

---

# Nathaniel Goldfarb

## Table of Contents

.....	1
Problem 1a .....	1
Problem 1a .....	1
Problem 1b .....	2
Problem 1c1 and 1c2 .....	2
Problem 1c3 .....	3
Problem 2 .....	4
Problem 3a .....	4
Problem 3b .....	6
Problem 3c .....	6
Problem 3d .....	7
Problem 4a .....	8
Problem 4b .....	8
Problem 4c .....	9
Problem 4d .....	10

HW2

```
clear all
close all
clc
```

## Problem 1a

$$m_1 = e^{0t}$$

$$m_2 = e^{-3t}$$

## Problem 1a

```
G = tf( [200], [1,3,0])
```

$G =$

$$\frac{200}{s^2 + 3s}$$

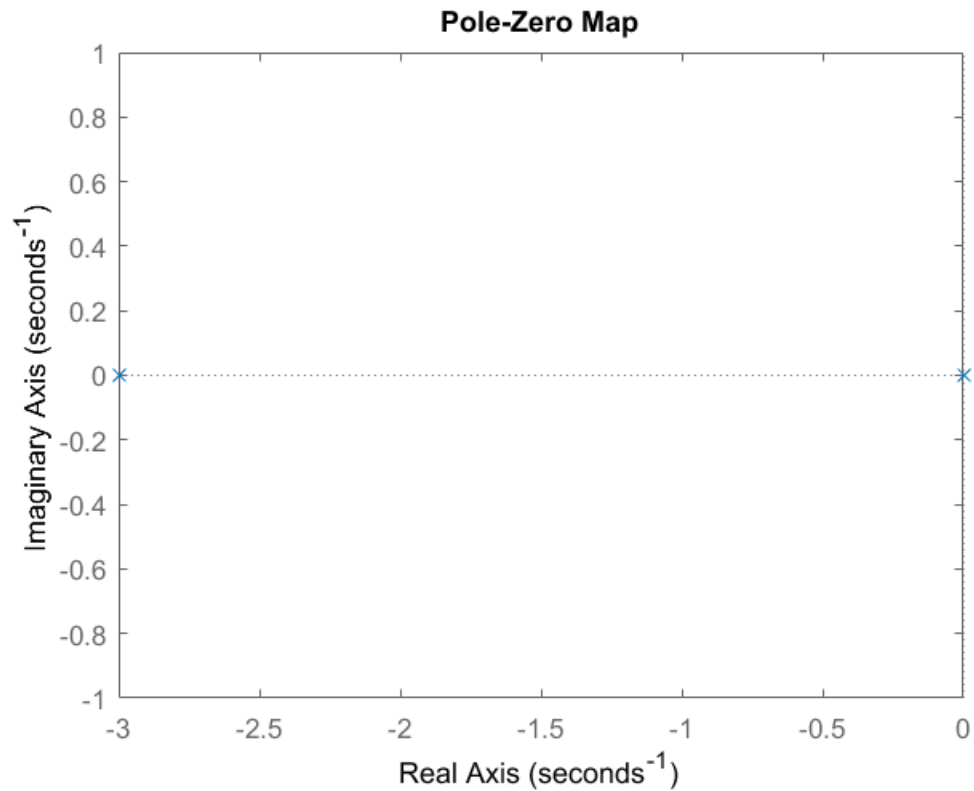
*Continuous-time transfer function.*

```
pole(G)
```

```
ans =  
0  
-3
```

## Problem 1b

```
pzmap(G)
```



Since one pole is non-zero, and one is less than zero the system is said to be marginally stable.

