

NA-DPVI AISTATS 2025 Rebuttle

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1 NA-DPVI Algorithm

$(\mathbf{x}_i)_{i=1}^N \leftarrow \text{data};$
 $(\epsilon, \delta) \leftarrow \text{DP privacy level};$
 $C \leftarrow \text{clipping threshold};$
 $T \leftarrow \text{training iterations};$
 $\lambda \leftarrow \text{learning rate};$
 $\kappa \leftarrow \text{Poisson sampling rate};$
 $\phi_0 \leftarrow \text{initial values for } \phi;$
 $d \leftarrow \dim(\phi_0)$
 $\sigma_{\text{DP}} \leftarrow \text{PRV-Accountant}(\epsilon, \delta, T, \kappa);$

Algorithm 1 DPVI

1: **for** $t = 1, \dots, T - 1$ **do**
2: $\mathbf{g}_{t+1} \leftarrow \sum_{i \in \mathcal{B}_{t+1}} \text{clip}(\nabla_{\phi} \ell(\phi_t; \mathbf{x}_i), C);$
3: Sample $\boldsymbol{\eta}_{t+1} \sim \mathcal{N}(0, \mathbf{I}_d);$
4: $\tilde{\mathbf{g}}_{t+1} \leftarrow \mathbf{g}_{t+1} + \sigma_{\text{DP}} C \boldsymbol{\eta}_{t+1}$
5: $\phi_{t+1} \leftarrow \phi_t - \lambda \tilde{\mathbf{g}};$
6: **end for**
7: **return** $\mathcal{T} = (\phi_t)_{t=0}^T, \tilde{\mathbf{g}} = (\tilde{\mathbf{g}}_t)_{t=1}^T;$

Algorithm 2 NA-DPVI

1: $M \leftarrow \text{number of samples};$
2: $\boldsymbol{\mu}_{\phi^*} \leftarrow \phi^*$ prior distribution mean;
3: $\Sigma_{\phi^*} \leftarrow \phi^*$ prior distribution covariance matrix;
4: $\boldsymbol{\mu}_{\mathbf{A}} \leftarrow \mathbf{A}$ entries prior distribution mean;
5: $\Sigma_{\mathbf{A}} \leftarrow \mathbf{A}$ entries prior distribution covariance matrix;
6: $\boldsymbol{\mu}_{\Sigma_{\text{sub}}} \leftarrow \Sigma_{\text{sub}}$ entries prior distribution mean;
7: $\Sigma_{\Sigma_{\text{sub}}} \leftarrow \Sigma_{\text{sub}}$ entries prior distribution covariance matrix;
8: $\mathcal{T}, \tilde{\mathbf{g}} \leftarrow \text{DPVI};$
9: **model-definition** $\tilde{\mathbf{g}} \mid \mathcal{T}, \phi^*, \mathbf{A}, \Sigma_{\text{sub}}$
10: $\phi^* \sim \mathcal{N}(\boldsymbol{\mu}_{\phi^*}, \Sigma_{\phi^*});$
11: $\mathbf{A} \sim \mathcal{N}(\boldsymbol{\mu}_{\mathbf{A}}, \Sigma_{\mathbf{A}});$
12: $\Sigma_{\text{sub}} \sim \mathcal{N}(\boldsymbol{\mu}_{\Sigma_{\text{sub}}}, \Sigma_{\Sigma_{\text{sub}}});$
13: $\tilde{\mathbf{g}}_{t+1} \mid \phi_t, \mathbf{A}, \phi^*, \Sigma_{\text{sub}} \sim \mathcal{N}(\kappa \mathbf{A}(\phi_t - \phi^*), \sigma_{\text{DP}}^2 C^2 \mathbf{I}_d + \Sigma_{\text{sub}});$
14: **end model-definition**
15: Sample $(\phi_i^*, \mathbf{A}_i, \Sigma_{\text{sub}, i})_{i=1}^M \sim \phi^*, \mathbf{A}, \Sigma_{\text{sub}} \mid \tilde{\mathbf{g}}, \mathcal{T};$ \triangleright using any approximate inference method.
16: **return** $\tilde{p}(\boldsymbol{\theta} \mid \mathcal{T}) = \frac{1}{M} \sum_{i=1}^M q_{\text{VI}}(\boldsymbol{\theta}; \phi_i^*);$

2 NA-DPVI vs Gibbs-SS-Noisy (Bernstein & Sheldon, 2019)

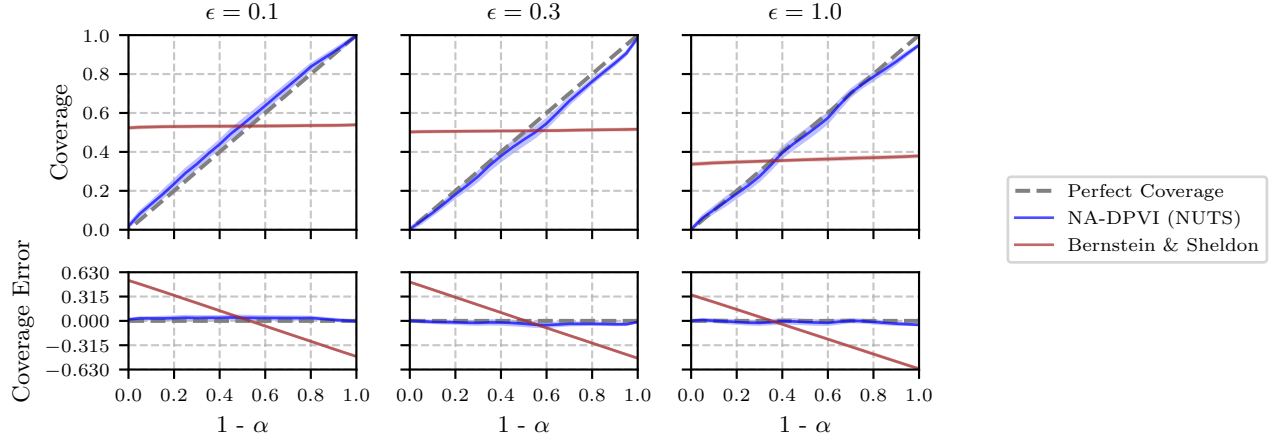


Figure 1: The first row in the figure shows the TARP coverages for the 10d Bayesian linear regression experiment for both NA-DPVI (NUTS) and Bernstein & Sheldon’s method. The second row shows the error for the coverages ($C(\alpha) - (1 - \alpha)$). The solid lines show the average performance over 20 independent TARP repetitions and the error bars show the corresponding std. The parameters for NA-DPVI (NUTS) are $\delta = 10^{-5}$, $N = 5000$, $\kappa = 0.1$ and $T = 10^4$. On the other hand, the parameters for Gibbs-SS-Noisy (Bernstein & Sheldon, 2019) were $n = 10^4$, 2×10^4 burnin iterations and 2×10^4 posterior samples.

Table 1: The RMSE errors corresponding to the linear regression coverages in Figure 1.

Method	$\epsilon = 0.1$	$\epsilon = 0.3$	$\epsilon = 1.0$
NA-DPVI (NUTS)	0.036 ± 0.011	0.035 ± 0.011	0.027 ± 0.009
Bernstein & Sheldon	0.301 ± 0.001	0.299 ± 0.001	0.323 ± 0.003