Motional Ground State Cooling Outside the Lamb-Dicke Regime

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We report Raman sideband cooling of a single sodium atom to its three-dimensional motional ground state in an optical tweezer. Despite having a very large Lamb-Dicke parameter, high initial temperature, and large differential AC Stark shifts between the excited state and the ground state, we achieve a ground state preparation fidelity of 77(4)% after 100 ms of cooling. Our technique includes addressing very high-order sidebands and fast modulation of the optical tweezer trap. We demonstrate that Raman sideband cooling to the 3D motional ground state is applicable outside the Lamb-Dicke regime, for example in systems where tight confinement and low initial temperature are difficult to realize. This is particularly relevant for systems which are challenging to laser-cool, such as molecules and exotic atoms, and opens up the possibility to gain quantum motional control of these systems.

Systems of trapped neutral atoms assembled from the bottom-up in optical tweezer arrays are an exciting platform to study quantum information and quantum simulations [2–8]. The inherent single-particle detection and control combined with tunable interactions are key to implementing neutral atom based quantum logic gates [4, 5], novel quantum phases [7], and single-photon switches [9, 10]. Advances in real-time re-arrangement of optical tweezers enable rapid preparation of atoms in large and complex geometries with high fidelity [11, 12]. Adding quantum motional control of individual atoms [13–17] enables efficient coupling of single atoms to photonic crystal cavities [18], high-fidelity single qubit gates [19], and studies of the atomic Hong-Ou-Mandel effect [20].

Extending optical tweezer array techniques to include polar molecules will open up a large range of new applications that exploit their many long-lived internal states and highly tunable interactions [21–24]. Molecules could be assembled from atom pairs in the optical tweezer [16], or directly loaded from magneto-optical traps (MOTs) [25–27]. For either approach, preparing the constituent atoms or molecules in the lowest motional quantum state is important for realizing long coherence times in quantum applications.

Preparation of single atoms in the motional ground state has been achieved in optical tweezers [14–17] using Raman sideband cooling (RSC) [28–30]. However, RSC in these systems has been applied in the Lamb-Dicke (LD) regime, where the size of the atomic wavefunction is much smaller than the wavelength of light used to address them. Extending ground state cooling to systems outside the LD regime, such as light atoms or polar molecules, is challenging. In this letter we demonstrate cooling of single sodium atoms in optical tweezers, initially outside of the LD regime, to the motional ground state. We achieve a ground state probability of $P_0 = 77(4)\%$ by utilizing

cooling of very high-order sidebands in a carefully optimized cooling sequence. Our approach is general and opens up ground state cooling for other systems.

Our experiment begins by loading a single sodium atom into an optical tweezer from a MOT for 250 ms [1], and has an overall repetition rate of 2.5 Hz. The tweezer is created by focusing a 700 nm laser beam through an NA=0.55 objective to create a focused beam with waist 0.7μm. With 45 mW of tweezer power, the trapping frequencies along the three axes are $\{\omega_x, \omega_y, \omega_z\}/2\pi = \{430(4), 590(5), 69(1)\}$ kHz where axis z is along the weakly confined axial direction and axis x and y are along the tightly confined radial directions. After attempting to load an atom from the MOT, an image is taken with 1.5 ms exposure time to determine if it was a success. At the same time, the atom is cooled via polarization gradient cooling (PGC), which reduces the temperature of the single atom to 70 μK, corresponding to an initial mean motional state along the three different axes of $\{\bar{n}_x, \bar{n}_y, \bar{n}_z\} = \{3.4(2), 2.5(2), 21(2)\}$, and therefore initial 3D ground state probability of $P_0 = 0.3\%$. A beam with σ^--polarization is used to initialize the atom into the $|F = 2, m_F = -2\rangle$ stretched state via optical pumping. The hyperfine state detection is performed by pushing out atoms in the stretched state with a strong beam on resonance with the $|F = 2, m_F = -2\rangle$ to $|F' = 3, m_{F'} = -3\rangle$ transition before taking the second image to determine if the atom was pushed out. The state preparation and detection have a combined fidelity of larger than 99%.

