

Question 7.2

Using the 20 years of daily high temperature data for Atlanta (July through October) from Question 6.2 (file temps.txt), build and use an exponential smoothing model to help make a judgment of whether the unofficial end of summer has gotten later over the 20 years. (Part of the point of this assignment is for you to think about how you might use exponential smoothing to answer this question. Feel free to combine it with other models if you'd like to. There's certainly more than one reasonable approach.)

Note: in R, you can use either <code>HoltWinters</code> (simpler to use) or the <code>smooth</code> package's <code>es</code> function (harder to use, but more general). If you use <code>es</code>, the Holt-Winters model uses <code>model="AAM"</code> in the function call (the first and second constants are used "A"dditively, and the third (seasonality) is used "M"ultiplicatively; the documentation doesn't make that clear).

Single Exponential Smoothness(ES) Values: # alpha: 0.8396301 # sum of squared error(SSE):53704.15

Double ES Values

alpha: 0.8455303 # beta: 0.003777803 # SSE: 54071.22

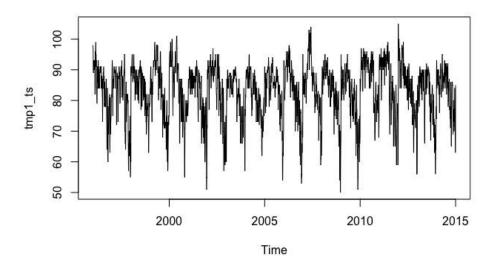
Triple ES Values:

alpha: 0.6677614

beta : 0

gamma: 0.6297674 # SSE: 63025.97





#Single ES has smallest SSE when compared to other two and it is closed to 1. It means there is less randomness in the system and recent temperature reading has more weight in predicting the current temperature.

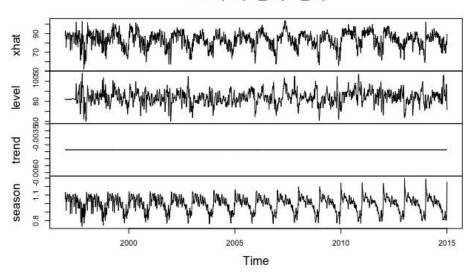
#Seasonality uses Model AAM:

#1. A - additive: seasonal variation is independent #2. M - multiplicative: seasonal variation is connected.

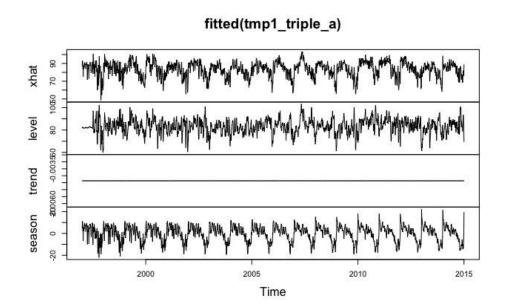
#Triple Exponential – using multiplicative #SSE:65648.65







#Triple Exponential - using additive #SSE:63025.97



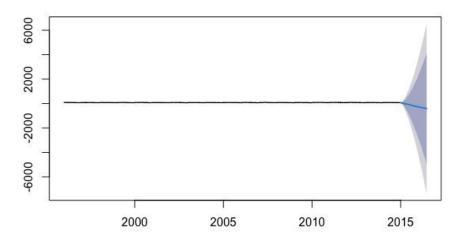
Triple ES with additive seasonal factor has better SSE.

From the above chart, Trend line is straight which means no trend.

The season sub chart shows that the duration of each season has been constant throughout all 20 years.



Forecasts from HoltWinters



The above plot reflects the actual.. Use Chkum formula from previous lesson St = max(0, St-1 + (Xmean - T - C)) as a running equation across each daily temperature observation there wasn't much of a change.

