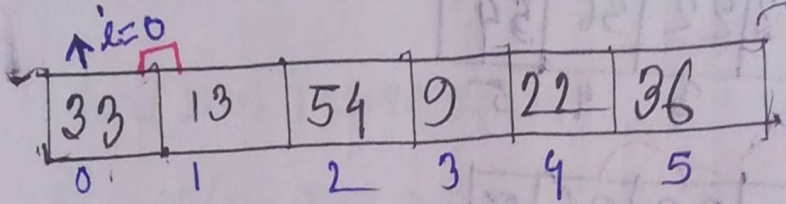
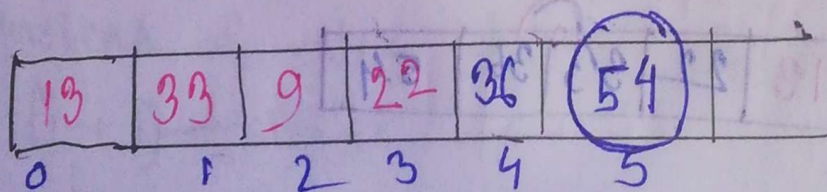
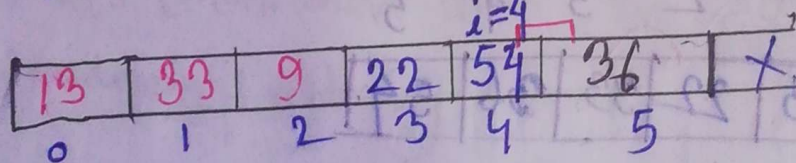
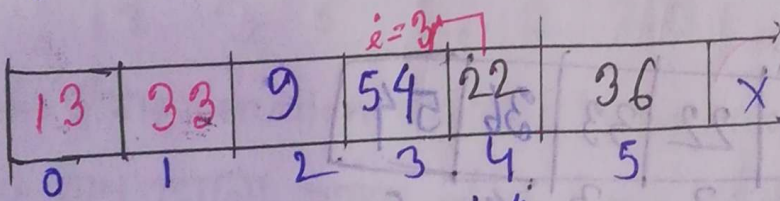
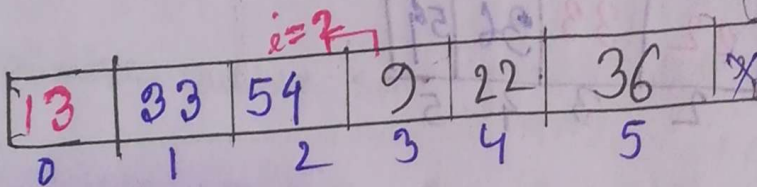
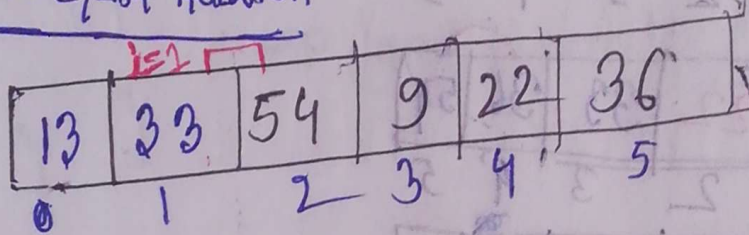


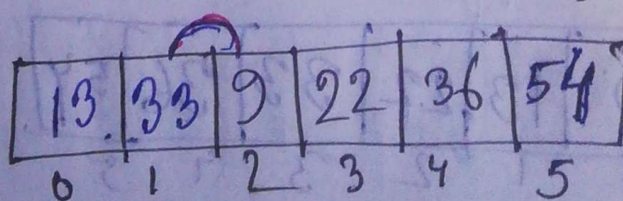
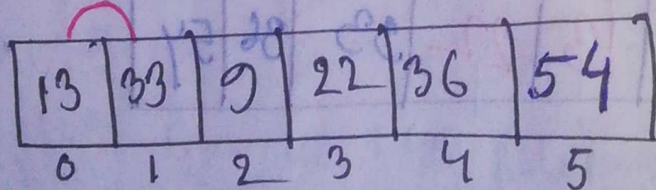
Bubble Sort



1st phase / 1st iteration



2nd phase



$$n=6$$

$$i=0 \rightarrow n-2$$

$$arr[i] \leftrightarrow arr[i+1]$$

1st phase 6 max value fixed

2nd phase

When not to use

1) Dealing with a large set of data

2) When you are looking for a quick algorithm

Bubble sort is slow

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13	9	33	22	36	54
0	1	2	3	4	5

13	9	22	33	36	54
0	1	2	3	4	5

13	9	22	33	36	54
0	1	2	3	4	5

13	9	22	33	36	54
0	1	2	3	4	5

3rd phase

9	13	22	33	36	54
0	1	2	3	4	5

9	13	22	33	36	54
0	1	2	3	4	5

9	13	22	33	36	54
0	1	2	3	4	5

4th phase

9	13	22	33	36	54
0	1	2	3	4	5

5th phase

9	13	22	33	36	54
0	1	2	3	4	5


```

for (i=1; i<size; i++)
{
    for (j=0; j<size-1; j++)
    {
        if (arr[j] > arr[j+1])
        {
            swap(arr[j], arr[j+1]) / temp = arr[j]
                                   arr[j] = arr[j+1]
                                   arr[j+1] = temp
        }
    }
}

```

iteration
Bubble up
Ascending
Descending
if (arr[j] < arr[j+1])

