

Mathematical Calculations & Formulas

1. Contour Center Calculation (Centroid)

$$cx = M10 / M00, \quad cy = M01 / M00$$

Where M10, M01, M00 are image moments from cv2.moments().

2. Kalman Filter Prediction Step

$$X' = A * X + W$$

Where A is the state transition matrix and W is process noise.

3. Kalman Filter Correction Step

$$X_{\text{new}} = X' + K * (Z - H * X')$$

Where K is the Kalman gain, Z is the measurement, and H is the measurement matrix.

4. Edge Detection using Canny

$$G = \sqrt{Gx^2 + Gy^2}$$

Where Gx and Gy are intensity gradients in x and y directions.

5. Hough Transform for Line Detection

$$\rho = x * \cos(\theta) + y * \sin(\theta)$$

Where rho is the distance from origin and theta is the angle of the line.

6. Optical Flow (Lucas-Kanade Algorithm)

$$\begin{bmatrix} u \\ v \end{bmatrix} = M^{-1} * \begin{bmatrix} -\sum(I_x * I_t) \\ -\sum(I_y * I_t) \end{bmatrix}$$

Where Ix, Iy are intensity gradients, It is the time change in intensity.

7. Contact Detection

$$y + h \geq \text{surface_y}$$

Where y + h is the bottom of the object and surface_y is the detected surface level.

8. Contact Length Calculation

$$\text{Contact Length} = x_{\text{max}} - x_{\text{min}}$$

Where xmax and xmin are the left and right edges of the contact region.

9. Deformation Calculation (Aspect Ratio)

Aspect Ratio = Width / Height = w / h

OR

Deformation = Minor Axis / Major Axis

Where Major Axis is the longest ellipse dimension and Minor Axis is the shortest.