I. R Script

```
## Clear Work Area ##
rm(list=ls()) #clear environment
cat("\014") #clear console
#Load dara from temperature table
getwd()
##Input data
tmp1_data <- read.table("temps.txt", header = TRUE) #read txt data into a table
#Exploring the data
tail(tmp_data)[1:5,]
str(tmp1_data)
print(summary(tmp1_data))
#Marix of temperature data
tmp1_mat <- as.vector(unlist(tmp1_data[,2:21]))
str(tmp1_mat)
tmp1_mat
# Time Series Values
```



```
tmp1_ts <- ts(tmp1_mat, start=1996, end = 2015, frequency=123)
tmp1_ts
class(tmp1_ts)
plot(tmp1_ts)
# Define beta to generate trend value to forecast a future trend
tmp1_b_ts <- HoltWinters(tmp1_ts , beta=.5)</pre>
plot(tmp1_b_ts)
# Exponential Smoothing
#Simple Exponential #
tmp1_single <- HoltWinters(tmp1_ts,beta=FALSE, gamma=FALSE)</pre>
#Double Exponential - model trend #
tmp1_double <- HoltWinters(tmp1_ts,gamma=FALSE)</pre>
#Triple Exponential - model trend and seasonality#
tmp1_triple <- HoltWinters(tmp1_ts, seasonal = "additive")</pre>
#Compare 3 kinds of Exp Smoothing#
tmp1_single
tmp1_single$SSE # Sum of Squared Error
tmp1_double
tmp1_double$SSE
tmp1_triple
tmp1_triple$SSE
# Triple Exponential using multiplicative ( Seasonal varioation is connected)
tmp1_triple_m <- HoltWinters(tmp1_ts, seasonal = "multiplicative")
tmp1_triple_m$SSE
# Triple Exponential using multiplicative ( Seasonal varioation is independent of the level)
tmp1_triple_a <- HoltWinters(tmp1_ts, seasonal = "additive")</pre>
tmp1_triple_a$SSE
tmp1_triple_a$fitted
plot(fitted(tmp1_triple_a))
plot(fitted(tmp1_triple_m))
#Forecast
```



```
library(forecast)
tmp1_forecast=predict( tmp1_b_ts, n.ahead = 100, prediction.interval = TRUE )
plot(forecast( tmp1_b_ts, h = 180 ))
```