## Problem 1c1 and 1c2

```
(x+4)^3 = x^3 + 12x^2 + 48x + 64  
  
B = [ 64; 48; 12; 1]  
A = [ 0 0 200 0; ...  
      3 0 0 200; ...  
      1 3 0 0; ...  
      0 1 0 0]  
x = A\B  
  
C = tf([ x(4) x(3)], [ x(2),x(3)])
```

$B =$

64  
48  
12  
1

$A =$

0      0      200      0  
3      0      0      200  
1      3      0      0  
0      1      0      0

$x =$

9.0000  
1.0000  
0.3200  
0.1050

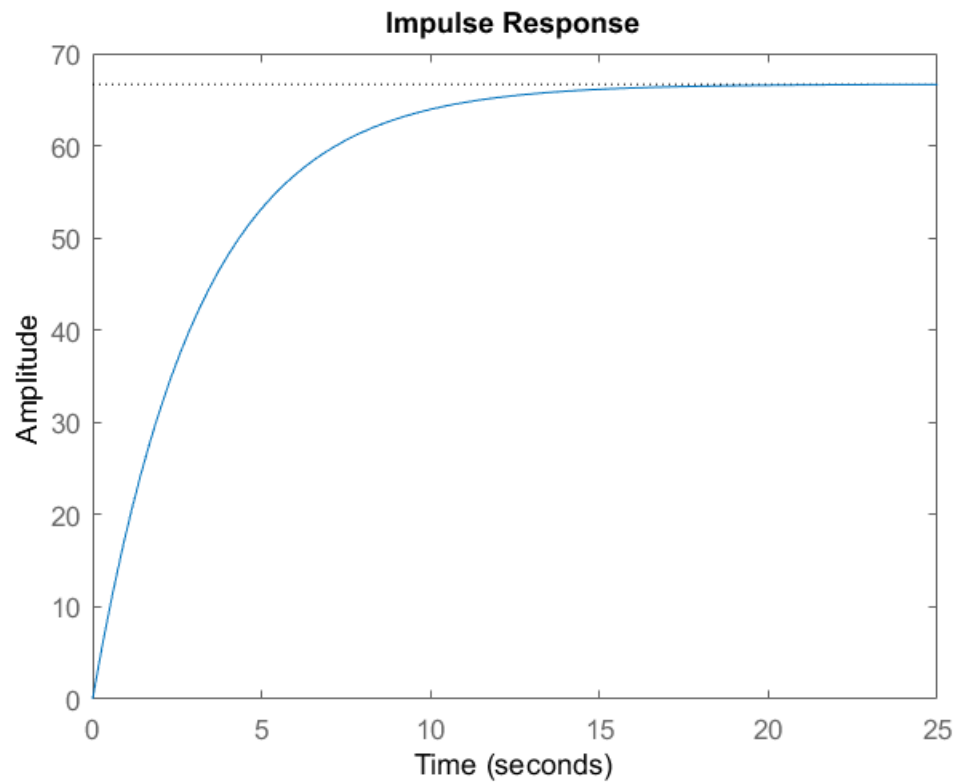
$C =$

$$\frac{0.105 s + 0.32}{s + 0.32}$$

*Continuous-time transfer function.*

## Problem 1c3

`impzplot(C*G)`



## Problem 2

$$\text{Let, } \beta = (Js^2 + Bs)^{-1}$$

$$\text{Let, } \alpha = (K_p + K_i/s)$$

$$\text{Let, } \gamma = 1 + \alpha\beta + K_d\beta s$$

$$\theta = \frac{\alpha\beta}{\gamma}\theta^d - \frac{\beta}{\gamma}D$$

## Problem 3a

```
Kd = 20;
Kp = 30;
J = 2;
B = 1;
omega = 1;
D = 1;
s = tf('s');
```

$B =$

1

The model and controller are:

$$A = 1 / (J \cdot s^2 + (B + K_d) \cdot s + K_p);$$

$$H = A \cdot (K_p \cdot \omega - D)$$

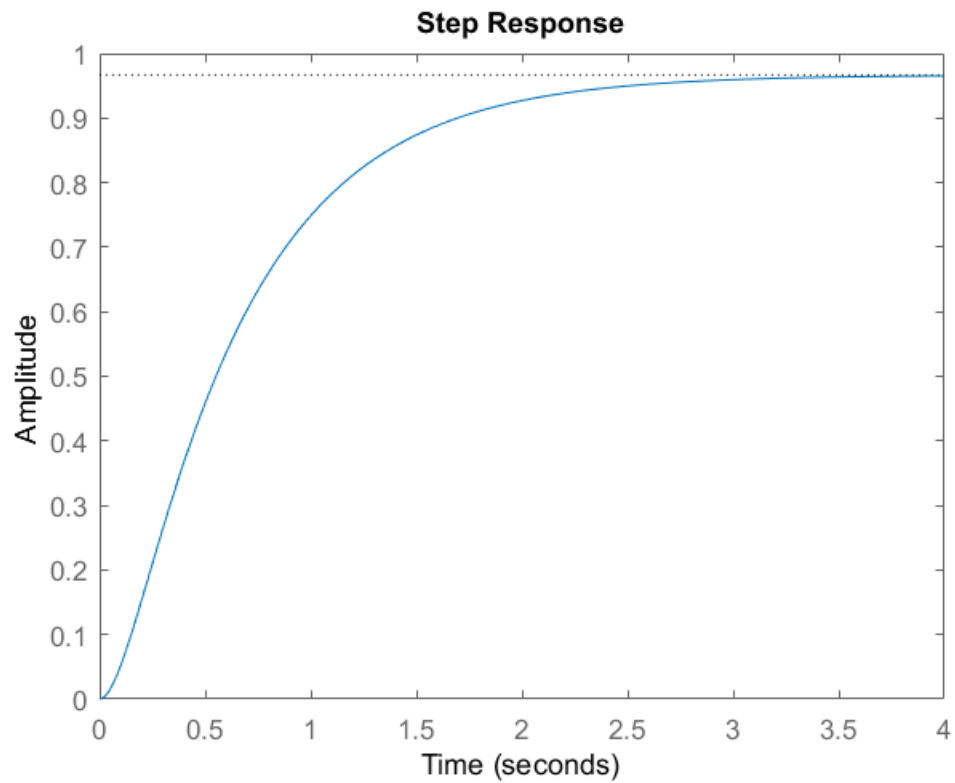
$$H =$$

$$\frac{29}{2 s^2 + 21 s + 30}$$

Continuous-time transfer function.

The poles of the transfer function are:

```
figure(2)
step(H)
```



Based on the transfer fucntion The damping ratio and natural frequency is:

$$\omega_n = \sqrt{15}$$

```

zeta = (.5*21)/(2*wn)
a = 1;
b = 2*zeta*wn;
c = wn*wn;

wn =

    3.8730

zeta =

    1.3555

if b*b > 4*a*c
    disp('over Damped')
elseif b*b < 4*a*c
    disp('under damped')
else
    disp('critical damped')
end

over Damped

```

## Problem 3b

The values for the PD control are

```

Kd_new = 79;
Kp_new = 600;
A = 1/(J*s^2 + (B+Kd_new)*s + Kp_new);
H2 = A*((Kp*omega) - D)

