# Package 'MaxWiK'

# November 2, 2022

**Title** Machine learning method based on Maxima Weighted Isolation Kernel mean embedding **Version** 1.0.0

**Description** This software is a package named \*\*MaxWiK\*\* contains Approximate Bayesian Computation method to choose a single parameter for a single observation point. The method involves the transformation of row data to a Hilbert space (mapping) and the measurement of the similarity between simulated points and maxima weighted Isolation Kernel mapping related to the observation point. We also design a heuristic algorithm for parameter estimation that requires no calculation and is dimension independent.

```
License AGPL (>= 3)
Depends R (>= 3.6.0)
Imports graphics,
     grDevices,
     randomcoloR,
     methods,
     stats,
     utils.
     scales,
     bayestestR,
     parallel,
     plotly,
     kernlab,
     abc,
     magrittr,
     ggplot2
Suggests rmarkdown,
     knitr,
     testthat,
     DiagrammeR
Encoding UTF-8
Roxygen list(markdown = TRUE)
RoxygenNote 7.2.1
VignetteBuilder knitr
LazyData true
R topics documented:
```

2 adjust\_Gram

adjus	st_Gram	Function kernel	n to	get	Gra	ım	ma	trix	x aj	fter	· ad	jus	ting	g of	sig	gm	a p	oar	an	ıet	er	of	a
Index																							40
	sudoku	• • • •							٠			•			•		•	•		٠		•	37
	simulation_example																						
	sampler_method																						32
	Results_toy_experim																						31
	restrict_data																						25
	read_file																						25
	plot_sudoku_2D																						23
	plot_2D_lines																						21
	plot_2D																						20
	norm_vec																						20
	MSE_sim																						19
	model																						18
	Mean_iKernel_parar																						17
	K2_ABC																						16
	iKernel																						14
	get_voronoi_feature																						14
	get_voronoi_feature																						13
	get_subset_of_featur																						12
	GET_SUBSET																						12
	get_par_best_from_s	simnet																					11
	Get_parameter																						10
	Get_MAP																						9
	get_kernel_mean_en																						9
	get_inverse_GRAM																						8
	gen_colors																						7
	Gaussian model																						6
	experiment_models																						5
	check_pkg																						5
	check_packages																						4
	check_numeric_forn																						4
	analyze_experiments	3																					- 3

# Description

Function to get Gram matrix after adjusting of sigma parameter of a kernel

# Usage

```
adjust_Gram(kernel, sigma = (2^{(1:20)}) * 0.001, x, y)
```

# Arguments

kernel	Function of kernel with parameter sigma, class from kernel lab package
sigma	numeric vector of possible values of the sigma parameter for a kernel function, by default sigma = $(2**(1:20))*1E-3$
x	Matrix of stat.sim
У	Matrix of stat.obs

analyze\_experiments 3

#### Value

adjust\_Gram function returns Gram matrix after adjusting of sigma

# **Examples**

NULL

analyze\_experiments

Function to get statistics from the results of experiments and find the best methods for each simulation case

# Description

Function to get statistics from the results of experiments and find the best methods for each simulation case

# Usage

```
analyze_experiments(DF, file_to_save = "../gplot.pdf")
```

# Arguments

DF

Data frame with results of experiments, output of experiment\_models() function

#### Value

List of statistical data with analysis of results:

- ;
- :
- ;
- :
- :
- ;
- •

# **Examples**

4 check\_packages

```
check_numeric_format Function to check DATA.FRAME
```

## **Description**

Check that DATA.FRAME has numeric format for ALL the columns and it has NO 'NA' values

## Usage

```
check_numeric_format(1)
```

## **Arguments**

1

DATA.FRAME that should have data of numeric type

#### Value

TRUE if data frame has ONLY numeric data and FALSE vice verse

#### **Examples**

```
## Not run: check_numeric_format( data.frame( A= c(9,0), B = c(4,6)) ) # TRUE check_numeric_format( data.frame( A= c(9,0), B = c(4,NA)) ) # Error due to NA value check_numeric_format( data.frame( A= c(9,0), B = c(4,6)) ) # Error due to character in the data ## End(Not run)
```

check\_packages

Check the installation of packages and attach them with corresponding functions

# Description

Check the installation of packages and attach them with corresponding functions

# Usage

```
check_packages(pkgs = NULL)
```

#### **Arguments**

pkgs

List of package names with related function names, by default (or when pkgs = NULL) the list of packages are described in Namespace file of the package or 'R/MaxWiK-package.R' file

## Value

if the packages are installed then it returns NULL else it returns error message

#### **Examples**

```
check_packages( )
```

check\_pkg 5

check\_pkg

Check the installation of a package for some functions

## **Description**

Check the installation of a package for some functions

## Usage

```
check_pkg(pkg)
```

# Arguments

pkg

Package name

## Value

if the package is installed then it returns NULL else it returns error message

## **Examples**

```
check_pkg( pkg = 'grDevices' )
```

experiment\_models

Function to prepare toy experiments

## **Description**

Function to prepare toy experiments

# Usage

```
experiment_models(
  file_name = "output.txt",
  models = c("Gaussian", "Linear"),
  dimensions = (1:20) * 2,
  stochastic_terms = c(0, 0.1, 0.3, 0.7, 1, 1.5),
  rng = c(0, 10),
  restrict_points_number = 300
)
```

## **Arguments**

```
file_name Name of file to output results

Mames of models for simulation, by default models = c('Gaussian', 'Linear')

dimensions Dimensions of models, by default dimensions = (1:20)*2

stochastic_terms

Stochastic terms for each model, by default stochastic_terms = c(0, 0.1, 0.3, 0.7, 1)

rng Range for each variable, by default rng = c(0, 10)
```

6 Gaussian\_model

#### Value

experiment\_models() returns list of results of experiments

#### **Examples**

NULL

Gaussian\_model

The model of simulations that is based on Gaussian functions for each dimension

# Description

The function Gaussian\_model() allows to generate parameters and statistics of simulations that are based on Gaussian function for each dimension:

```
f(x) = { \exp(-(x1-x01)^2/2), ..., \exp(-(xn-x0n)^2/2)} = { y1, y2, ..., yn} is a vector of output data
```

The function linear\_model() allows to generate parameters and statistics of simulations that are based on linear function for each dimension:

```
f(x) = \{1 + (x1 - x01) / x01 + noise_1, ..., 1 + (xn - x0n) / x0n + noise_n\} = \{y1, y2, ..., yn\} is a vector of output data
```

## Usage

```
Gaussian_model(
  d = 1,
  x0 = 3,
  probability = TRUE,
  n = 1000,
  r = range(0, 10),
  noise = 0
)
linear_model(
  d = 1,
  x0 = 3,
  probability = TRUE,
  noise = 0.2,
  n = 1000,
  r = range(0, 10)
)
```

# **Arguments**

d	Dimension of the parameter and model space
x0	Numeric vector with length of dimensionality of data frame, that contents the truth value of parameter. Each number in the vector should be within the range r
probability	Logical, if TRUE then apply uneven distribution for parameters generation
n	Integer number of points in data frames

gen\_colors 7

```
r Range r = c(min, max), by default r = range(0,10)
noise Noise factor, implemented as coefficient in f(x) = ... + noise * runif(1)
```

## Value

The function Gaussian\_model() returns list of two objects:

- stat.sim data frame of simulations statistics,
- par.sim data frame of parameters,
- stat.obs data frame of an observation point.