To further reduce the temperature of the single atom and to achieve high ground state preparation fidelity, we apply Raman sideband cooling (RSC). The relevant energy levels, cooling sequence, and Raman beam geometries for our system are shown in Figure 1. Briefly, the RSC consists of two steps: driving a coherent Raman transition while removing motional quanta, followed
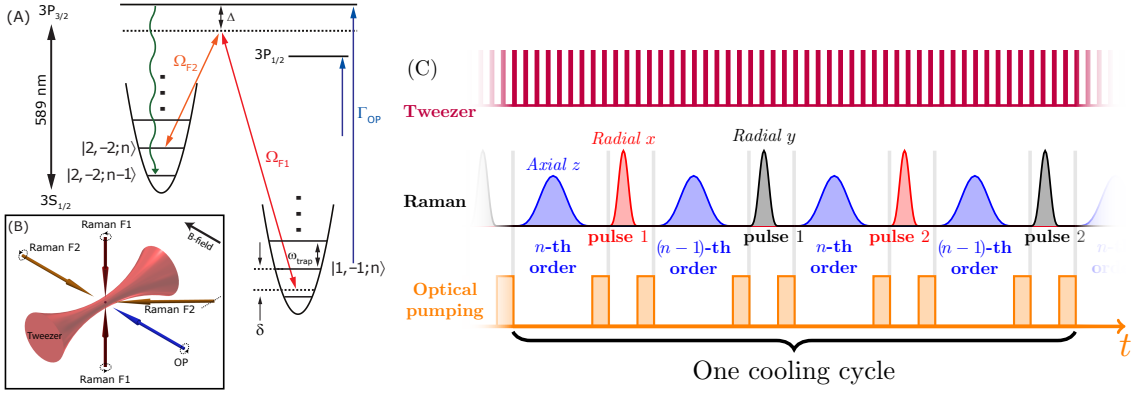
FIG. 1. (A) Energy levels and schematic of Raman sideband cooling. The Raman transitions have a one photon detuning $\Delta = 25$ GHz from the D2 line. We use D1 light with σ^- polarization to repump atoms out of $|F = 2, m_F = -1\rangle$ state to minimize heating on the atom in the $|F = 2, m_F = -2\rangle$ state (B) Geometry and polarizations of the Raman and optical pumping beams relative to the optical tweezer and bias magnetic field. (C) Schematic of the cooling sequence. The tweezer is strobed at 3 MHz to reduce light shifts during optical pumping [1]. Each cooling cycle consists of 8 pulses. The four axial pulses are addressing two neighboring cooling orders. The two pulses in each radial direction are either addressing two neighboring cooling orders or having different length on the first order when most of the population are below $n = 3$ towards the end of the cooling sequence. All of the Raman pulses use Blackman pulse envelopes to reduce the off-resonant coupling to carrier and heating sidebands.

by resetting the atom's internal state via optical pumping (OP). RSC is applied repeatedly until the motional ground state is populated with high probability.

Specifically, Raman transitions are driven in Na between the hyperfine states $|F = 2, m_F = -2\rangle$ and $|F = 1, m_F = -1\rangle$ in the presence of a 8.8 G magnetic field to suppress vector light shifts [14, 15]. Subsequently, an OP/repump pulse brings the atom back to $|F = 2, m_F = -2\rangle$ via spontaneous emission.

It is important that the re-pumping step scatter as few photons as possible to minimize heating. Therefore, we use a σ^--polarized laser resonant with the D1 line since $|F = 2, m_F = -2\rangle$ is a dark state in this case [31][**cite ion**]. Compared to using a D2 repump beam, from which the $|F = 2, m_F = -2\rangle$ state could always scatter a photon via the excited $|F = 3, m_F = -3\rangle$ state, we find a reduction in the scattering rate of a factor of 130(20).