R-Script With Answers

```
> #Load dara from temperature table
> getwd()
[1] "/Users/nagarajanmurugan/Documents/MS/Data"
> ##Input data
> tmp1_data <- read.table("temps.txt", header = TRUE) #read txt data into a table
>
> #Exploring the data
> str(tmp1 data)
'data.frame': 123 obs. of 21 variables:
$ DAY : chr "1-Jul" "2-Jul" "3-Jul" "4-Jul" ...
$ X1996: int 98 97 97 90 89 93 93 91 93 93 ...
$ X1997: int 86 90 93 91 84 84 75 87 84 87 ...
$ X1998: int 91 88 91 91 91 89 93 95 95 91 ...
$ X1999: int 84 82 87 88 90 91 82 86 87 87 ...
$ X2000: int 89 91 93 95 96 96 96 91 96 99 ...
$ X2001: int 84 87 87 84 86 87 87 89 91 87 ...
$ X2002: int 90 90 87 89 93 93 89 89 90 91 ...
$ X2003: int 73 81 87 86 80 84 87 90 89 84 ...
$ X2004: int 82 81 86 88 90 90 89 87 88 89 ...
$ X2005: int 91 89 86 86 89 82 76 88 89 78 ...
$ X2006: int 93 93 93 91 90 81 80 82 84 84 ...
$ X2007: int 95 85 82 86 88 87 82 82 89 86 ...
```



```
$ X2008: int 85 87 91 90 88 82 88 90 89 87 ...
$ X2009: int 95 90 89 91 80 87 86 82 84 84 ...
$ X2010: int 87 84 83 85 88 89 94 97 96 90 ...
$ X2011: int 92 94 95 92 90 90 94 94 91 92 ...
$ X2012: int 105 93 99 98 100 98 93 95 97 95 ...
$ X2013: int 82 85 76 77 83 83 79 88 88 87 ...
$ X2014: int 90 93 87 84 86 87 89 90 90 87 ...
$ X2015: int 85 87 79 85 84 84 90 90 91 93 ...
> print(summary(tmp1_data))
  DAY
              X1996
                                   X1998
                        X1997
                                              X1999
              Min. :60.00 Min. :55.00 Min. :63.00 Min. :57.00
Length:123
Class:character 1st Qu.:79.00 1st Qu.:78.50 1st Qu.:79.50 1st Qu.:75.00
Mode :character Median :84.00 Median :84.00 Median :86.00 Median :86.00
         Mean :83.72 Mean :81.67 Mean :84.26 Mean :83.36
         3rd Qu.:90.00 3rd Qu.:88.50 3rd Qu.:89.00 3rd Qu.:91.00
         Max. :99.00 Max. :95.00 Max. :95.00 Max. :99.00
                                   X2003
                                              X2004
  X2000
             X2001
                        X2002
                                                         X2005
Min.: 55.00 Min.: 51.00 Min.: 57.00 Min.: 57.00 Min.: 62.00 Min.: 54.00
1st Qu.: 77.00 1st Qu.:78.00 1st Qu.:78.00 1st Qu.:78.00 1st Qu.:78.00 1st Qu.:81.50
Median: 86.00 Median: 84.00 Median: 87.00 Median: 84.00 Median: 82.00 Median: 85.00
Mean: 84.03 Mean: 81.55 Mean: 83.59 Mean: 81.48 Mean: 81.76 Mean: 83.36
3rd Qu.: 91.00 3rd Qu.:87.00 3rd Qu.:91.00 3rd Qu.:87.00 3rd Qu.:87.00 3rd Qu.:88.00
Max. :101.00 Max. :93.00 Max. :97.00 Max. :91.00 Max. :95.00 Max. :94.00
  X2006
             X2007
                        X2008
                                   X2009
                                              X2010
                                                         X2011
Min. :53.00 Min. :59.0 Min. :50.00 Min. :51.00 Min. :67.00 Min. :59.00
1st Qu.:79.00 1st Qu.: 81.0 1st Qu.:79.50 1st Qu.:75.00 1st Qu.:82.00 1st Qu.:79.00
Median: 85.00 Median: 86.0 Median: 85.00 Median: 83.00 Median: 90.00 Median: 89.00
Mean :83.05 Mean :85.4 Mean :82.51 Mean :80.99 Mean :87.21 Mean :85.28
3rd Qu.:91.00 3rd Qu.: 89.5 3rd Qu.:88.50 3rd Qu.:88.00 3rd Qu.:93.00 3rd Qu.:94.00
Max. :98.00 Max. :104.0 Max. :95.00 Max. :95.00 Max. :97.00 Max. :99.00
                        X2014
  X2012
             X2013
                                   X2015
Min.: 56.00 Min.: 56.00 Min.: 63.00 Min.: 56.0
1st Qu.: 79.50 1st Qu.:77.00 1st Qu.:81.50 1st Qu.:77.0
Median: 85.00 Median: 84.00 Median: 86.00 Median: 85.0
Mean: 84.65 Mean: 81.67 Mean: 83.94 Mean: 83.3
3rd Qu.: 90.50 3rd Qu.:88.00 3rd Qu.:89.00 3rd Qu.:90.0
Max. :105.00 Max. :92.00 Max. :95.00 Max. :97.0
