

RBE501 HW2

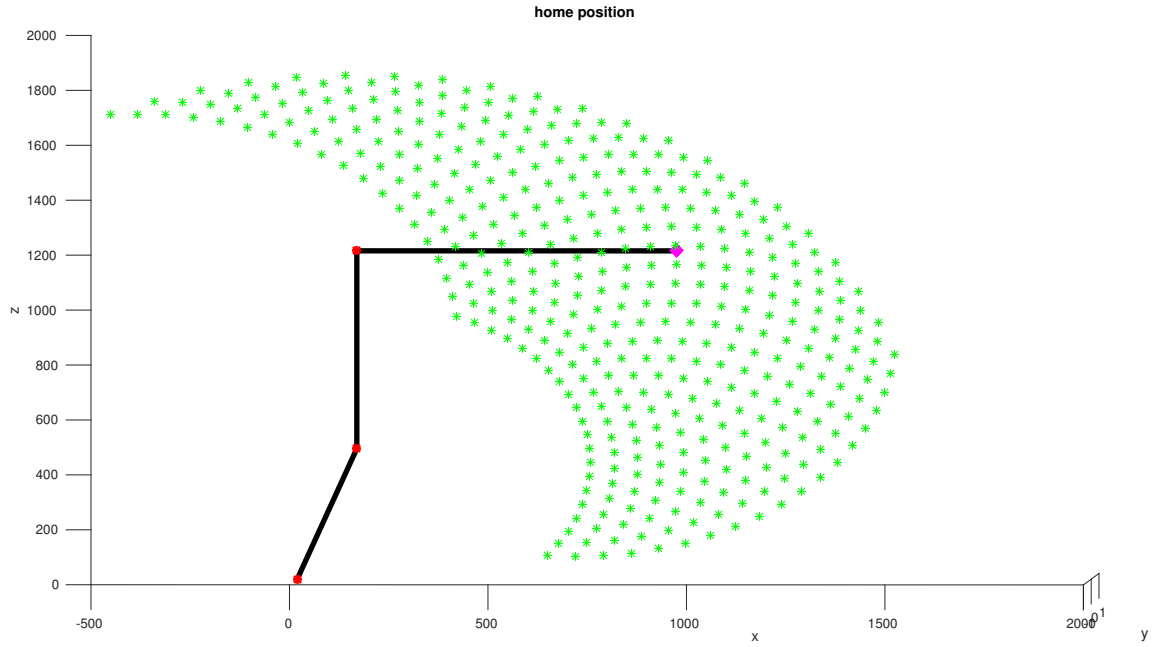
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Part A

$$\begin{aligned}x &= 150 + 720 * \cos(\theta_2) + 805 * \cos(\theta_2 + \theta_3) \\z &= 475 + 720 * \sin(\theta_2) + 805 * \sin(\theta_2 + \theta_3) \\y &= 0; \\ \text{where, } -50 < \theta_2 < 50, -45 < \theta_3 < 45,\end{aligned}\tag{1}$$



Part B

$$\begin{aligned}\theta_1 &= \text{atan2}(Py, Px) \\ \theta_2 &= \text{atan2}(Pz, Px) - \text{atan2}(805 * \sin(\theta_3), (720 + 805 * \cos(\theta_3))) \\ \theta_3 &= \text{acos} \left[\frac{(Px^2 + Pz^2 - (720)^2 - (805)^2)}{(2(720)(805))} \right] \\ \theta_4 &= \theta_5 = \theta_6 = \infty\end{aligned}\tag{2}$$

Part C

$$\begin{aligned}\theta_1 &= 16.8584 \\ \theta_2 &= 23.7742 \\ \theta_3 &= 90.3410 \\ \theta_4 &= \theta_5 = \theta_6 = \infty\end{aligned}\tag{3}$$

Part D

See appendix for the exact form of the T matrixs. Matlab was used to generate them. The jacobian of matrix was then found using the equation in the book.

$$J = \begin{bmatrix} -a_2 S_1 C_2 - a_3 S_1 C_{23} & -a_2 S_2 C_1 - a_3 S_{23} C_1 & -a_3 S_{23} C_1 \\ a_2 C_1 C_2 + a_3 C_1 C_{23} & -a_2 S_2 S_1 - a_3 S_{23} S_1 & -a_3 S_1 C_{23} \\ 0 & a_2 C_2 + a_3 C_{23} & a_3 C_{23} \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}\tag{4}$$

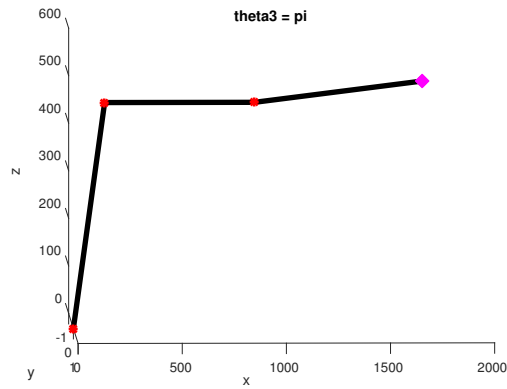
Part E

$$\dot{\vec{\theta}} = J^+ \dot{\vec{x}} = [-0.026, 0.0471, -0.0211]^T\tag{5}$$

Part F

Taking the determinant of Jacobian reveals the singularities of the kinematic chain.

$$\begin{aligned} \det(J) &= a_2 a_3 S_3 (a_2 C_2 + a_3 C_{23}) = 0 \\ &\Rightarrow \sin(\theta_3) = 0 \rightarrow \theta_3 = 0, \pi \\ &\Rightarrow a_2 C_2 + a_3 C_{23} = 0 \end{aligned} \tag{6}$$



Extra Credit

see Appendix $(do_i k.m)$