For an atom in motional level n, the OP could result in motional-state redistribution as shown in Fig. 2A. The state redistribution probability is approximately proportional to the effective LD parameter $\eta_{\text{eff}}^{\text{OP}} = \sqrt{2n + 1}\eta^{\text{OP}}$, where $\eta^{\text{OP}} = kz_0 = k\sqrt{\hbar/2m\omega}$, k is the wavenumber of the optical pumping beam, z_0 is the zero-point wavefunction spread, m is the mass of the atom, and $\hbar$ is the reduced Planck constant. Such heating presents a major challenge for efficient cooling of single Na atoms which feature a light mass and short D-line wavelengths. For our trap frequencies and beam geometry, $\{\eta_x^{\text{OP}}, \eta_y^{\text{OP}}, \eta_z^{\text{OP}}\} = \{0.241(2), 0.206(1), 0.602(5)\}$. Combined with a relatively large PGC temperature gives initial $\{\eta_{x,\text{eff}}^{\text{OP}}, \eta_{y,\text{eff}}^{\text{OP}}, \eta_{z,\text{eff}}^{\text{OP}}\} = \{0.67(2), 0.50(1), 4.0(1)\}$. For the weak axial direction, $(\eta_{z,\text{eff}}^{\text{OP}})^2 > 1$ is far outside of the LD regime. As a result, the average change of motional state per OP step is large, which creates a large uncertainty on the motional state at the end of a full RSC step, possibly leading to runaway heating. For example, the average change in motional states over the initial distribution is 2.4 in the axial direction, which is significantly
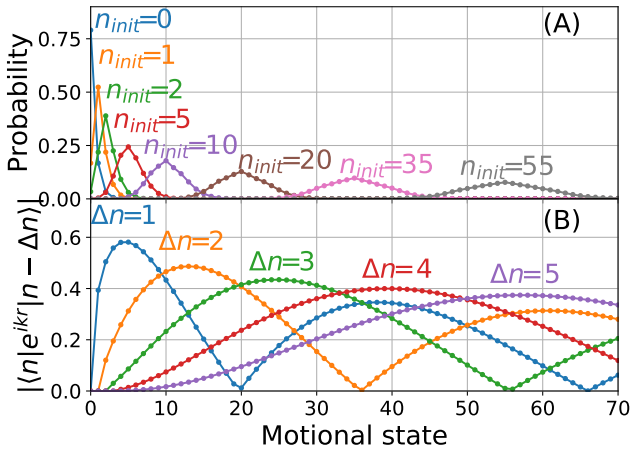