> #Marix of temperature data
> tmp1_mat <- as.vector(unlist(tmp1_data[,2:21]))
> str(tmp1_mat)
int [1:2460] 98 97 97 90 89 93 93 91 93 93 ...
>tmp1 mat
 [1] 98 97 97 90 89 93 93 91 93 93 90 91 93 93 82 91 96 95 96 99 91 95 91
[24] 93 84 84 82 79 90 91 87 86 90 84 91 93 88 91 84 90 89 88 86 84 86 89
[47] 90 91 91 90 89 90 91 91 91 84 88 84 86 88 84 82 80 73 87 84 87 89 89
[70] 89 91 84 86 88 78 79 86 82 82 78 79 79 78 81 84 84 87 84 79 75 72 64
```



```
[93] 66 72 84 70 66 64 60 78 70 72 69 69 73 79 81 80 82 66 63 68 79 81 69
[116] 73 73 75 75 81 82 82 81 86 90 93 91 84 84 75 87 84 87 84 88 86 90 91
[139] 91 89 89 89 90 89 84 87 88 89 89 91 91 89 88 72 80 84 88 89 88 84 84
[162] 80 73 80 86 88 88 87 88 91 91 89 89 88 82 79 81 82 84 87 90 90 91 91
[185] 88 88 91 93 81 81 82 86 88 84 80 82 86 87 87 88 88 90 88 91 95 89 70
[208] 80 82 66 70 64 68 77 86 75 73 75 78 81 82 82 82 80 82 82 79 80 68 63
[231] 57 66 64 69 70 70 62 63 62 75 71 57 55 64 66 60 91 88 91 91 91 89 93
[254] 95 95 91 91 86 88 87 91 87 90 91 95 91 91 89 91 91 86 88 80 88 89 90
[277] 86 86 82 84 86 90 89 89 86 82 87 88 84 86 80 82 86 84 87 90 79 84 87
[300] 87 88 90 91 89 90 93 93 91 87 84 77 90 91 89 90 89 79 78 81 84 89 87
[323] 87 88 87 82 80 82 82 88 84 81 82 84 87 80 75 75 86 78 77 82 82 73 82
[346] 69 72 73 78 78 78 75 79 78 77 78 82 75 73 63 63 72 75 79 79 79 78 82
[369] 79 84 82 87 88 90 91 82 86 87 87 82 77 73 81 81 86 82 87 88 90 90 91
[392] 93 93 91 93 93 93 93 97 99 96 93 88 89 91 93 93 93 91 90 96 98 97 98
[415] 93 93 96 98 98 89 91 91 90 80 82 89 88 90 91 91 84 88 91 84 93 96 96
[438] 91 91 77 87 87 87 86 87 89 81 81 82 79 68 79 72 75 78 81 82 78 80 77
[461] 71 73 75 84 71 73 71 73 73 72 72 73 70 64 75 73 77 80 71 66 60 64 73
[484] 57 59 64 69 75 73 72 75 75 89 91 93 95 96 96 96 91 96 99 96 93 91 93
[507] 93 93 91 97 100 99 93 96 87 82 75 82 88 91 89 87 86 86 81 84 88 91 91
[530] 91 91 96 95 89 89 89 89 94 97 99 101 101 97 87 86 88 92 92 90 90 92 92
[553] 88 87 79 81 82 87 81 66 66 75 80 82 84 86 87 86 80 75 73 73 84 87 77
[576] 73 81 84 82 68 71 75 73 75 77 79 82 81 82 73 66 55 55 64 71 73 75 75
[599] 77 80 80 80 73 73 75 79 75 75 78 75 78 80 75 77 78 84 87 87 84 86 87
[622] 87 89 91 87 90 90 86 82 82 84 87 88 90 87 84 87 90 84 82 88 90 84 89
[645] 89 87 84 84 84 86 88 84 86 88 87 88 86 86 81 87 84 90 91 91 87 86 88
[668] 90 88 93 90 91 91 81 86 81 82 80 75 73 81 90 88 87 86 86 89 87 84 84
[691] 86 77 77 81 81 82 84 86 87 88 69 66 72 75 78 71 71 75 80 81 80 79 70
[714] 68 79 66 73 75 78 78 75 75 62 60 64 71 75 79 80 81 79 73 64 51 55 63
[737] 72 71 90 90 87 89 93 93 89 89 90 91 84 77 82 88 91 93 93 93 93 91 95
[760] 91 89 87 84 86 89 91 91 88 90 93 91 91 93 97 87 87 86 88 89 91 91
[783] 89 88 90 91 93 91 93 93 91 95 93 91 88 84 82 82 78 77 84 84 89 95 93
[806] 91 88 87 91 95 95 90 75 78 91 88 86 81 80 86 84 77 82 73 69 75 75 79
[829] 73 79 82 84 84 82 87 86 80 71 66 70 78 84 79 68 57 66 64 68 71 73 71
[852] 64 59 68 60 68 69 75 75 68 60 73 81 87 86 80 84 87 90 89 84 84 86 87
[875] 84 86 88 88 88 88 88 89 86 81 82 84 87 87 89 88 84 88 84 84 84 82 84
[898] 82 84 84 86 87 84 81 87 89 90 86 89 90 90 87 88 88 90 89 88 89 90 91
[921] 89 88 89 88 86 87 87 84 73 75 81 82 79 80 81 84 82 82 81 81 81 84 87
[944] 82 75 81 80 82 82 82 73 66 71 72 68 66 77 78 75 73 73 73 73 66 78 78
[967] 78 69 72 68 70 75 78 84 78 78 73 73 68 64 57 70 77 75 82 81 86 88 90
[990] 90 89 87 88 89 90 89 91 91 84 84
[ reached getOption("max.print") -- omitted 1460 entries ]
> # Time Series Values
> tmp1_ts <- ts(tmp1_mat, start=1996, end = 2015, frequency=123)
> tmp1_ts
Time Series:
Start = c(1996, 1)
```