The function linear\_model() returns list of two objects:

- stat.sim data frame of simulations statistics,
- par.sim data frame of parameters,
- stat.obs data frame of an observation point.

#### **Functions**

linear\_model(): The model of simulations that is based on linear functions for each dimension

## **Examples**

NULL

NULL

gen\_colors

Function to make a large number of colors

## **Description**

Function to make a large number of colors

# Usage

```
gen\_colors(nm = 12)
```

#### **Arguments**

nm

Number of colors

#### Value

Vector of colors with length more than nm

# Examples

```
clrs = gen_colors( nm = 120 )
```

get\_inverse\_GRAM

get\_inverse\_GRAM

The function to get inverse Gram matrix

# Description

Function get\_inverse\_GRAM() allows to get inverse Gram matrix based on given positive regularization constant lambda

Function check\_positive\_definite() returns logical value about n trials on 'is Gram matrix positive definite or not?' Just incorrect trial returns FALSE

## Usage

```
get_inverse_GRAM(G, 1 = 1e-06, check_pos_def = FALSE)
check_positive_definite(G, n = 10)
```

## Arguments

G	Gram matrix gotten via GRAM_iKernel() function
1	Lambda parameter or positive regularization constant
check_pos_def	Logical parameter to check the Gram matrix is positive definite or do not check
n	Number of iterations to check the positive definite property

#### Value

Function get\_inverse\_GRAM() returns the inverse Gram matrix based on the given positive regularization constant lambda l

Function check\_positive\_definite() returns logical value: TRUE if Gram matrix is positive definite, and FALSE if it is not

#### **Functions**

• check\_positive\_definite(): The function to check the positive definite property of Gram matrix

## **Examples**

NULL

get\_kernel\_mean\_embedding

The function to calculate Maxima weighted kernel mean mapping for Isolation Kernel in RKHS related to parameters space

#### **Description**

The function to calculate Maxima weighted kernel mean mapping for Isolation Kernel in RKHS related to parameters space

#### Usage

```
get_kernel_mean_embedding(parameters_Matrix_iKernel, Hilbert_weights)
```

## **Arguments**

parameters\_Matrix\_iKernel

Matrix of all the points represented in RKHS related to parameters space

Hilbert\_weights

Maximal weights in RKHS to get related part of kernel mean embedding from parameters\_Matrix\_iKernel

#### Value

Maxima weighted kernel mean mapping in the form of integer vector with length t (number of trees). Each element of the vector is index of Voronoi cell with maximal weight in the Voronoi diagram

# **Examples**

NULL

Get\_MAP

The function to get Maximum A Posteriori from numeric data frame

## **Description**

The function Get\_MAP returns the Maximum A Posteriori (MAP) of data frame.

# Usage

Get\_MAP(DF)

#### **Arguments**

DF

Data frame of the integer or numeric numbers or characters

# Value

The function Get\_MAP returns the MAP for each dimension in data frame DF of vector

10 Get\_parameter

## **Examples**

NULL

Get\_parameter

Function to call a method to get parameter estimation and MSE for each used method

# Description

Function to call a method to get parameter estimation and MSE for each used method

# Usage

```
Get_parameter(
  method_name,
  kernel_name = "",
  stat.obs,
  stat.sim,
  par.sim,
  G = NULL,
  par.truth
)
```

## **Arguments**

```
method_name Name of a method
kernel_name Name of kernel function
stat.obs Data frame of statistics of observation point
stat.sim Data frame of statistics of simulations
par.sim Data frame of parameters
G Matrix of similarities for K2-ABC based on isolation kernel
par.truth Truth parameter value to check result of estimation
```

#### Value

```
par.truth,() returns the list:
method_name = method_name,
```

- · kernel\_name,
- model\_name,
- stochastic\_term,
- MSE,
- running\_time,
- iteration.

#### **Examples**

NULL

```
get_par_best_from_simnet
```

Function to extract all the best parameters estimation from results of the function simulation\_example\_many\_psi\_t()

#### **Description**

Function to extract all the best parameters estimation from results of the function simulation\_example\_many\_psi\_t()

## Usage

```
get_par_best_from_simnet(simnet)
get_spiderweb_from_simnet(simnet)
get_network_from_simnet(simnet)
```

#### **Arguments**

simnet

results of the function simulation\_example\_many\_psi\_t()

## Value

```
get_par_best_from_simnet() returns all the best parameters estimation
get_spiderweb_from_simnet() returns all the spiderwebs from results of the function simulation_example_many_ps
get_network_from_simnet() returns all the networks from results of the function simulation_example_many_psi_t()
```

## **Functions**

- get\_spiderweb\_from\_simnet(): Function to extract all the spiderwebs from results of the function simulation\_example\_many\_psi\_t()
- get\_network\_from\_simnet(): Function to extract all the networks from results of the function simulation\_example\_many\_psi\_t()

## **Examples**

NULL

NULL

**GET\_SUBSET** 

The function to get subset with size psi for Voronoi diagram

# Description

The function to get subset with size psi for Voronoi diagram

#### Usage

```
GET_SUBSET(data_set, pnts)
```

## **Arguments**

data\_set Data.frame of Voronoi diagram

pnts Integer vector of indexes of columns of the data\_set

#### Value

Subset of data\_set with columns pnts

# **Examples**

NULL

```
get_subset_of_feature_map
```

The function to get subset of points based on feature mapping

# Description

The function to get subset of points based on feature mapping

## Usage

```
get_subset_of_feature_map(dtst, Matrix_Voronoi, iFeature_point)
```

## **Arguments**

dtst Dataset of all the original points

Matrix\_Voronoi Matrix of Voronoi diagrams based on the Isolation Kernel algorithm

iFeature\_point Feature mapping in RKHS for a point, that can be gotten via add\_new\_point\_iKernel()

function

#### Value

The subset of dtst that has points extracted with feature mapping of an observation point (iFeature\_point)

# **Examples**

get\_voronoi\_feature 13

get_voronoi_feature	The function to get feature representation in RKHS based on Voronoi
	diagram for WHOLE dataset

# Description

The function to get feature representation in RKHS based on Voronoi diagram for WHOLE dataset

# Usage

```
get_voronoi_feature(
   psi = 40,
   t = 350,
   data,
   talkative = FALSE,
   new = TRUE,
   Matrix_Voronoi = NULL
)
add_new_point_iKernel(data, d1, Matrix_Voronoi, dissim, t, psi, nr)
```