Optimize Bubble sort ! कलमगुमक test मरु (मरु) sort करु नरु।

14 3 5 2 1 20

total 5 बार iteration करु नरु। for example 3rd iteration करु 600 शरु करु। तशु वरु 2 बार 300 करु करु करु नरु। (Redundant testing)

1) Instead of value of $j = \text{size} - 2$ ($j=0; j<\text{size}-1; j++$) use $(j-i-1) \rightarrow \text{size}-i$

1 iteration →

14	3	5	2	1	20
14	3	5	2	1	20
14	3	5	2	1	20
14	3	5	2	1	20
14	3	5	2	1	20

Redundant testing inside iteration
already sorted. don't need to compare again

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$$\frac{2}{\text{for } (i=1; i < n; i++)$$

$$\{ \text{int flag} = 0$$

$$\text{for } (j=0; j < \text{size}-i; j++)$$

$$\{ \text{if } (A[j] > A[j+1])$$

$$\{ \text{swap } (A[j], A[j+1]); \text{flag} = 1$$

$$\}$$

$$\text{if } (\text{flag} == 0)$$

$$\text{break;}$$

$$\}$$

Insertion Sort

sorted	unsorted				
33	13	54	9	22	36
0	1	2	3	4	5

$$C=1$$

$$S=1$$

sorted	unsorted				
13	33	54	9	22	36

$$C=1$$

$$S=0$$

13	33	54	9	22	36
----	----	----	---	----	----

$$C=3$$

$$S=3$$

9	13	33	54	22	36
---	----	----	----	----	----

$$C=3$$

$$S=2$$

9	13	22	33	54	36
---	----	----	----	----	----

9	13	22	33	36	54
---	----	----	----	----	----

$$C=2, S=1$$

13 EOH

33

54

9

for ($i=1; i < n; i++$) $\rightarrow i = 1$ to $n-1$ traversal

{
key = arr[i]

// $j = i-1$ to $j=0$

$j = i-1$

while ($j >= 0$ && $key < arr[j]$)

{
arr[j+1] = arr[j]; $j--$;
}

arr[j+1] = key

$i = 1$ to $n-1$ traversal
33 13 54 9 22 36
0 1 2 3 4 5
key = 13
 $j = i-1 = 0$
key = 13
 $j = 0$
arr[1] = 33
 $j--$
arr[0] = 13

Selection Sort: selection sort is a sorting algorithm that selects the minimum element from the unsorted part of the array and swaps it with the first element of the unsorted part.

33 13 54 9 22 36

$i=0$ 9 13 54 33 22 36
index 0 sorted

$i=1$ 9 13 54 33 22 36
index 0, 1 sorted

$i=2$ 9 13 22 33 54 36
index 0, 1, 2 sorted

$i=3$ 9 13 22 33 54 36
index 0, 1, 2, 3 sorted

9 13 22 33 36 54
 $i=5$

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0 1 2 3 4 5
33 13 54 9 22 36

```
for(i=0; i<n-1; i++)
{
    int min=i
    for(j=i+1; j<n; j++)
    {
        if(A[j] < A[min])
        {
            min=j
        }
    }
    if(min != i)
    {
        swap(A[i], A[min])
    }
}
```

```
i=0, min=0
j=1, 2, 3
A[1] < A[0]
13 < 33, 33 < 54, 54 < 9
min = 1, 3
i=i+1
```

- * Bubble sort \hookrightarrow 2nd for loop use 2nd
- * Insertion sort \hookrightarrow for loop \hookrightarrow 1st while / do while loop use 2nd
- * selection sort \hookrightarrow 2nd for loop use 2nd

Insertion	Bubble
Best case: $O(n)$	Best case: $O(n)$
Worst case: $O(n^2)$	Worst case: $O(n^2)$ \rightarrow Reverse

→ Not comparison sort

Array Consolidation

Counting sort

array 1 2 5 9 2 6 5 4

Step 1: Find maximum num from unsorted array

Step 2: Make new array, size will be $\text{max} + 1$

	0	1	2	3	4	5	6	7	8	9	count [max+1]
count	0	0	0	0	0	0	0	0	0	0	

Step 3: Find frequency of each element. $1=1$

Then press these element into count array. $2=2$
 $3=0$
 $5=2$

0	1	2	3	4	5	6	7	8	9
0	1	2	0	1	2	1	0	0	1

Step 4: Find cumulative sum [Prefix sum] $C[i] = C[i-1] + \text{array}[i]$

0	1	2	3	4	5	6	7	8	9
0	1	3	3	4	6	7	7	7	8

Step 5: Do actual sorting. Make a new final array. size will be same as main array. Scan the main array from back [backtracking]. 4 found.

Go to count array in the 4th index. Decrement the value of 4th index, put the value of main array (4) in the decrement index (3).

Final	1	2	2	4	5	5	6	9
	0	1	2	3	4	5	6	7

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Q. Why backtracking instead of fronttracking?

ans: concept: FIFO

Pseudo code

S-1 for (0 \rightarrow n-1) \rightarrow (main array) \rightarrow $O(n)$
 {
 // find max

S-2
 int count[Max+1]
 for () \rightarrow $O(n)$
 {
 // initialize with 0

S-3
 for (n-1 \rightarrow 0) \rightarrow array \rightarrow $O(n)$
 count[arr[i]]--
 k = count[arr[i]]
 final[k] = arr[i]

S-3:
 for (0 \rightarrow n-1) \rightarrow $O(n)$
 {
 arr[i]

count[arr[i]]++;

S-4 for (1 \rightarrow Max) \rightarrow $O(n)$
 {
 count[i] += count[i-1]

S-5

Time complexity

$O(n)$