End = c(2015, 1) Frequency = 123

[reached getOption("max.print") -- omitted 1338 entries]



```
> class(tmp1_ts)
[1] "ts"
> plot(tmp1_ts)
> # Define beta to generate trend value to forecast a future trend
> tmp1_b_ts <- HoltWinters(tmp1_ts , beta=.5)
> plot(tmp1_b_ts)
> # Exponential Smoothing
> #Simple Exponential #
> tmp1_single <- HoltWinters(tmp1_ts,beta=FALSE, gamma=FALSE)
> #Double Exponential - model trend #
> tmp1_double <- HoltWinters(tmp1_ts,gamma=FALSE)
> #Triple Exponential - model trend and seasonality#
> tmp1_triple <- HoltWinters(tmp1_ts, seasonal = "additive")
> #Compare 3 kinds of Exp Smoothing#
> tmp1_single
Holt-Winters exponential smoothing without trend and without seasonal component.
Call:
HoltWinters(x = tmp1_ts, beta = FALSE, gamma = FALSE)
Smoothing parameters:
alpha: 0.8396301
beta: FALSE
gamma: FALSE
Coefficients:
  [,1]
a 81.62444
> tmp1_single$SSE # Sum of Squared Error
[1] 53704.15
>
> tmp1 double
Holt-Winters exponential smoothing with trend and without seasonal component.
Call:
HoltWinters(x = tmp1_ts, gamma = FALSE)
Smoothing parameters:
alpha: 0.8455303
beta: 0.003777803
gamma: FALSE
```



```
Coefficients:
    [,1]
a 81.729657393
b -0.004838906
> tmp1_double$SSE
[1] 54071.22
> tmp1_triple
Holt-Winters exponential smoothing with trend and additive seasonal component.
Call:
HoltWinters(x = tmp1_ts, seasonal = "additive")
Smoothing parameters:
alpha: 0.6677614
beta:0
gamma: 0.6297674
Coefficients:
      [,1]
   66.739214602
b -0.004362918
s1 17.167113056
s2 12.692593452
s3 11.926233267
s4 12.862822489
s5 11.026083880
s6 8.860499089
s7 9.547553333
s8 7.755384526
s9 4.419013466
s10 2.272689626
s11 4.628251667
s12 2.396834852
s13 3.512957136
s14 1.734948091
s15 3.035023890
s16 6.257944053
s17 5.086362292
s18 8.599153274
s19 5.507486014
s20 10.404819396
s21 10.115801978
s22 9.628840064
s23 7.658623118
```