## **Arguments**

psi	Integer number related to the size of each Voronoi diagram
t	Integer number of trees in Isolation Kernel or dimension of RKHS
data	dataset of points, rows - points, columns - dimensions of a point
talkative	logical. If TRUE then print messages, FALSE for the silent execution
new	logical. Is Matrix_Voronoi new ? If TRUE then function will calculate Matrix_Voronoi, if FALSE function will use input Matrix_Voronoi.
Matrix_Voronoi	Matrix of Voronoi diagrams that is used only if new = FALSE
d1	Data point - usually it is an observation data point
dissim	Matrix of dissimilarity or distances between all points.
nr	Integer number of rows in matrix of distances (dissim) and also the size of dataset

# Value

Feature representation in RKHS based on Voronoi diagram for WHOLE dataset RKHS mapping for a new point based on Isolation Kernel mapping

#### **Functions**

• add\_new\_point\_iKernel(): The function to get RKHS mapping based on Isolation Kernel for a new point

# **Examples**

```
NULL
NULL
```

14 iKernel

```
get_voronoi_feature_PART_dataset
```

The function to get feature representation in RKHS based on Voronoi diagram for PART of dataset

# Description

get\_voronoi\_feature\_PART\_dataset() function returns the feature (mapping) representation in RKHS based on Voronoi diagram for NEW PART of dataset. The Matrix\_Voronoi is based on the PREVIOUS dataset. The NEW PART of dataset will appear at the end of PREVIOUS dataset

#### Usage

```
get_voronoi_feature_PART_dataset(
  data,
  talkative = FALSE,
  start_row,
  Matrix_Voronoi
)
```

#### **Arguments**

data Data.frame of new points

talkative Logical parameter to print or do not print messages start\_row Row number from which a new data should be added

Matrix\_Voronoi Matrix of Voronoi diagrams based on the PREVIOUS dataset

#### Value

List of three matrices: Matrix\_Voronoi, Matrix\_iKernel and dissim

# **Examples**

NULL

iKernel	Function returns the value of similarity or Isolation KERNEL for TWO
	points

#### **Description**

iKernel() function returns value of similarity or Isolation KERNEL for TWO points that is number in the range [0,1]

iKernel\_point\_dataset() function returns vector of values of similarity based on Isolation Kernel between a new point and all the points of dataset

get\_weights\_iKernel() function returns list of two objects: the first object is numeric vector of weights for RKHS space, and the second object is numeric vector of weights of similarity for iFeature\_point corresponding observation point

GRAM\_iKernel() is the function to calculate Gram matrix for Isolation Kernel method based on Voronoi diagrams

iKernel 15

# Usage

```
iKernel(Matrix_iKernel, pnt_1, pnt_2, t)
iKernel_point_dataset(Matrix_iKernel, t, nr, iFeature_point)
get_weights_iKernel(GI, Matrix_iKernel, t, nr, iFeature_point)
GRAM_iKernel(Matrix_iKernel, check_pos_def = FALSE)
```

#### **Arguments**

Matrix_iKernel	Matrix of indexes of Voronoi cells for each point and each tree based on Isolation Kernel calculation
pnt_1	The first point of dataset
pnt_2	The second point of dataset
t	is a number of columns of Matrix_iKernel or dimension of Matrix_iKernel (corresponding to the number of trees t)
nr	is number of rows in Matrix_iKernel or size of dataset
iFeature_point	Feature mapping in RKHS for a new point, that can be gotten via $add_new_point_iKernel()$ function
GI	The inverse Gram matrix
check_pos_def	Logical parameter to check the Gram matrix is positive definite or do not check

## Value

The function iKernel() returns a value of similarity or Isolation KERNEL for TWO points

The function iKernel\_point\_dataset() returns a value of Isolation Kernel between a new point and dataset represented via Matrix\_iKernel

The function get\_weights\_iKernel() returns the list of weights for RKHS space and weights of similarity for iFeature\_point

The function GRAM\_iKernel() returns Gram matrix of Isolation Kernel

#### **Functions**

- iKernel\_point\_dataset(): The function to get Isolation Kernel between a new point and dataset
- get\_weights\_iKernel(): The function to get weights from Feature mapping
- GRAM\_iKernel(): The function to calculate Gram matrix for Isolation Kernel method

# Examples

NULL

NULL

NULL

 $K2\_ABC$ 

K2\_ABC

Function to get parameter estimation and weights using K2-ABC method

#### **Description**

K2\_ABC() function allows to get parameter estimation and weights using K2-ABC method described in the paper Mijung Park, Wittawat Jitkrittum, Dino Sejdinovic, Proceedings of the 19th International Conference on Artificial Intelligence and Statistics, PMLR 51:398-407, 2016.

adjust\_K2\_ABC() allows to adjust epsilon parameter for K2-ABC method using numeric vector of epsilon, find parameter estimation for each epsilon and choose the best one.

adjust\_K2\_ABC\_iKernel() allows to adjust epsilon parameter for K2-ABC method using numeric vector of epsilon, find parameter estimation for each epsilon and choose the best one based on matrix of isolation kernel.

adjust\_ABC\_tolerance() allows to adjust tolerance parameter for rejection ABC method using numeric vector of tolerance, find parameter estimation for each tolerance and choose the best one.

#### Usage

```
K2\_ABC(G, epsilon = 0.5, par.sim)
adjust_K2_ABC(
  epsilon = c(0.01, 0.02, 0.03, 0.04, (0.05 * 1:20)),
  par.sim,
  stat.sim,
  stat.obs,
  kernel
)
adjust_K2_ABC_iKernel(
  epsilon = c(0.01, 0.02, 0.03, 0.04, (0.05 * 1:20)),
  par.sim,
  stat.sim,
  stat.obs,
  G
)
adjust_ABC_tolerance(
  tolerance = c(0.001, 0.002, 0.005, (0.01 * 1:20)),
  par.sim,
  stat.sim,
  stat.obs
)
```

#### **Arguments**

Kernel matrix G containers similarities between simulation points and observation point based on isolation kernel
 epsilon Numeric vector of possible values of epsilon, by default epsilon = (0.05 \* 1:20)

par.sim	dataset/matrix of parameters for simulation
stat.sim	Matrix of statistics of simulations
stat.obs	Matrix of statistics of an observation
kernel	Kernel function of class kernel from kernlab package
tolerance	Vector of tolerance values for rejection ABC method to get the best one, by default tolerance = $c(0.001, 0.002, 0.005, (0.01 * 1:20)$

#### Value

K2\_ABC() returns the list of:

- 1. weights for par.sim related to observation point based on Gram matrix
- 2. parameter estimation par.est

adjust\_K2\_ABC() returns the best parameter estimation using K2-ABC method varying epsilon adjust\_K2\_ABC\_iKernel() returns the best parameter estimation using K2-ABC method varying epsilon and based on isolation kernel

adjust\_ABC\_tolerance() returns the best parameter estimation using rejection ABC method varying tolerance and tolerance value

#### **Functions**

- adjust\_K2\_ABC(): Function to adjust epsilon parameter for K2-ABC method
- adjust\_K2\_ABC\_iKernel(): Function to adjust epsilon parameter for K2-ABC method
- adjust\_ABC\_tolerance(): Function to adjust tolerance parameter for rejection ABC method

## **Examples**

NULL

NULL

NULL NULL

Mean\_iKernel\_parameters

The function returns the weighted mean of the parameter based on Isolation Kernel ABC method

## **Description**

The function Mean\_iKernel\_parameters() returns the weighted mean of the parameter that was calculated with KernelABC() function that represents Isolation Kernel ABC method

## Usage

Mean\_iKernel\_parameters(param, sm)

18 model

## **Arguments**

param Data frame of parameters

sm Numeric vector of weights gotten from iKernelABC() function

## Value

The function Mean\_iKernel\_parameters() returns the weighted mean of the parameter

## **Examples**

NULL

model

Model definition for sampler to calculate one simulation

# Description

Model definition for sampler to calculate one simulation

# Usage

```
model(name = c("Gaussian", "Linear")[1], parameter, x0, stat.obs, noise = 0)
```

# Arguments

name Name of a model, can be either 'Gaussian' or 'Linear'

parameter Value of a parameter

x0 True value of parameter

stat.obs Data frame of statistics of observation point

noise Value of stochastic term

# Value

model() returns data frame with a result of a simulation based on the model

## **Examples**

MSE\_sim

MSE_sim	The function to get the mean square error values for statistics of simulations

# Description

The function MSE\_sim() allows to get the mean square error values for statistics of simulations

The function MSE\_parameters() allows to get MSE for parameters if the truth parameter is known

# Usage

```
MSE_sim(stat.obs, stat.sim)
MSE_parameters(par.truth, par.top = NULL, par.best)
```

# Arguments

stat.obs	Summary statistics of the observation point
stat.sim	Summary statistics of the simulations (model output)
par.truth	The truth parameter
par.top	Parameters from the top of similarities of iKernelABC() algorithm
par.best	The best parameter from iKernelABC() algorithm

# Value

The function MSE\_sim() returns numeric vector of the mean square error values for statistics of simulations

The function MSE\_parameters() returns list of two numbers:

- mean of MSE values for all the points from par.top;
- MSE value for the point of par.best

#### **Functions**

• MSE\_parameters(): The function calculates mean square error (MSE) value for parameters as differences between them and already the known truth parameter

# **Examples**

 $\mathsf{NULL}$ 

20 plot\_2D

norm\_vec

The norm function for vector

## **Description**

The norm function for vector

### Usage

```
norm_vec(x)
norm_vec_sq(x)
```

## **Arguments**

Х

numeric vector

## Value

The squared root of sum of squared elements of the vector x or Euclid length of the vector x. The squared Euclid norm or the sum of squared elements of the vector x.

## **Functions**

• norm\_vec\_sq(): The squared norm or the sum of squared elements of the vector x

# **Examples**

```
norm_vec(c(3,4)) # that returns 5
norm_vec(c(12,5)) # that returns 13
norm_vec_sq(c(3,4)) # that returns 25
norm_vec_sq(c(12,5)) # that returns 169
```

plot\_2D

Function to plot 2D figure of points y = y(x)

# Description

Function to plot 2D figure of points y = y(x)

# Usage

```
plot_2D(
    x,
    y,
    names = c("X", "Y"),
    pch = 18,
    col = "blue",
    cex = 1.2,
```

plot\_2D\_lines 21

```
xr = c(-10, 10),
yr = c(-10, 10),
safe_pdf = FALSE,
filename = "./plot.pdf",
change_par = TRUE
)
```

## **Arguments**

 $\begin{array}{ccc} x & & & & & \\ & & & & \\ y & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\ & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & &$ 

names  $\hspace{1.5cm} \text{Vector of two characters with names for } X \text{ and } Y \text{ axes}$ 

pch Parameter pch for plot function

col Colors of points

cex Parameter cex for plot function

xr Range for X yr Range for Y

safe\_pdf Indicator to save plot to a file or not

filename Name of file to save plot if safe\_pdf == TRUE

change\_par Indicator to change par() or not for a plot. By default change\_par = TRUE, after

plot it will be returned to initial values

## Value

NULL, making 2D plot using points

## **Examples**

```
plot_2D(x=-5:5, y=-3:7)
```

plot\_2D\_lines

Function to plot 2D figure of lines y\_i = DF[, nl[i]]), i - index

# Description

Function to plot 2D figure of lines  $y_i = DF[, nl[i]]$ ), i - index

## Usage

```
plot_2D_lines(
    x,
    DF,
    nl = 1:2,
    names = c("X", "Y"),
    legend_names = "",
    col = c("blue3", "darkmagenta", "red", "green4", "darkorange", "steelblue1"),
    cex = 1.2,
    lwd = 2,
    lt = c(1:6),
```

22 plot\_2D\_lines

```
xr = c(-10, 10),
yr = c(-10, 10),
safe_pdf = FALSE,
filename = "./plot.pdf",
type = "l",
logscale = "",
draw_key = TRUE,
change_par = TRUE)
```

### **Arguments**

Input data for axes X Χ data.frame with data to plot DF nl indexes of columns in DF to plot Vector of two characters with names for X and Y axes names legend\_names Name of legend Vector of colors for lines col Parameter cex for plot function cex lwd Vector of width of lines Vector of types of lines lt Range for X xr Range for Y yr safe\_pdf Indicator to save plot to a file or not Name of file to save plot if safe\_pdf == TRUE filename Parameter type in plot function type logscale Parameter logscale in plot function Indicator to draw key or not draw\_key Indicator to change par() or not for a plot. By default change\_par = TRUE, after change\_par

# Value

NULL, making 2D plot using lines

### **Examples**

```
NULL
# plot_2D_lines( x = DF[, 1 ], DF, nl = 8:12 , xr = c(1,max(DF$Time) ), yr = c(0,1) )
# xr = c(1,max(DF$Time) )
# yr = c(0,max(DF[,14],DF[,16],DF[,17] ))
# plot_2D_lines( x = DF[, 1 ], DF, nl = c(14,16,17) , xr =xr, yr = yr )
# plot_2D_lines( x = DF[, 1 ], DF, nl = 18:22 , xr = c(1,max(DF$Time) ), yr = c(0,1) )
```

plot it will be returned to initial values

plot\_sudoku\_2D 23

plot\_sudoku\_2D

Function to plot all the results of the function sudoku()

# **Description**

The function plot\_sudoku\_2D draws all the results of the function sudoku()
The function plot\_web\_2D() draws all the results of the function spiderweb()

