



AMERICAN INTERNATIONAL UNIVERSITY-BANGLADESH

Faculty of Science & Technology

Department of Mathematics

MAT1205: Integral Calculus and Ordinary Differential Equations

Assignment 1

1. Evaluate the followings integrals:

(a)  $\int_2^4 \int_0^3 (x + y) dx dy$

(b)  $\int_0^1 \int_x^y xy dy dx$

(c)  $\int_0^1 \int_{y^2}^y (x^2 y + xy^2) dx dy$

(d)  $\int_1^2 \int_1^y \left(\frac{1}{x} + \frac{1}{y}\right) dx dy$

(e)  $\int_0^1 \int_0^{\sqrt{x}} ye^{x^2} dy dx$

(f)  $\int_0^{\sqrt{\frac{\pi}{2}}} \int_0^{x^2} x \cos y dy dx$

(g)  $\int_0^1 \int_0^{x^2} (x^2 + y) dy dx$

(h)  $\int_0^{\pi/2} \int_0^2 r \sqrt{4 - r^2} dr d\theta$

(i)  $\int_0^1 \int_{-x}^x (x^2 - y^2) dy dx$

(j)  $\int_0^{\frac{\pi}{2}} \int_0^{\sin \theta} r \cos \theta dr d\theta$

2. Evaluate the following integrals:

(a)  $\iint_R (xy - y^2) dA$  where R is rectangle whose vertices are  $(-1,0)$ ,  $(0,0)$ ,  $(0,1)$ , and  $(-1,1)$ .

(b)  $\iint_R (2x + y) dA$  over the rectangle  $R = \{(x,y) | 3 \leq x \leq 5, 1 \leq y \leq 2\}$ .

(c)  $\iint_R (x^2 + y^2) dA$  where R is rectangle whose vertices are  $(0,1)$ ,  $(1,1)$ ,  $(1,2)$  and  $(0,2)$ .

(d)  $\iint_R x dA$  over the triangular region R enclosed by the lines  $x + 2y = 2$ ,  $x = 0$  and  $y = 0$ .

3. Sketch the region and **using** double integrals, find the finite area bounded by the following curve (s).

(a)  $y = 2x - x^2$  and x-axis

(b)  $x^2 = 4y$ ,  $8y = x^2 + 16$

(c)  $y = -x, x = 0, y = 2$

4. Evaluate the following integrals:

(a)  $\int_1^2 \int_0^1 \int_{-1}^1 (x^2 + y^2 + z^2) dx dy dz$

(b)  $\int_0^1 \int_0^{y^2} \int_0^{x+y} x dz dx dy$

(c)  $\int_0^1 \int_0^x \int_0^{x-y} x dz dy dx$

(d)  $\int_0^2 \int_{-1}^{y^2} \int_{-1}^z yz dx dz dy$

(e)  $\int_0^{2\pi} \int_0^2 \int_0^{4-r^2} zr dz dr d\theta$

(f)  $\int_0^{2\pi} \int_0^\pi \int_0^a r^3 \sin \theta dr d\theta d\phi$

5. Find the mass and center of mass of the lamina that occupies the region  $D$  and has the given density function  $\rho$ . Where  $D = \{(x, y) | 0 \leq x \leq 1, 0 \leq y \leq 2\}$  and  $\rho(x, y) = y^2$ .
6. Find the mass and center of mass of the lamina that occupies the region  $D$  and has the given density function  $\rho$ . Where  $D = \{(x, y) | 0 \leq x \leq 1, 0 \leq y \leq 1\}$  and  $\rho(x, y) = 2x$ .

#### Instruction of submission:

- Write down the answer on paper.
  - Scan and make one pdf file.
- or
- Take photo and compile all photos in one word file.
  - Give the name of the file (Section, Name, ID).
  - Submit assignment in the assignment section of Microsoft TEAMS and turn on.
  - Submit by 21 August (Friday).