s24 7.150473636



- s25 6.306599371
- s26 5.850691115
- s27 5.770487458
- s28 4.280481134
- s29 7.229771199
- s30 4.632381095
- s31 6.006248308
- s32 6.443645890
- s33 5.701166527
- s34 3.546887269
- s35 3.879569716
- s36 3.517339384
- s37 2.828550977
- s38 2.122971410
- s39 2.627923984
- s40 1.658896597
- s41 0.165866282
- 341 0.103000202
- s42 -0.001574460
- s43 -1.557500303
- s44 -2.159601227
- s45 -2.260609558 s46 0.474052766
- 340 0.474032700
- s47 2.501631056
- s48 6.552191593
- s49 7.240238719
- s50 8.395899120
- s51 8.633263084
- s52 7.504540260
- s53 4.804135812
- s54 0.449902809
- s55 -1.045831475
- s56 1.562077049
- s57 1.632745190
- s58 0.857309158
- s59 2.909614779
- s60 0.626594899
- s61 4.491805650
- s62 4.567058619 s63 3.065433531
- s64 3.787652805
- s65 -2.147135463
- s66 1.759895146
- s67 1.541155061
- s68 1.278521842
- s69 0.895959617
- s70 2.009912430
- s71 3.695537344



- s72 4.675235988
- s73 4.535880359
- s74 1.710420810
- s75 0.822675780
- s76 2.363162195
- s77 1.925012161
- s78 -1.656914701
- s79 -1.809929506
- s80 -0.427021203
- 300 0.427021203
- s81 0.056812125
- s82 -1.137248149
- s83 -1.037423821
- s84 -2.817503990
- s85 -4.578240308
- s86 -3.080091372
- s87 -2.710719111
- s88 -2.255335538
- s89 -4.518502545
- s90 -5.159556421
- s91 -4.440834373
- s92 -5.790113744
- s93 -7.461163074
- s94 -8.882612687
- s95 -8.619859733
- s96 -6.200719796
- s97 -6.055889182
- s98 -11.167287691
- s99 -13.489975101
- s100 -13.615536188
- s101 -14.373453486
- s102 -15.142110213
- s103 -14.419874185
- s104 -14.023613348
- s105 -16.187082843
- s106 -15.999259045
- s107 -12.074075053
- s108 -9.199729415
- s109 -10.403127076
- s110 -12.075113349
- s111 -9.722863134
- s112 -5.846856763
- s113 -8.047801338
- s114 -9.636669876
- s115 -10.510269852 s116 -12.876648138
- s117 -8.657362442
- s118 -9.828539578



```
s119 -14.522204766
s120 -11.852457644
s121 -8.714763993
s122 -4.711332904
s123 18.737998957
> tmp1 triple$SSE
[1] 63025.97
>
> # Triple Exponential using multiplicative ( Seasonal varioation is connected)
> tmp1_triple_m <- HoltWinters(tmp1_ts, seasonal = "multiplicative")
> tmp1 triple m$SSE
[1] 65648.65
>
>
> # Triple Exponential using multiplicative ( Seasonal varioation is independent of the level)
> tmp1_triple_a <- HoltWinters(tmp1_ts, seasonal = "additive")
> tmp1 triple a$SSE
[1] 63025.97
>
> tmp1_triple_a$fitted
Time Series:
Start = c(1997, 1)
End = c(2015, 1)
Frequency = 123
      xhat level
                     trend
                              season
1997.000 87.17619 82.87739 -0.004362918 4.303159495
1997.008 90.32137 82.08762 -0.004362918 8.238118845
1997.016 92.95607 81.86865 -0.004362918 11.091777381
1997.024 90.93226 81.89363 -0.004362918 9.042996893
1997.033 83.99752 81.93450 -0.004362918 2.067387137
1997.041 84.04359 81.93179 -0.004362918 2.116167625
1997.049 75.06703 81.89832 -0.004362918 -6.826921806
1997.057 87.04230 81.84919 -0.004362918 5.197468438
1997.065 84.01782 81.81658 -0.004362918 2.205598519
1997.073 87.05847 81.80032 -0.004362918 5.262509089
1997.081 84.04758 81.75692 -0.004362918 2.295029414
