

Ejercicio 1:

Simplificar las siguientes funciones booleanas a un número mínimo de literales.

Postulados y teoremas del álgebra booleana

Postulado 2	a)	$x + 0 = x$	b)	$x \cdot 1 = x$
Postulado 5	a)	$x + x' = 1$	b)	$x \cdot x' = 0$
Teorema 1	a)	$x + x = x$	b)	$x \cdot x = x$
Teorema 2	a)	$x + 1 = 1$	b)	$x \cdot 0 = 0$
Teorema 3, involución		$(x')' = x$		
Postulado 3, conmutatividad	a)	$x + y = y + x$	b)	$xy = yx$
Teorema 4, asociatividad	a)	$x + (y + z) = (x + y) + z$	b)	$x(yz) = (xy)z$
Postulado 4, distributividad	a)	$x(y + z) = xy + xz$	b)	$x + yz = (x + y)(x + z)$
Teorema 5, DeMorgan	a)	$(x + y)' = x'y'$	b)	$(xy)' = x' + y'$
Teorema 6, absorción	a)	$x + xy = x$	b)	$x(x + y) = x$

$$a) \quad x\gamma + x\bar{\gamma} \stackrel{P4}{=} x(\gamma + \bar{\gamma}) \stackrel{P5}{=} x \cdot 1 \stackrel{P2}{=} x$$

$$b) \quad (x + \gamma)(x + \bar{\gamma}) \stackrel{P4}{=} x + \gamma\bar{\gamma} \stackrel{P5}{=} x + 0 \stackrel{P2}{=} x$$

$$c) \quad x\gamma z + \bar{x}\gamma + x\gamma\bar{z} \stackrel{P4}{=} x\gamma(z + \bar{z}) + \bar{x}\gamma \stackrel{P5}{=} x\gamma \cdot 1 + \bar{x}\gamma \stackrel{P2}{=} x\gamma + \bar{x}\gamma \stackrel{P4}{=} \gamma(x + \bar{x}) \stackrel{P5}{=} \gamma \cdot 1 \stackrel{P2}{=} \gamma$$

$$d) \quad z\bar{x} + z\bar{x}\gamma = z(\bar{x} + \bar{x}\gamma) \stackrel{P4}{=} z((\bar{x} + \bar{x})(\bar{x} + \gamma)) \stackrel{P5}{=} z(1 + (\bar{x} + \gamma)) \stackrel{P2}{=} z(1 + \bar{x} + \gamma) = z(\bar{x} + \gamma)$$

$$e) \quad \overline{(A+B)} \cdot \overline{(\bar{A} + \bar{B})} \stackrel{T5}{=} \bar{A}\bar{B} \cdot \overline{(\bar{A} + \bar{B})} \stackrel{T5}{=} \bar{A}\bar{B} \cdot \bar{\bar{A}}\bar{\bar{B}} \stackrel{T3}{=} \bar{A}\bar{B}AB \stackrel{T4}{=} (\bar{A}A)(\bar{B}B) \stackrel{P5}{=} 0 \cdot 0 \stackrel{T2}{=} 0$$

$$f) \quad \gamma(\omega\bar{z} + \omega z) + x\gamma \stackrel{P4}{=} \gamma(\omega(\bar{z} + z)) + x\gamma \stackrel{P5}{=} \gamma(\omega \cdot 1) + x\gamma \stackrel{P2}{=} \gamma\omega + x\gamma \stackrel{P4}{=} \gamma(\omega + x)$$