# Usage

```
plot_sudoku_2D(
  stat.sim,
  par.sim,
  par.truth,
  iKernelABC,
  rslt,
  ind_X,
  ind_Y,
  names = c("Parameter_1", "Parameter_2"),
  xlim,
  ylim,
  show_tracer = TRUE,
  show_obs = TRUE,
  show_appropriate = TRUE,
  show_best = TRUE,
  show_u_point = TRUE,
  show_legend = FALSE
plot_web_2D(
  stat.sim,
  par.sim,
  par.truth,
  iKernelABC,
  web,
  ind_X,
  ind_Y,
  names = c("P1", "P2"),
  xlim,
  show_tracer = TRUE,
  show_obs = TRUE,
  show_network = TRUE,
  show_best = TRUE,
  show_u_point = TRUE,
  show_legend = FALSE
)
```

#### **Arguments**

stat.sim Summary statistics of the simulations (model output)

24 plot\_sudoku\_2D

par.sim Data frame of parameters of the model

par.truth Truth value of the parameter corresponding to observation point (if known)

iKernelABC Result of calculations based on Isolation Kernel ABC that can be gotten by the

function iKernelABC()

rslt Results of function sudoku()

ind\_X Column index of the par.sim data frame to plot as X axes

ind\_Y Column index of the par.sim data frame to plot as Y axes

names Vector of axes names, by default names = c( 'Parameter\_1', 'Parameter\_2'

)

xlim Numeric vector of the range for X axes
ylim Numeric vector of the range for Y axes

show\_tracer Logical to show or do not show all the tracer points

show\_obs Logical to show or do not show the stat.obs or parameter of observation point

(if known)

show\_appropriate

Logical to show or do not show all the points of the object rslt\$surroundings\_best\_points

from results of sudoku() function

show\_best Logical to show or do not show the best point of the results of sudoku() function

show\_u\_point Logical to show or do not show the estimated point of parameter for an obser-

vation

show\_legend Logical to show or do not show the legend

web Results of the function spiderweb() to draw on the plot

show\_network Logical to show or do not show network points

#### Value

Plot all the results of sudoku() function

The function plot\_web\_2D() draws all the results of the function spiderweb()

#### **Functions**

• plot\_web\_2D(): The function to plot all the results of the function spiderweb()

## **Examples**

NULL

read\_file 25

read\_file

Function to read file

#### **Description**

Function to read file

## Usage

```
read_file(file_name = "", stringsAsFactors = FALSE, header = TRUE)
```

#### **Arguments**

file\_name Name of file to read stringsAsFactors

Parameter for read.table function, by default stringsAsFactors = FALSE

header Logical type to read or do not read head of a file

#### Value

data.frame of data from a file

### **Examples**

```
# fl = system.file('extdata/Input', 'gene_map.txt',package = 'tugHall.3', mustWork = TRUE )
# read_file(file_name = fl, stringsAsFactors = FALSE )
# fl = system.file('extdata/Input', 'CF.txt',package = 'tugHall.3', mustWork = TRUE )
# read_file(file_name = fl, stringsAsFactors = FALSE, header = FALSE )
NULL
```

restrict\_data

Function to get Approximate Bayesian Computation based on Maxima Weighted Isolation Kernel mapping

#### **Description**

restrict\_data() is based on rejection ABC method to restrict original dataset

The function iKernelABC() is used to get Approximate Bayesian Computation based on Maxima Weighted Isolation Kernel mapping. On given data frame of parameters, statistics of the simulations and an observation, using the internal parameters psi and t, the function iKernelABC() returns the estimation of a parameter corresponding to Maxima weighted Isolation Kernel ABC method.

The function spiderweb() itteratively generates tracer points gotten from sudoku() algorithm, based on the simple procedure:

- making a reflection of the top points from the best point,
- and then generating the point tracers between them,

• finally, the algorithm chooses again the top points and the best point (sudoku() function is used).

```
    repeat all the steps until condition to be TRUE:
    abs(max(sim_tracers) - sim_previous) < epsilon</li>
```

The function spiderweb() itteratively generates tracer points gotten from sudoku() algorithm, based on the simple procedure:

- making a reflection of the top points from the best point,
- and then generating the point tracers between them,
- finally, the algorithm chooses again the top points and the best point (sudoku() function is used),
- repeat all the steps until condition to be TRUE:
   abs(max(sim\_tracers) sim\_previous) < epsilon</li>

The function spiderweb\_slow() itteratively generates tracer points gotten from sudoku() algorithm, based on the simple procedure:

- making a reflection of the top points from the best point,
- and then generating the point tracers between them,
- finally, the algorithm chooses again the top points and the best point (sudoku() function is used).
- repeat all the steps until condition to be TRUE:
   abs(min(sim\_tracers) sim\_previous) < epsilon</li>

# Usage

```
restrict_data(par.sim, stat.sim, stat.obs, size = 300)
sampler_MaxWiK(
 stat.obs,
 stat.sim,
 par.sim,
 model,
 arg0 = list(),
  size = 500,
 psi_t,
 epsilon,
 nmax = 100,
 include_top = FALSE,
 slowly = FALSE,
  rate = 0.2
iKernelABC(
 psi = 40,
```

```
t = 350,
      param,
      stat.sim,
      stat.obs,
      talkative = FALSE,
      check_pos_def = TRUE
Get_iKernel_estimation(iKernelABC, par.sim, stat.sim, stat.obs)
adjust_psi_t(
      par.sim,
      stat.sim,
      stat.obs,
      talkative = FALSE,
      check_pos_def = FALSE,
      n_best = 10,
    psi_t = data.frame(psi = as.numeric(sapply(X = c(2:8) * 2, FUN = function(x) rep(x, FUN = func
             8))), t = rep(c(4, 6, 8, 10, 12, 14, 16, 20), 7)),
      cores = 4
)
spiderweb_old(
      psi = 4,
       t = 35,
      param = param,
      stat.sim = stat.sim,
      stat.obs = stat.obs,
       talkative = FALSE,
      check_pos_def = FALSE,
      n_bullets = 5,
      n_best = 10,
      halfwidth = 0.5,
      epsilon = 0.001
spiderweb(
      psi = 4,
      t = 35,
      param = param,
      stat.sim = stat.sim,
      stat.obs = stat.obs,
      talkative = FALSE,
      check_pos_def = FALSE,
      n_bullets = 16,
      n_best = 10,
      halfwidth = 0.5,
      epsilon = 0.001,
      rate = 0.1,
      max_iteration = 5,
      save\_web = TRUE
)
```

```
spiderweb_slow(
  psi = 4,
  t = 35,
  param = param,
  stat.sim = stat.sim,
  stat.obs = stat.obs,
  talkative = FALSE,
  check_pos_def = FALSE,
  n_bullets = 16,
  n_best = 10,
  halfwidth = 0.5,
  epsilon = 0.001,
  rate = 0.1,
  max_iteration = 15,
  save\_web = TRUE
)
```