FIG. 2. Optical pumping state changing probability and Raman matrix element for axial direction. The range plotted covers 95% of the initial thermal distribution. (A) Axial motional state distribution after one optical pumping cycle for different initial n. Due to the large Lamb-Dicke parameter, there is a high probability of n changing. (B) Matrix elements for Raman transition in the axial direction showing deviation from $\sqrt{n}$ scaling and multiple minima for different sideband orders. (k is the difference in wave vector of the Raman beams, r is the coordinate in axial direction).
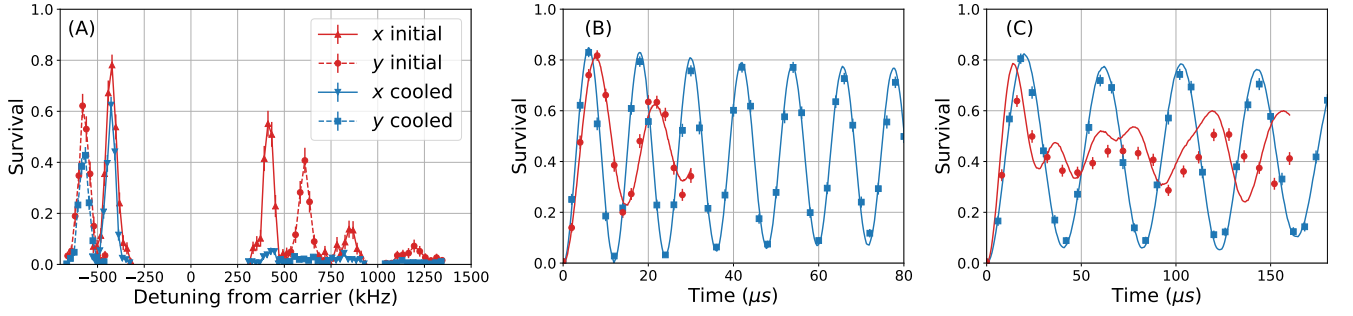
FIG. 3. (A) Radial Raman sideband spectrum of first order heating, first order cooling and second order cooling before and after Raman sideband cooling. (B,C) Rabi flopping on axis y (B) carrier and (C) first order heating sideband before (red) and after (blue) cooling. Solid lines in (B) and (C) are theoretical calculation of the Rabi flopping. The blue lines correspond to a ground state probability of 93% after cooling and the red lines correspond to a thermal distribution of 70 μK before cooling.
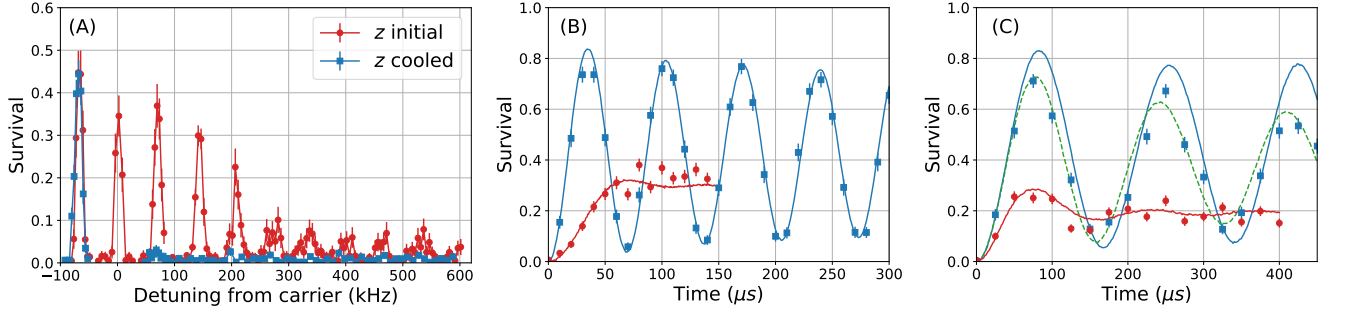

FIG. 4. (A) Axial Raman sideband spectrum from first order heating to eighth order cooling before and after Raman sideband cooling. The data for the second and higher orders of cooling sidebands are taken with 150 μs pulse time and the rest are taken with 125 μs pulse time. (B,C) Rabi flopping on axial (B) carrier and (C) first order heating sideband before (red) and after (blue) cooling. Solid lines in (B) and (C) are theoretical calculation of the Rabi flopping. The blue and green lines corresponds to a ground state probability of 92% after cooling and the red lines corresponds to a thermal distribution of 70 μK before cooling. The blue lines do not take into account the effect of decoherence due to resonance fluctuation. By comparing it to the green line in (C), which includes a 3 kHz fluctuation, we can clearly see that this effect is the strongest for the post-cooling data on the axial heating sideband where the Rabi frequency is the lowest. The asymptotic values for the red lines are low also because of resonance fluctuation.

greater than $0.89 - 0.95$ in previous experiments of RSC of Rb and Cs [13–16].