```

```

H2 =

    29
-----
 2 s^2 + 80 s + 600

```

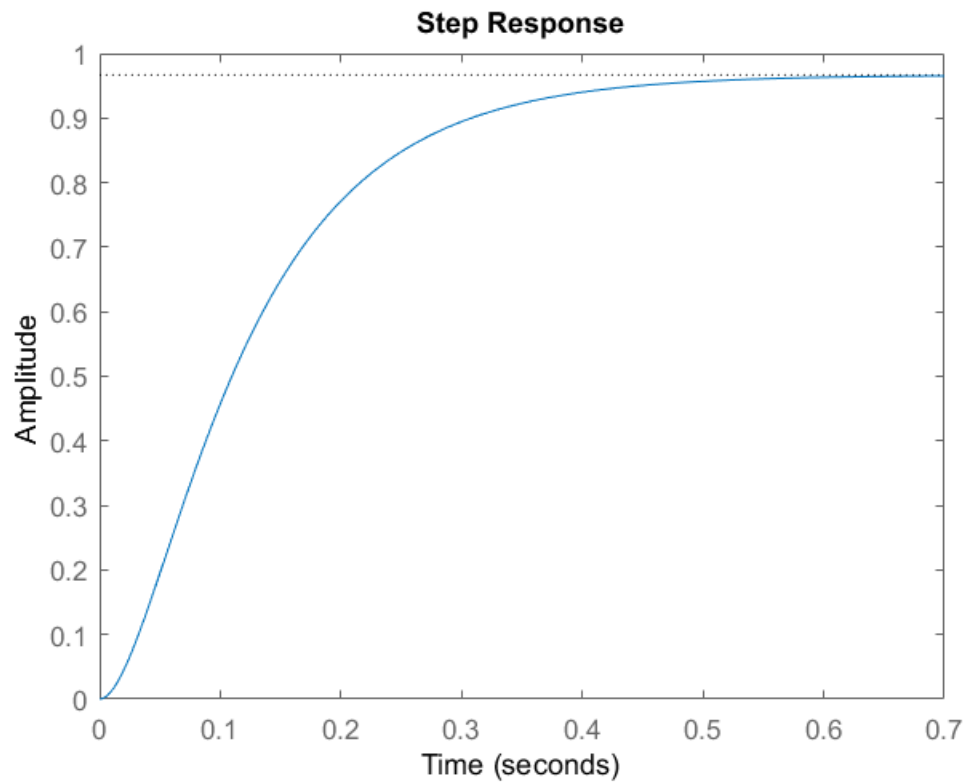
*Continuous-time transfer function.*

## Proble 3c

```

step(20*H2)

```



## Problem 3d

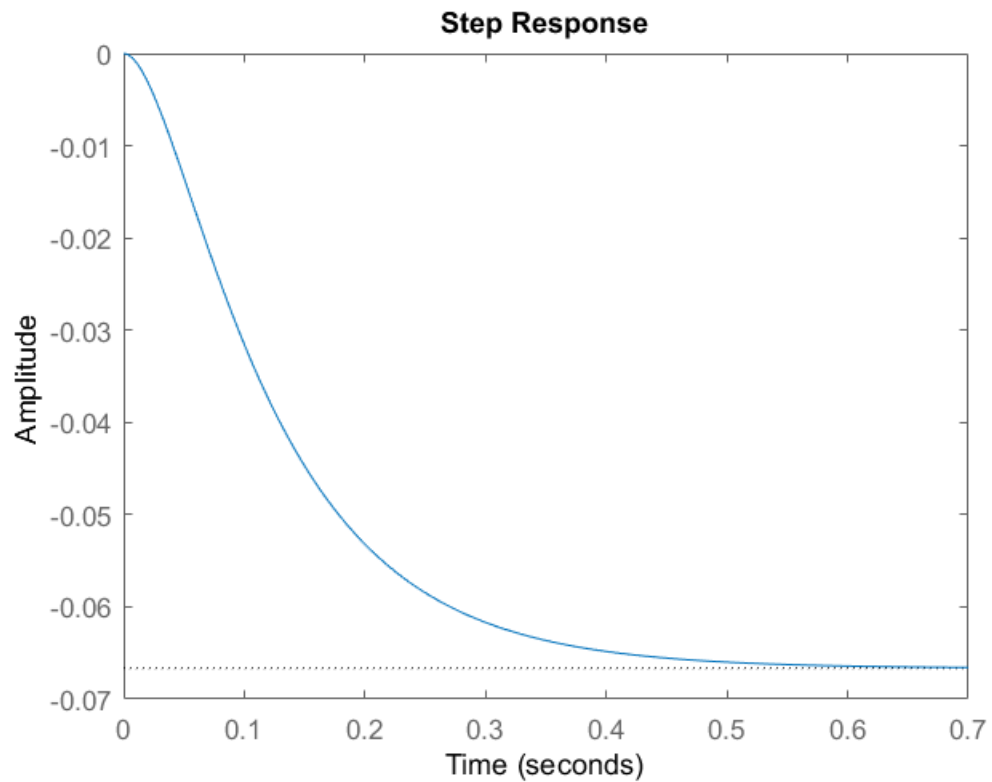
$$\lim_{s \rightarrow \infty} s \frac{40}{s} \frac{-1}{2s^2 + 80s + 600} = -40/600$$

```
A = 1/(J*s^2 + (B+Kd_new)*s + Kp_new);
D = 40;
omega = 0;
H3 = A*((Kp*omega) - D)
stepplot(H3)
```