# **Arguments**

par.sim	Data frame of parameters
stat.sim	Summary statistics of the simulations (model output)
stat.obs	Summary statistics of the observation point
size	Number of point to restrict original dataset
model	is a function to get output of simulation during sampling
arg0	is a list with arguments for a model function, so that arg0 is NOT changed during sampling
psi_t	<pre>Initial data.frame of psi and t, by default psi_t = data.frame(psi = as.numeric(sapply(X = c(2:8)*2, FUN = function( x) rep(x, 8)), t = rep(c(4,6,8,10,12,14,16,20), 7))</pre>
epsilon	Criterion to stop algorithm spiderweb() that isused to check: if (abs(max(sim_tracers) - sim_previous) < epsilon) break
nmax	is maximal number of iterations
include_top	Logical to include top points from spider_web() function to simulate or do not
slowly	Logical for two algorithms: slow and fast seekers in sampling
rate	Numeric rate from 0 to 1 that gives rate of changing of surround points of proposed max of similarity or part of changing of network during meta-sampling
psi	Integer number. Size of each Voronoi diagram or number of areas/points in the Voronoi diagrams
t	Integer number of trees in the Isolation Forest
param	or par.sim - data frame of parameters of the model
talkative	Logical parameter to print or do not print messages
check_pos_def	Logical parameter to check the Gram matrix is positive definite or do not check
iKernelABC	Result of function iKernelABC
n_best	Integer number of the best tracer bullets / points to consider them at the next algorithmic step
cores	Number of available cores for parallel computing

n\_bullets Integer number of tracer bullets / additional points between the TWO most dis-

tant points

halfwidth Criterion to choose the best tracer points like:

if similarity\_of\_point >= halfwidth then it is the point to be included to

the poool of the best points

max\_iteration Maximal number of iteration in the function

save\_web Logical to save or do not save network during meta-sampling

#### Value

restrict\_data() returns the list of:

par.sim - restricted parameters which are close to observation point

stat.sim - restricted stat.sim which are close to observation point

sampler\_MaxWiK() returns the list:

results - results of simulations;

best - the best value of parameter;

MSE\_min - minimum of MSE;

number\_of\_iterations - number of iterations;

time - time of sampling in seconds.

The function iKernelABC() returns the list of:

• kernel\_mean\_embedding is a maxima weighted kernel mean embedding (mapping) related to the observation point;

- parameters\_Matrix\_Voronoi is a matrix of information about Voronoi trees (rows trees, columns Voronoi points/areas IDs) for parameters data set;
- parameters\_Matrix\_iKernel is a matrix of of all points of PARAMETERS in a Hilbert space (rows points, columns isolation trees);
- Hilbert\_weights is a weights in Hilbert space to get maxima weighted kernel mean embedding for parameters\_Matrix\_iKernel;
- Matrix\_iKernel is a matrix of all points of simulations in a Hilbert space (rows points, columns isolation trees);
- iFeature point is a feature embedding mapping for the OBSERVATION point;
- similarity is a vector of similarities between the simulation points and observation point;
- Matrix\_Voronoi is a matrix of information about Voronoi trees (rows trees, columns Voronoi points/areas IDs);
- t is a number of trees in the Isolation Forest;
- psi is a number of areas/points in the Voronoi diagrams

Get\_iKernel\_estimation() returns list of:

- iKernel\_ABC parameter estimation based on isolation kernel / weighted sum;
- K2\_ABC\_iKernel parameter estimation based on K2-ABC method with matrix of isolation kernel.

adjust\_psi\_t() returns adjusted hyper parameters psi and t as a data.frame with set of pair psi\_t

The function spiderweb() returns the list of the next objects:

- input.parameters the list of all the input parameters for Isolation Kernel ABC method;
- par.best that is data frame of one point that is the best from all the generated tracer points;
- par.top that is data frame of n\_best points that are the top from all the generated tracer points;
- sim.top that is numeric vecor of similarities of the top points;
- sim.best that is numeric value of the similarity of the best tracer point; tracers\_all that is data frame of all the generated tracer points;
- sim.tracers all that is numeric vector of similarities of all the generated tacer points;
- iKernelABC that is result of the function iKernelABC() given on input parameters.

The function spiderweb() returns the list of the next objects:

- input parameters that is the list of all the input parameters for Isolation Kernel ABC method;
- iteration that is iteration value when algorithm stopped;
- network that is network points when algorithm stopped;
- par.best that is data frame of one point that is the best from all the generated tracer points;
- sim.best that is numeric value of the similarity of the best tracer point;
- iKernelABC that is result of the function iKernelABC() given on input parameters;
- spiderweb that is the list of all the networks during the meta-sampling.

The function spiderweb() returns the list of the next objects:

- input.parameters that is the list of all the input parameters for Isolation Kernel ABC method;
- iteration that is iteration value when algorithm stopped;
- network that is network points when algorithm stopped;
- par.best that is data frame of one point that is the best from all the generated tracer points;
- sim.best that is numeric value of the similarity of the best tracer point;
- iKernelABC that is result of the function iKernelABC() given on input parameters;
- spiderweb that is the list of all the networks during the meta-sampling.

#### **Functions**

- restrict\_data(): Function to restrict data in the size to accelerate the calculations
- sampler\_MaxWiK(): Function to generate parameters and simulate a model based on MaxWiK algorithm
- Get\_iKernel\_estimation(): function to get parameter estimation based on isolation kernel
- adjust\_psi\_t(): Function to adjust hyper parameters psi and t for isolation kernel ABC
- spiderweb\_old(): The function to get the best value of parameter corresponding to Maxima Weighted Isolation Kernel mapping which is related to an observation point
- spiderweb(): The function to get the best value of parameter corresponding to Maxima Weighted Isolation Kernel mapping which is related to an observation point
- spiderweb\_slow(): The function to get the best value of parameter corresponding to Maxima Weighted Isolation Kernel mapping which is related to an observation point

#### **Examples**

 $\mathsf{NULL}$ 

NULL

NULL

NULL NULL

NULL

NULL

NULL

Results\_toy\_experiments

Data frame with results of function experiment\_models()

# Description

```
A dataset containing results of function experiment_models() with next input:

Results_toy_experiments = experiment_models(file_name = '../Results_ALL.txt',

models = c( 'Gaussian', 'Linear'),

dimensions = (1:10)*2,

stochastic_terms = c(0, 1, 5, 10, 20, 30),

rng = c(0,10),

restrict_points_number = 300))

Please, pay attention it will take 4-6 hours for 4 cores.

To analyze these data, please, use:

RES_methods = analyze_experiments(Results_toy_experiments, file_to_save = '../ggplot.pdf')

that gives the best methods for each case and statistical data of simulations
```

