Quantum Computing cheatsheet

2024-09-10 by Naglis Šuliokas

1. Basics:

$$|0\rangle = \begin{bmatrix} 1\\0 \end{bmatrix}, |1\rangle = \begin{bmatrix} 0\\1 \end{bmatrix}, |\pm\rangle = \frac{1}{\sqrt{2}}(|0\rangle \pm |1\rangle), iY = ZX$$

2. Phase kickback

$$|\psi\rangle \longrightarrow |\psi_{\theta}\rangle$$

$$|v\rangle \longrightarrow U \longrightarrow |v\rangle$$

$$U|v\rangle = e^{i\theta}|v\rangle$$

$$\psi \text{ is in superposition}$$

3. Superdense coding

$$\begin{split} |\Phi^{+}\rangle &= \mathrm{CNOT}\left(H\otimes I\right)|0\rangle\otimes|0\rangle = \frac{1}{\sqrt{2}}(|00\rangle + |11\rangle), \,\, \mathrm{encodes} \,\, 00 \\ |\Phi^{-}\rangle &= \qquad \qquad (Z\otimes I)\,|\Phi^{+}\rangle = \frac{1}{\sqrt{2}}(|00\rangle - |11\rangle), \,\, \mathrm{encodes} \,\, 01 \\ |\Psi^{+}\rangle &= \qquad \qquad (X\otimes I)\,|\Phi^{+}\rangle = \frac{1}{\sqrt{2}}(|01\rangle + |10\rangle), \,\, \mathrm{encodes} \,\, 10 \\ |\Psi^{-}\rangle &= \qquad \qquad (iY\otimes I)\,|\Phi^{+}\rangle = \frac{1}{\sqrt{2}}(|01\rangle - |10\rangle), \,\, \mathrm{encodes} \,\, 11 \end{split}$$

4. Oracles

$$|x\rangle \longrightarrow |x\rangle \qquad |x\rangle \longrightarrow |x\rangle \qquad |x\rangle \longrightarrow (-1)^{f(x)} |x\rangle$$

$$|y\rangle \longrightarrow U_f \longrightarrow |y \oplus f(x)\rangle \qquad |0\rangle \longrightarrow U_f \longrightarrow |f(x)\rangle \qquad |-\rangle \longrightarrow U_f \longrightarrow |-\rangle$$

- 5. Deutsch's algorithm
- 6. Deutsch-Jozsa algorithm

$$H^{\otimes n} |0\rangle^{\otimes n} = \frac{1}{\sqrt{2^n}} \sum_{x \in \{0,1\}^n} |x\rangle$$

$$H^{\otimes n} |x\rangle = \frac{1}{\sqrt{2^n}} \sum_{z \in \{0,1\}^n} (-1)^{x \cdot z} |z\rangle$$

References:

- 1. Quantum Soar on YouTube.
- Nielsen, M. A., & Chuang, I. L. (2001). Quantum computation and quantum information (Vol. 2). Cambridge: Cambridge university press.