

- (6) Calcular el coseno de los ángulos interiores del triángulo cuyos vértices son: $(3, 1, 1)$, $(-1, 2, 1)$ y $(2, -2, 5)$.

Sea $A = (3, 1, 1)$, $B = (-1, 2, 1)$ y $C = (2, -2, 5)$, estoy buscando $\langle \vec{AB}, \vec{AC} \rangle = |\vec{AB}| |\vec{AC}| \cos \theta$

$$\vec{AB} = B - A = (-1, 2, 1) - (3, 1, 1) = (-4, 1, 0), \quad \vec{AC} = C - A = (2, -2, 5) - (3, 1, 1) = (-1, -3, 4)$$

$$\langle \vec{AB}, \vec{AC} \rangle = \langle (-4, 1, 0), (-1, -3, 4) \rangle = (-4)(-1) + 1(-3) + 0 \cdot 4 = 4 - 3 = 1$$

$$|\vec{AB}| = |(-4, 1, 0)| = \sqrt{(-4)^2 + 1^2} = \sqrt{17}$$

$$|\vec{AC}| = |(-1, -3, 4)| = \sqrt{(-1)^2 + (-3)^2 + 4^2} = \sqrt{26}$$

$$\text{Entonces } 1 = \sqrt{17} \sqrt{26} \cos \theta \Rightarrow \cos \theta = \frac{1}{\sqrt{17} \sqrt{26}}$$