# Usage

 ${\tt Results\_toy\_experiments}$ 

#### **Format**

A data frame with 12960 rows and 8 variables:

method\_name Name of a method for calculation

kernel\_name Name of using kerel or "if not applicapable

model\_name Name of a model, can be 'Gaussian' or 'Linear'

dimension Dimension of the toy task

stochastic\_term Stochastic term in a function of a model

MSE Mean square error

running\_time Running time in seconds

iteration Iteration number

32 sampler\_method

sampler\_method

Function to call a method to get MSE

# Description

Function to call a method to get MSE

# Usage

```
sampler_method(
  stat.obs,
  stat.sim,
  par.sim,
  model,
  method_name,
  kernel_name,
  arg0 = list(),
  size = 500,
  nmax = 30,
  G,
  model_name,
  dimension,
  stochastic_term,
  par.truth
sampler_all_methods(
  model_name,
  dimension,
  stochastic_term,
  stat.obs,
  stat.sim,
  par.sim,
  G,
  par.truth,
  cores = 4,
  nmax
)
Get_call(
  method_name,
  kernel_name = "",
  model_name,
  dimension,
  stochastic_term,
  iteration,
  stat.obs,
  stat.sim,
  par.sim,
  G = NULL,
  par.truth
```

sampler\_method 33

```
)
Get_call_all_methods(
  model_name,
  dimension,
  stochastic_term,
  iterations,
  stat.obs,
  stat.sim,
  par.sim,
  G,
  par.truth,
  cores = 4
)
experiment_samplers(
  file_name = "./output.txt",
  model_name = "Gaussian",
  dimension = 6,
  stochastic_term = 5,
  rng = c(0, 10),
  restrict_points_number = 500,
  nmax = 30
)
```

#### **Arguments**

stat.obs Data frame of statistics of observation point stat.sim Data frame of statistics of simulations

par.sim Data frame of parameters

model is a function to get output of simulation during sampling

method\_name Name of a method kernel\_name Name of kernel function

arg0 is a list with arguments for a model function, so that arg0 is NOT changed during

sampling

size Number of point to restrict original dataset

nmax is maximal number of iterations

G Matrix of similarities for K2-ABC based on isolation kernel

model\_name Name of a model

dimension Dimension of the model

stochastic\_term

A number (usually in the range [0,1]) of stochastic term in the dataset stat.sim

par.truth Truth parameter value to check result of estimation cores Number of cores for parallel calculation with iterations

iteration Iteration number of trial with the same model and other parameters

file\_name File to save results

rng Range of points for each dimension, by default rng = range(0, 10)

restrict\_points\_number

Number of points which will be used in each method and that are close to observation point

34 sampler\_method

#### Value

```
sampler_method() returns the list:
results - results of simulations;
best - the best value of parameter;
MSE_min - minimum of MSE;
number_of_iterations - number of iterations;
time - time of sampling in seconds.
sampler_all_methods() returns data.frame with MSE for all defined methods
Get_call() returns the list:
method_name = method_name,
```

- · kernel\_name,
- model\_name,
- · stochastic\_term,
- MSE,
- running\_time,
- iteration.

Get\_call\_all\_methods() returns data.frame with MSE for all defined methods experiment\_samplers() returns data frame with results of experiment for sampling using all the methods

#### **Functions**

- sampler\_method(): Function to generate parameters and simulate a model based on MaxWiK algorithm
- sampler\_all\_methods(): Function to call all the methods to get estimation of parameter and MSE
- Get\_call\_all\_methods(): Function to call all the methods to get estimation of parameter and MSE
- experiment\_samplers(): Make experiments with sampling for all the methods and one case of toy model and dimension

## **Examples**

 $\mathsf{NULL}$ 

NULL

NULL

 $\mathsf{NULL}$ 

simulation\_example 35

simulation\_example

Example of simulation for lazy start

## **Description**

Example of simulation for lazy start

## Usage

```
simulation_example(
  verbose = TRUE,
  to_plot = TRUE,
  seed = NA,
  model = c("Gaussian", "linear")[2],
  d = 2,
  x0 = c(3, 4),
  probability = TRUE,
  n = 1000,
  r = range(0, 10),
  psi = 8,
  t = 8,
  restrict_points_number = 300
simulation_example_many_psi_t(
  verbose = TRUE,
  to_plot = TRUE,
  seed = NA,
  model = c("Gaussian", "linear")[2],
  d = 2,
  x0 = c(3, 4),
  probability = TRUE,
  n = 1000,
  r = range(0, 10),
 psi_t = data.frame(psi = c(4, 4, 8, 8, 8, 8, 10, 10), t = c(8, 20, 6, 8, 16, 20, 6, 8, 10, 10)
  restrict_points_number = 300,
  cores = 4
get_Spider_MAP(
  stat.sim,
  par.sim,
  stat.obs,
  restrict_points_number = 300,
  cores = 4,
  n_best = 8
plot_3d_similarities(sim, r = range(0, 10), n = 12)
```

36 simulation\_example

```
plot_3d_net_similarities(simnet, r = range(0, 10), n = 20)
```

# **Arguments**

verbose Logical type to show or do not show messages during execution to\_plot Logical type to plot or do not plot graphical results of a simulation

seed Numeric type to set seed for a simulation, if seed = NA (by default) then it will

be skipped

Mame of the toy model, can be 'Gaussian' or 'linear' only

d Integer number of dimension of the model

x0 Truth value of parameter corresponding to observation point

probability Logical to apply the probabilistic distribution to input data generation

Integer number of points for each axes to get net for plotly 3D graph

r Range of parameters to plot, by default r = range(0, 10)

psi Integer number. Size of each Voronoi diagram or number of areas/points in the

Voronoi diagrams

t Integer number of trees in the Isolation Forest

restrict\_points\_number

Maximal number of points in the data sets to get MAP

psi\_t Data.frame with different set of psi and t hyperparameters

cores Number of cores for parallel calculation

stat.sim Summary statistics of the simulations (model output)

par.sim • data frame of parameters of the model stat.obs Summary statistics of the observation point

n\_best Number of best psi\_t pairs adjusted for MaxWiK algorithm

sim Results of the function simulation\_example

simnet Results of the function simulation\_example\_many\_psi\_t

### Value

List of results of simulation with default values for all the parameters

List of results of simulation with default values for all the parameters

Maximum A Posteriori of meta-sampling distribution of parameters

Plot of 3D to show the similarity of each point of the parameter space

Many 3D plots to show the similarity of each point of the parameter space for each set of hyperparameters psi and t