Fortunately, the large LD parameters also provide opportunities to overcome OP heating. The Raman transitions in our configuration have LD parameters of $\{\eta_x^R, \eta_y^R, \eta_z^R\} = \{0.341(2), 0.291(1), 0.40(1)\}$, which allow strong coupling to higher order sidebands for atoms in higher motional states as calculated in Figure 2B. The LD parameter for Raman transitions is defined as $\eta^R \equiv \Delta k z_0$ similar to OP where Δk being the wave vector difference between the two beams that drives the Raman transition. To offset heating from OP initially, higher-order Raman cooling sidebands can be utilized to remove more motional quanta in a single cooling pulse. Since the coupling strengths of different orders do not reach minima for the same pulse duration, using multiple orders of cooling sidebands avoids accumulations of population near the coupling minima.

Taking the large motional-state changing heating and cooling sources into account, it is not immediately clear that efficient cooling can be achieved. We therefore use a Monte-Carlo simulation to guide our search and to find a robust cooling sequence[32]. In the simulation, we indeed observe a high heating rate due to the large LD parameters and confirm that cooling with higher-order Raman sidebands can suppress heating. In particular, we find that instead of cooling on only one sideband order repeatedly, it is more efficient to alternate the cooling pulses (Fig. 1C) between two neighboring orders for the axial direction and 2nd- and 1st-orders for the radial directions to minimize the accumulation of the atom in motional states that have zero Raman coupling. The simulation also indicates that setting the coupling strength of each cooling sideband to drive a Rabi π pulse corresponding to the maximum matrix element motional state (i.e. the maxima in 2B) can yield efficient cooling. The efficiency of cooling on higher-order sidebands diminishes as the atom approaches the ground state, so the final cooling cycles utilize only the first-order sideband while alternating between the three different axes.

Guided by the simulation results, we construct our axial cooling sequence by starting at the two highest observed cooling sidebands (8th- and 7th-orders) and decreasing the orders to the next pair after every 6 to 15 cycles. This process is repeated until we reach the first order cooling sideband, and most of the population is in the first few excited states. We then switch to cooling only on the first order sideband with two different pulse lengths in order to efficiently cool atoms in the few remaining motional states. The radial cooling is performed similarly to the axial cooling with the initial cooling orders being the 2nd and 1st order and switching to first order only after 20 to 30 pulses. This sequence gives good initial cooling performance, which can then be used to measure experimental parameters, including the Rabi rates of the Raman beams and optical pumping rates, in order to optimize the sequence further.

There are two additional important challenges in cooling single sodium atoms. First, the high initial temperature populates high motional states, meaning that the atoms sample the anharmonicity of the trap away from the center. In order to address this, we drive the sidebands with a large Rabi frequency and short pulses to Fourier broaden the spectrum coverage, and use Blackman pulse envelopes to avoid unwanted coupling to the carrier and heating sidebands [33]. The anharmonicity in the radial directions is calculated to be $1 kHz/n$, meaning that a Rabi frequency of at least 15 kHz is needed to couple to 99% population up to $n = 15$. Second, the tweezer trap causes a large AC Stark shift (as large as 300 MHz) in the excited state. This creates a large, position-dependent OP detuning and mixes the excited-state hyperfine levels, which reduces the optical pumping fidelity. We address this by strobing the trapping light at 3 MHz during the whole cooling sequence, similar to our loading and imaging process [1], while leaving OP on with constant intensity. Due to the large light shift, the OP is effectively off whenever the trap light switches back on. Since the atom can only be addressed by the optical pumping light when the trap light is off, the effect of light shifts on OP fidelity is suppressed.

