) \in \mathbb{R}^3$ . Verificar que

$$v = x_1 e_1 + x_2 e_2 + x_3 e_3 = \langle v, e_1 \rangle e_1 + \langle v, e_2 \rangle e_2 + \langle v, e_3 \rangle e_3.$$

$$\begin{aligned} \kappa_1 e_1 + \kappa_2 e_2 + \kappa_3 e_3 &= \langle v, e_1 \rangle e_1 + \langle v, e_2 \rangle e_2 + \langle v, e_3 \rangle e_3 \\ \kappa_1 (1, 0, 0) + \kappa_2 (0, 1, 0) + \kappa_3 (0, 0, 1) &= \langle (\kappa_1, \kappa_2, \kappa_3)(1, 0, 0) \rangle (1, 0, 0) + \langle (\kappa_1, \kappa_2, \kappa_3)(0, 1, 0) \rangle (0, 1, 0) + \langle (\kappa_1, \kappa_2, \kappa_3)(0, 0, 1) \rangle (0, 0, 1) \\ (\kappa_1, 0, 0) + (0, \kappa_2, 0) + (0, 0, \kappa_3) &= \kappa_1 (1, 0, 0) + \kappa_2 (0, 1, 0) + \kappa_3 (0, 0, 1) \\ (\kappa_1, \kappa_2, \kappa_3) &= (\kappa_1, \kappa_2, \kappa_3) \end{aligned}$$