#### **Functions**

- simulation\_example\_many\_psi\_t(): Example of simulation for lazy start and different psi / t hyperparameters
- get\_Spider\_MAP(): Function to get MAP of SpiderWeb algorithm based on different psi / t hyperparameters
- plot\_3d\_similarities(): Function to plot whole space of parameters related to similarity of the observation point:
- plot\_3d\_net\_similarities(): Function to plot whole space of parameters related to similarity of the observation point for each set of hyperparameters psi and t

sudoku 37

#### **Examples**

```
NULL
# it takes a time for a simulation and then it will demonstrates results, \cr
# so, please, wait for a while
sim = simulation_example( verbose = FALSE , to_plot = FALSE )
NULL
# it takes a time for a simulation and then it will demonstrates results, \cr
# so, please, wait for a while
sim = simulation_example_many_psi_t( verbose = FALSE , to_plot = FALSE )
NULL
# it takes a time for a simulation and then it will demonstrates results, \cr
# so, please, wait for a while
sim = simulation_example_many_psi_t( verbose = FALSE , to_plot = FALSE )
NULL
NULL
NULL
```

sudoku

The function to get the best tracer bullets related to kernel mean embedding

#### **Description**

The function sudoku() allows to get the best tracer bullets related to kernel mean embedding. The calculation performs ONLY for parameters dataset DT = par.sim. This function performs a heuristic algorithm to seek a space/area related to the feature mapping in Hilbert space for the dataset of the parameters.

The main idea of the algorithm is just:

- 1. Generate points between the centers of Voronoi diagrams related to the Maxima weighted feature mapping based on Isolation Kernel
- 2. Following strategy to puzzle out of SUDOKU: delete all points that do not match feature mapping
- 3. Output: The remaining points should be corresponding to the feature mapping.

The function get\_pairs\_of\_data\_frame() is used to get pairs of points from the Data Frame that is the most distant each other. In other words, the algorithm seeks the most distant coupled point to each point from the data frame

The function generate\_points\_between\_two\_points() is used to generate points between two given points

The function get\_tracer\_bullets() is used to to get 'tracer bullets' or tracer points generated between all the pairs of the most distant points

## Usage

```
sudoku(DT, iKernelABC, n_bullets = 20, n_best = 10, halfwidth = 0.5)
get_pairs_of_data_frame(DF)
```

38 sudoku

```
generate_points_between_two_points(pair, n = 10)
get_tracer_bullets(DF, n_bullets = 20)
```

# Arguments

DT	Whole dataset of parameters
iKernelABC	Result of calculations based on Isolation Kernel ABC that can be gotten by the function $iKernelABC()$
n_bullets	Integer number of tracer points between each pair of points from DF
n_best	Integer number of the best tracer bullets / points to consider them at the next algorithmic step
halfwidth	Criterion to choose the best tracer points like: if similarity_of_point >= halfwidth then it is the point to be included to the pool of the best points
DF	Data frame of oints that is used for generation of tracer points, so it is usually a subset of points corresponding to Voronoi sites/seeds
pair	Data frame of two points
n	Integer number of points that should be located between two input points

#### Value

The function sudoku() returns the list of next objects:

- tracer\_bullets that is all the points generated during the run of the algorithm,
- criterion that is a value of the similarity that is used to choose the best tracer points,
- best\_tracer\_bullets that is the best tracer points that have similarity more or equal than criterion value,
- surroundings\_best\_points that is the best tracer points that have similarity more or equal than halfwidth value,
- feature\_tracers that is results of the function get\_voronoi\_feature\_PART\_dataset() applied to the new tracer points,
- similarity\_to\_mean that is numeric vector of similarities of all the tracers points.

The function get\_pairs\_of\_data\_frame() returns the list of the pairs of points

The function generate\_points\_between\_two\_points() returns data frame of generated points between two given points, including given points as the first and the last rows

The function get\_tracer\_bullets() returns data frame of generated tracer points

## **Functions**

- get\_pairs\_of\_data\_frame(): The function to get pairs from Data Frame
- generate\_points\_between\_two\_points(): The function to generate points between the pair of given points
- get\_tracer\_bullets(): The function to get 'tracer bullets' or tracer points

sudoku 39

# Examples

NULL

NULL

NULL

# Index

* datasets	<pre>get_voronoi_feature, 13</pre>
Results_toy_experiments, 31	<pre>get_voronoi_feature_PART_dataset, 14</pre>
	<pre>get_weights_iKernel(iKernel), 14</pre>
add_new_point_iKernel	GRAM_iKernel (iKernel), 14
(get_voronoi_feature), 13	
adjust_ABC_tolerance(K2_ABC), 16	iKernel, 14
adjust_Gram, 2	<pre>iKernel_point_dataset(iKernel), 14</pre>
adjust_K2_ABC (K2_ABC), 16	iKernelABC (restrict_data), 25
adjust_K2_ABC_iKernel (K2_ABC), 16	
<pre>adjust_psi_t (restrict_data), 25</pre>	K2_ABC, 16
analyze_experiments, 3	linear model (Coursian model) 6
	linear_model(Gaussian_model),6
<pre>check_numeric_format, 4</pre>	Mean_iKernel_parameters,17
check_packages, 4	model, 18
check_pkg, 5	MSE_parameters (MSE_sim), 19
<pre>check_positive_definite</pre>	MSE_sim, 19
(get_inverse_GRAM), 8	1102_31111, 17
	norm_vec, 20
<pre>experiment_models, 5</pre>	norm_vec_sq (norm_vec), 20
experiment_samplers (sampler_method), 32	//
	plot_2D, 20
Gaussian_model, 6	plot_2D_lines, 21
gen_colors, 7	plot_3d_net_similarities
<pre>generate_points_between_two_points</pre>	(simulation_example), 35
(sudoku), 37	plot_3d_similarities
<pre>Get_call (sampler_method), 32</pre>	(simulation_example), 35
<pre>Get_call_all_methods (sampler_method),</pre>	plot_sudoku_2D, 23
32	plot_web_2D (plot_sudoku_2D), 23
<pre>Get_iKernel_estimation (restrict_data),</pre>	
25	read_file, 25
<pre>get_inverse_GRAM, 8</pre>	restrict_data, 25
<pre>get_kernel_mean_embedding, 9</pre>	Results_toy_experiments, 31
Get_MAP, 9	
<pre>get_network_from_simnet</pre>	<pre>sampler_all_methods (sampler_method), 32</pre>
(get_par_best_from_simnet), 11	sampler_MaxWiK (restrict_data), 25
<pre>get_pairs_of_data_frame (sudoku), 37</pre>	sampler_method, 32
<pre>get_par_best_from_simnet, 11</pre>	simulation_example, 35
Get_parameter, 10	simulation_example_many_psi_t
<pre>get_Spider_MAP (simulation_example), 35</pre>	(simulation_example), 35
<pre>get_spiderweb_from_simnet</pre>	spiderweb (restrict_data), 25
(get_par_best_from_simnet), 11	spiderweb_old(restrict_data), 25
GET_SUBSET, 12	spiderweb_slow(restrict_data), 25
<pre>get_subset_of_feature_map, 12</pre>	sudoku, 37
<pre>get_tracer_bullets (sudoku), 37</pre>	