Our final cooling results are shown in Fig. 3 and 4. In total, 1000 cooling pulses (with a total duration of 100 ms) are applied along three axes with cooling beginning on the radial second order. To characterize the single atom thermal occupation before and after cooling, we perform Raman sideband thermometry. For the more tightly confined (non-degenerate) radial directions, we observe clear first-order heating, first-order cooling, and second-order cooling sidebands before RSC as is shown in red in Figure 3A. After cooling, the first and second order cooling sidebands on both radial axes are suppressed. It is important to note that the simple sideband thermometry formula, which predicts the ratio of the cooling and heating sideband heights to be $\bar{n}/(\bar{n}+1)$ [28], assumes that the coupling strength for different motional states

to be proportional to $\sqrt{n}$. However, outside of the LD regime, the coupling strength rapidly deviates from this simple scaling rule, as shown in figure 2A. Since the Raman spectroscopy is performed with relatively large Raman LD parameters η^R, we cannot use this formula to measure $\bar{n}$. Instead, given the absence of the second order cooling sideband, we assume that the atoms are cold enough to have stronger coupling to the first order cooling sideband than the second order, i.e. below where the matrix element for the two orders cross, in which case the lower bound of the ground state population can be computed from the heights of the sidebands by assuming all of the excitations are in the $n = 1$ state. In doing this, we found a ground state population of $90(2)\%$ and $94(3)\%$ along the two radial directions. We also use an independent measurement of Rabi flopping on the carrier (Fig. 3B) and first-order heating(Fig. 3C) sidebands to verify our assumption about the distribution and the ground state population [34]. The data is fitted using the same Monte-Carlo simulation we used to simulate the cooling which yields $89(2)\%$ and $92(2)\%$ and show good agreement with the population extracted from the sideband thermometry. We also extracted the initial temperature before cooling from the motional-state decohered Rabi flopping to obtain the initial temperature of $70\mu K$.

For the weaker axial direction, cooling is much more challenging due to the large $\eta_{z,\mathrm{eff}}^{\mathrm{OP}} \approx 4.0(2)$. We observe up to 8th-order Raman cooling sidebands initially, which indicates population in highly-excited motional states. Nevertheless, our cooling sequence works efficiently as all the cooling sidebands are suppressed after RSC (Fig. 4). The ground state population calculated using the ratio of first-order sideband heights yields $92(3)\%$. We also perform Rabi flopping on the carrier(Figure 4B) and extracted a ground state population of $91(2)\%$, in agreement with the other method. For the first-order heating sideband Rabi flopping (Figure 4C), we observed additional decoherence that is more pronounced due to the slower Rabi frequency. The decoherence time scale is consistent with magnetic field fluctuations of 1.5 mG that we measure independently in the lab, which produces a Zeeman shift of ~ 3 kHz.

Combining the axial and radial cooling results, we have prepared a single Na atom with 3D ground state probability of $77(4)\%$. We measured a heating rate of the single atoms in the tweezer to be 67nK/ms due to off-resonant scattering of the trapping light, which corresponds to $0.9\%/ms$ decrease in ground state population[35]. The ground state preparation fidelity is currently limited by off-resonant scattering from the Raman beams, which are measured to be between 3 to 15 kHz for the detuning and power we use, and the resonance shift caused by magnetic field fluctuations.

There is an additional 5% loss from finite imaging fidelity and 10% loss from very high-lying initial motional states that are not efficiently cooled by RSC, but instead

off-resonantly heated by the Raman beams. These give us a 66(3)% probability of ground state atom after each successful loading event. We are planning to improve these by increasing the detuning of the Raman beams, addressing a wider range of trap anharmonicity by frequency sweeps, implementing better control of the magnetic field, and optimizing the temperature during imaging. Another improvement could be to implement grey molasses cooling to achieve a lower starting temperature before RSC[36].

[**The distinction between 77 and 66 percent is confusing, we should discuss it**]

We have shown that despite the difficulty in achieving a low optical cooling temperature of light mass sodium atoms, reliable three dimensional cooling with significant ground state population can be achieved by using high-order Raman sidebands in an optimized cooling sequence. These techniques are well-suited for a large variety of systems and open up a route to ground state cooling to other species, including molecules and exotic atoms.

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