1997.089 88.04397 81.72078 -0.004362918 6.327549739
1997.098 86.02650 81.68706 -0.004362918 4.343809902
1997.106 89.93127 81.66500 -0.004362918 8.270639170
1997.114 90.90776 81.70653 -0.004362918 9.205598519
1997.122 90.94873 81.76376 -0.004362918 9.189338357
1997.130 88.92982 81.79363 -0.004362918 7.140557869
1997.138 88.90728 81.83613 -0.004362918 7.075517219
1997.146 88.88353 81.89368 -0.004362918 6.994216406
1997.154 89.85938 81.96709 -0.004362918 7.896655430
1997.163 88.81884 82.05663 -0.004362918 6.766574129
1997.171 83.84602 82.17324 -0.004362918 1.677143235
```



```
1997.179 87.03391 82.27170 -0.004362918 4.766574129
1997.187 88.03942 82.24469 -0.004362918 5.799094454
1997.195 89.02500 82.21400 -0.004362918 6.815354617
1997.203 89.17467 82.19295 -0.004362918 6.986086324
1997.211 91.16749 82.07195 -0.004362918 9.099907462
1997.220 91.17324 81.95574 -0.004362918 9.221858682
1997.228 89.11010 81.83570 -0.004362918 7.278769251
1997.236 87.99157 81.75781 -0.004362918 6.238118845
1997.244 71.81397 81.75908 -0.004362918 -9.940742944
1997.252 79.86066 81.87894 -0.004362918 -2.013913676
1997.260 83.94121 81.96762 -0.004362918 1.977956243
1997.268 88.04928 82.00251 -0.004362918 6.051126975
1997.276 88.94697 81.96524 -0.004362918 6.986086324
1997.285 87.85607 81.99629 -0.004362918 5.864135105
1997.293 83.80148 82.08804 -0.004362918 1.717793641
1997.301 83.75082 82.21625 -0.004362918 1.538931853
1997.309 79.88033 82.37828 -0.004362918 -2.493588472
1997.317 72.87458 82.45383 -0.004362918 -9.574889285
1997.325 79.87267 82.53322 -0.004362918 -2.656190098
1997.333 85.84764 82.61388 -0.004362918 3.238118845
1997.341 87.86372 82.71126 -0.004362918 5.156818032
1997.350 87.89345 82.79790 -0.004362918 5.099907462
1997.358 87.04967 82.86469 -0.004362918 4.189338357
1997.366 88.15848 82.82716 -0.004362918 5.335679820
1997.374 91.23528 82.71697 -0.004362918 8.522671690
1997.382 91.20389 82.55550 -0.004362918 8.652752991
1997.390 89.07964 82.41499 -0.004362918 6.669013154
1997.398 88.97332 82.35745 -0.004362918 6.620232666
1997.407 87.97051 82.37090 -0.004362918 5.603972503
1997.415 82.05901 82.38623 -0.004362918 -0.322856765
1997.423 79.16971 82.34246 -0.004362918 -3.168385220
1997.431 81.10080 82.22477 -0.004362918 -1.119604733
1997.439 82.11856 82.15310 -0.004362918 -0.030173838
1997.447 84.01877 82.06956 -0.004362918 1.953565999
1997.455 87.03439 82.05267 -0.004362918 4.986086324
1997.463 90.15341 82.02534 -0.004362918 8.132427788
1997.472 90.25799 81.91854 -0.004362918 8.343809902
1997.480 91.22769 81.74190 -0.004362918 9.490151365
1997.488 91.20137 81.58550 -0.004362918 9.620232666
1997.496 84.21295 81.44667 -0.004362918 2.770639170
1997.504 80.81467 83.97116 -0.004362918 -3.152125058
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[ reached getOption("max.print") -- omitted 1965 rows ]
> plot(fitted(tmp1_triple_a))
> plot(fitted(tmp1_triple_m))
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- > #Forecast
- > library(forecast)
- > tmp1_forecast=predict(tmp1_b_ts, n.ahead = 100, prediction.interval = TRUE)
- > plot(forecast(tmp1_b_ts, h = 180))