```
ket0 = \{1, 0\};
       ket1 = \{0, 1\};
       (* Defines H = - \sigma_x and subsequent Z(t) evolution *)
       ham0 = - PauliMatrix[1];
       u0 = MatrixExp[-iham0t];
       udg0 = MatrixExp[i ham0 t];
       zt0 = udg0.PauliMatrix[3].u0;
       (* Defines H = - \sigma_x / 2 and subsequent Z(t) evolution *)
       ham1 = -PauliMatrix[1] / 2;
       u1 = MatrixExp[-iham1t];
       udg1 = MatrixExp[i ham1 t];
       zt1 = udg1.PauliMatrix[3].u1;
In[373]:=
       (* Compute <1| Z(t)|1> in both cases and compare to classical solution*)
       zt0ExpVal = ket1.zt0.ket1;
       zt1ExpVal = ket1.zt1.ket1;
       csol = NDSolveValue[\{x''[t] + Cos[x[t]] = 0, x[0] = \pi, x'[0] = 0\}, x, \{t, 0, 20\}];
       Plot[\{Cos[csol[t]], zt0ExpVal\}, \{t, 0, 20\}, PlotLegends \rightarrow \{"Classical", "<math>\sigma x"}]
       Plot[\{Cos[csol[t]], zt1ExpVal\}, \{t, 0, 20\}, PlotLegends \rightarrow \{"Classical", "\sigma x/2"\}]\}
Out[376]=
       1.0
       0.5

    Classical

                                                          20
                      5
                                                                σx
       -0.5
Out[377]=
       1.0
       0.5

    Classical

                                  10
                                              15
                                                           20
                                                                -\sigma x/2
       -0.5
```

In[182]:=

-1.0

```
In[319]:=
        (* Compute <0 | Z(t) |0> in both cases and compare to classical solution*)
       zt0ExpVal = ket0.zt0.ket0;
       zt1ExpVal = ket0.zt1.ket0;
       csol = NDSolveValue[\{x''[t] + Cos[x[t]] == 0, x[0] == 0, x'[0] == 0\}, x, \{t, 0, 20\}];
       Plot[\{Cos[csol[t]], zt0ExpVal\}, \{t, 0, 20\}, PlotLegends \rightarrow \{"Classical", "\sigmax"\}]
       Plot[\{Cos[csol[t]], zt1ExpVal\}, \{t, 0, 20\}, PlotLegends \rightarrow \{"Classical", "\sigma x/2"\}]
Out[322]=
        1.0
        0.5

    Classical

                                                               20
                                                                   <u></u> σx
       -0.5
       -1.0
Out[323]=
        1.0
        0.5
                                                                      Classical
                                     10
                                                  15
                                                                     -\sigma x/2
       -0.5
```