$H3 =$

$$\frac{-40}{2 s^2 + 80 s + 600}$$

*Continuous-time transfer function.*



## Problem 4a

using the RH the following boundaries are found

$$1 + K_d > 0$$

$$K_p(1 + K_d) > 2K_I$$

$$K_I > 0$$

## Problem 4b

```
Ki_new = 1;
J = 1;
B = 2;
G = tf( [ Kp_new, Ki_new],[J, (B+Kd_new), Kp_new,Ki_new])
figure(3)
rlocus(G)
```

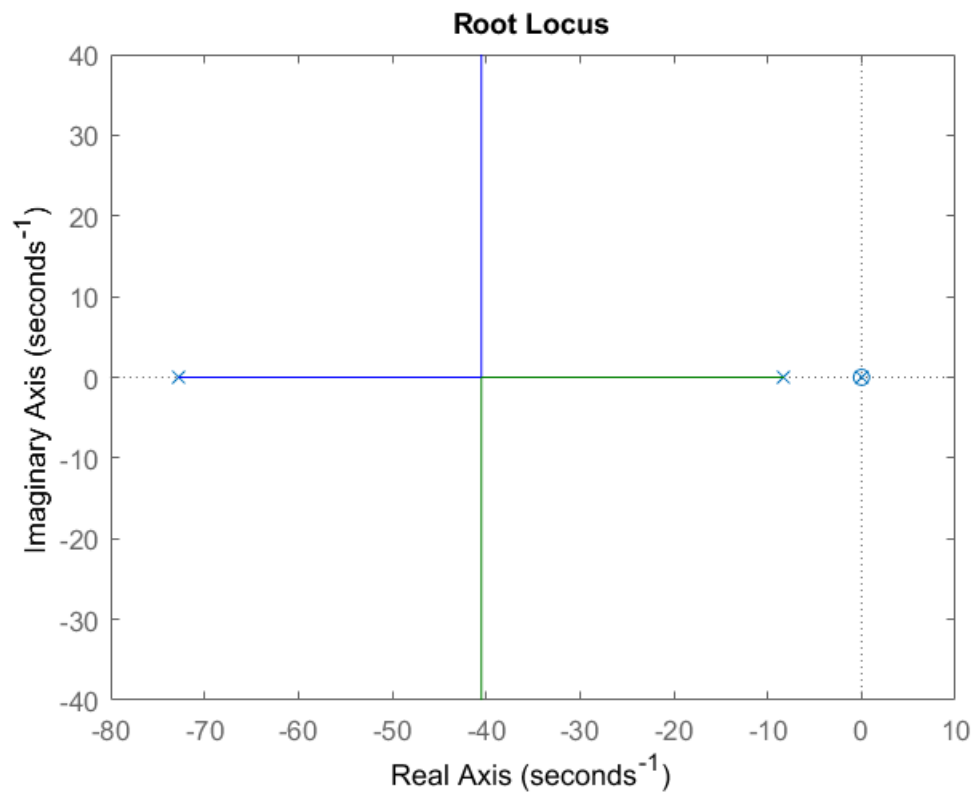
$G =$

$$\frac{600 s + 1}{-----}$$



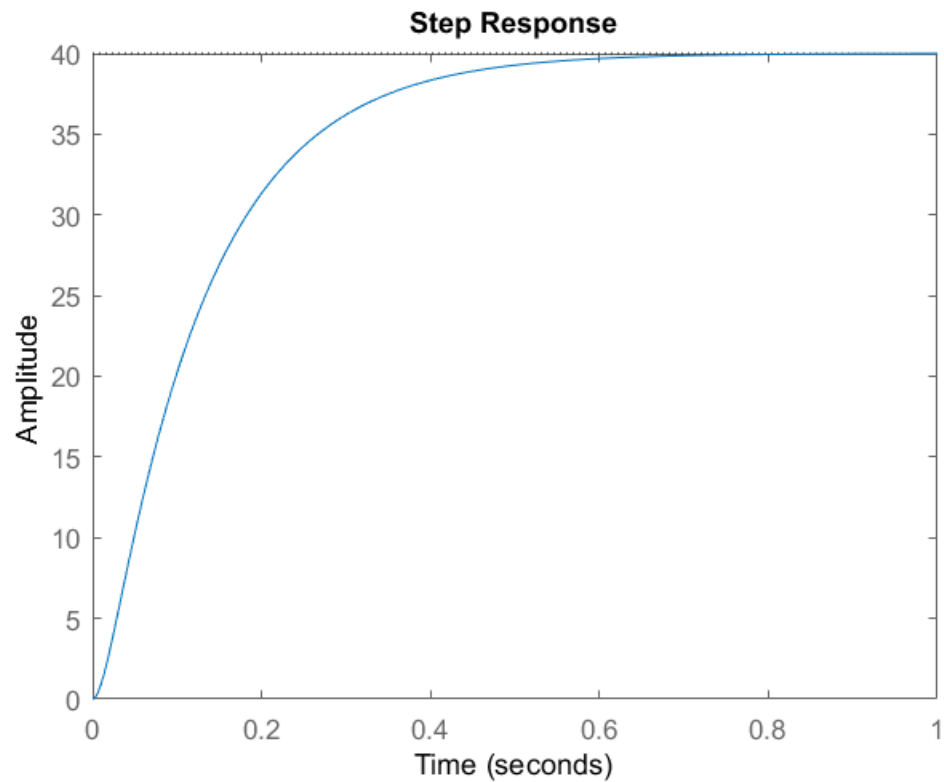
$$s^3 + 81 s^2 + 600 s + 1$$

Continuous-time transfer function.



## Problem 4c

```
figure(4)  
step(40*G)
```



## Problem 4d

```
Kp4 = 1;
Kd4 = 1;
```

Using the Routh Hurwitz criteria, the following value is set for Kd. These values are then plugged in to the closed loop transfer function. This reduces the system to a 2nd order with one zero pole

```
Ki4 = 0;
```

```
G = tf( [ Kp4, Ki4], [J, (B+Kd4), Kp4, Ki4])
```

