

## CSE 537 - Artificial Intelligence

### Report: Project 3

**Khan Mostafa    Abhijit Betigeri**  
109365509    109229784

{khan.mostafa, abhijit.betigeri}@stonybrook.edu  
Department of Computer Science  
Stony Brook University

## Word Cross: Finding the missing letter in an incomplete word

### Q1. Returning the most possible missing letter

**Methodology Used:** Using the CPT table given. Visualizing the query set as a Markov Chain of the form  $a \rightarrow B \rightarrow c$ . B being blank position under consideration to be found out. Probability for each assignment to B is computed by considering each of the ascii lowercase characters including (') and then returning most likeliest character with highest conditional probability calculated with a,c & set of ascii characters.

**Probability Evaluation Function:**  $P(b, a) * P(c, b)$

#### Execution Details

##### Command 1:

```
python wordCross.py -q1 --test
```

**Accuracy:** 1.000000

**Time used:** 0.0010000 secs

##### Command 2:

```
python wordCross.py -q1
```

**Accuracy:** 0.311102

**Time used:** 0.196000 secs.

### Q2. Return the most possible missing two consecutive letters

**Methodology Used:** Using the CPT table given. Visualizing the query set as a Markov Chain of the form  $a \rightarrow B \rightarrow C \rightarrow d$ . B & C being blank position under consideration to be found out. Probability for each assignment to B & C is computed by considering each of the ascii lowercase characters including (') and then returning most likeliest characters with highest conditional probability calculated with a,d & set of ascii characters.

**Probability Evaluation Function:**  $P(b, a) * P(c, b) * P(d, c)$

**Execution Details****Command 1:**

```
python wordCross.py -q2 --test
```

**Accuracy:** 1.000000 (two correct letters)

**Accuracy:** 1.000000 (at least one correct letter)

**Time used:** 0.004000 secs.

**Command 2:**

```
python wordCross.py -q2
```

**Accuracy:** 0.089656 (two correct letters)

**Accuracy:** 0.360026 (at least one correct letter)

**Time used:** 6.077000 secs.

**Q3. Return the most possible missing letter**

**Methodology Used:** We Visualize the query as a Markov Chain of  $a \rightarrow ? \rightarrow C \rightarrow ? \rightarrow e$ . C represents the letter we are looking for at (  ). a & e are known/given letters in the query.

Query  $gu\_ \_ \_ n$  can be set up as following chain:  $u \rightarrow ?? \rightarrow C \rightarrow ?? \rightarrow n$ . The level of indirection between  $a='u'$  and C is 2, we represent it by h, similarly t for C and e.

Let's break down the problem this way: The probability of having letter  $C=c$  given  $a=a$  followed by two hidden variables  $a \rightarrow H1 \rightarrow c$  is given by  $\sum (P(H1|a) * P(c|H1))$  for all  $h=H$ . All the one and two level of hidden values are pre-computed this way and is accessible using the defined `getConditionalProbability` function ( This function helps in getting the CPT based on the number of hidden variables.)

Then we compute the probability of each assignments of C from the set of all lowercase characters including ` and returning most likeliest character with highest conditional probability using probability evaluation function as defined below.

**Probability Evaluation Function:**  $P(h, c, a) * P(t, e, c)$

**Execution Details****Command 1:**

```
python wordCross.py -q3 --test
```

**Accuracy:** 1.000000

**Time used:** 0.025000 secs

**Command 2:**

```
python wordCross.py -q3
```

**Accuracy:** 0.149693

**Time used:** 0.278000 secs

#### Q4. Return the most possible missing letter – Given Graphical Model

**Methodology Used:** We visualize the queries as finding the likely letter in the blank space of intersection of four words, having the knowledge of neighboring letters. Representation of the form:

```
a1->? ->C->? ->e1
a2->? ->C->? ->e2
a3->? ->C->? ->e3
a4->? ->C->? ->e4
```

where C represents letter in the blank intersection and a1, e1, a2, e2, a3, e3, a4, e4 are known letters of four words.

Similar to Q3, the probability of having the letter  $C=c$ , given  $a=a$  followed by two hidden letters  $a \rightarrow H1 \rightarrow c$  is given by  $\text{Sum} (P (H1 | a) * P (c | H1))$ , for all  $h=H$ . All the one and two level of hidden values are pre-computed this way and is accessible using the defined `getConditionalProbability` function ( This function helps in getting the CPT based on the number of hidden variables.).

Here we take the intersection of four letters, the probability of  $C=c$  is product of  $P (c | a_i) * P (e_i | c)$ , for  $i = [1, 4]$ , P is the probability of the hidden intermediate variables.

Then we compute the probability of each assignments of C from the set of all lowercase characters including ` and returning most likeliest character with highest conditional probability using probability evaluation function as defined below.

**Probability Evaluation Function:**  $P (h1, c, a1) * P (t1, e1, c) * P (h2, c, a2) * P (t2, e2, c) * P (h3, c, a3) * P (t3, e3, c) * P (h4, c, a4) * P (t4, e4, c)$

##### Execution Details

###### Command 1:

```
python wordCross.py -q4 --test
```

**Accuracy: 1.000000**

**Time used: 0.025000 secs**

###### Command 2:

```
python wordCross.py -q4
```

**Accuracy: 0.426571**

**Time used: 1.006000 secs**

#### Q5. Based on Second Order Markov Chain- Return the most possible missing letter

##### Methodology Used:

We visualize the query as 2<sup>nd</sup> Order Markov Chain of the following form:

```
a->b->C->d->e
```

where C represent the letter to be found out. a,b,d,e are known letter of the word.

Eg: ques\_ion => e->s->C->i->o

Probability for each assignment to C is computed by considering each of the ascii lowercase characters including (') and then returning most likeliest character with highest conditional probability calculated with a,b,d,e & set of ascii characters.

**Probability Evaluation Function:  $P(c, a, b) * P(d, b, c) * P(e, c, d)$**

### Execution Details

#### Command 1:

```
python wordCross.py -q5 --test
```

**Accuracy: 1.000000**

**Time used: 0.002000 secs**

#### Command 2:

```
python wordCross.py -q5
```

**Accuracy: 0.465159**

**Time used: 0.351000 secs**

### Appendix:

```
>python wordCross.py -q1 -q2 -q3 -q4 -q5 --test
```

```
Question 1 accuracy: 1.000000
```

```
Q1 time used: 0.001000 secs.
```

```
Question 2 accuracy: 1.000000 (two correct letters)
```

```
Question 2 accuracy: 1.000000 (at least one correct letter)
```

```
Q2 time used: 0.004000 secs.
```

```
Question 3 accuracy: 1.000000
```

```
Q3 time used: 0.025000 secs.
```

```
Question 4 accuracy: 1.000000
```

```
Q4 time used: 0.025000 secs.
```

```
Question 5 accuracy: 1.000000
```

```
Q5 time used: 0.002000 secs.
```

```
>python wordCross.py -q1 -q2 -q3 -q4 -q5
```

```
Question 1 accuracy: 0.311102
```

```
Q1 time used: 0.196000 secs.
```

```
Question 2 accuracy: 0.089656 (two correct letters)
```

```
Question 2 accuracy: 0.360026 (at least one correct letter)
```

```
Q2 time used: 6.077000 secs.
```

```
Question 3 accuracy: 0.149693
```

```
Q3 time used: 0.278000 secs.
```

```
Question 4 accuracy: 0.426571
```

```
Q4 time used: 1.006000 secs.
```

```
Question 5 accuracy: 0.465159
```

```
Q5 time used: 0.351000 secs.
```