$G =$

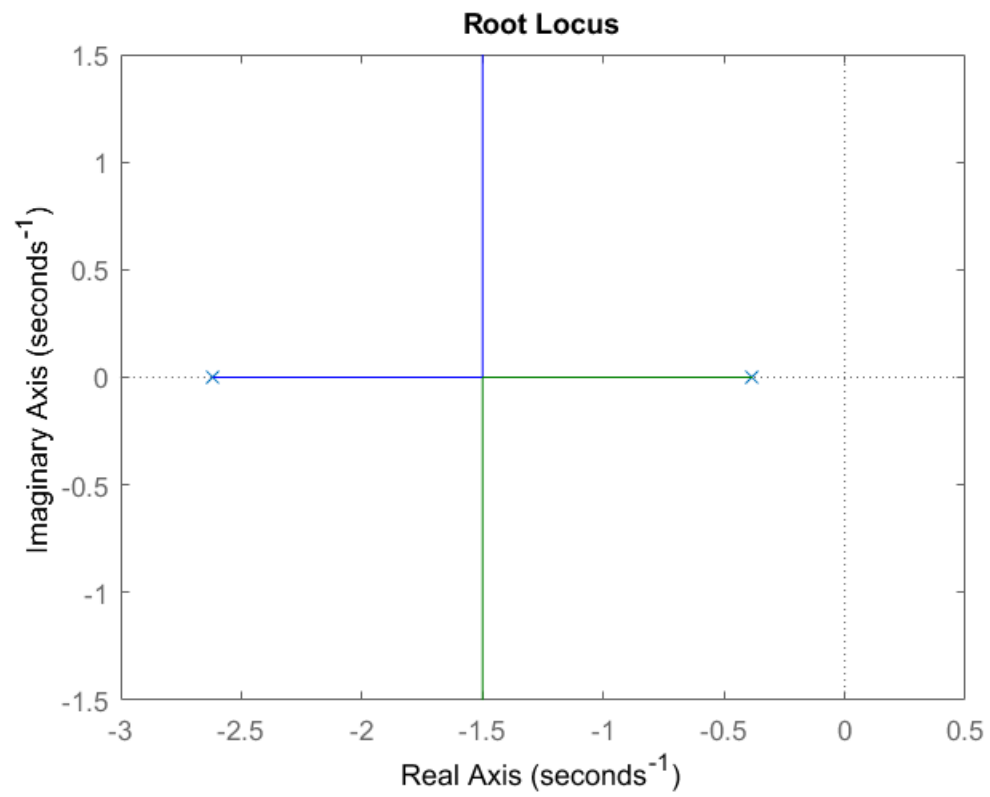
$$\frac{s}{s^3 + 3s^2 + s}$$

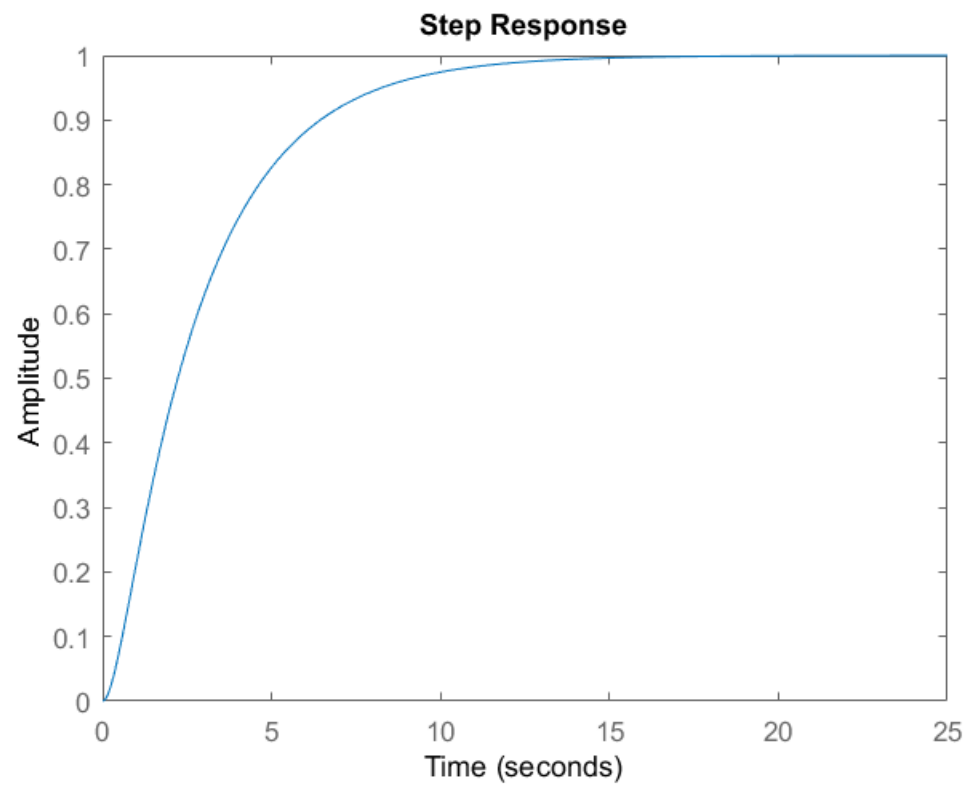
*Continuous-time transfer function.*

Plotting the root locus

```
figure(5)
rlocus(G)
```

```
figure(6)
step(G)
```





*Published with MATLAB® R2016b*