

```
In [4]: from chemostat_report import *
from citrate import *
```

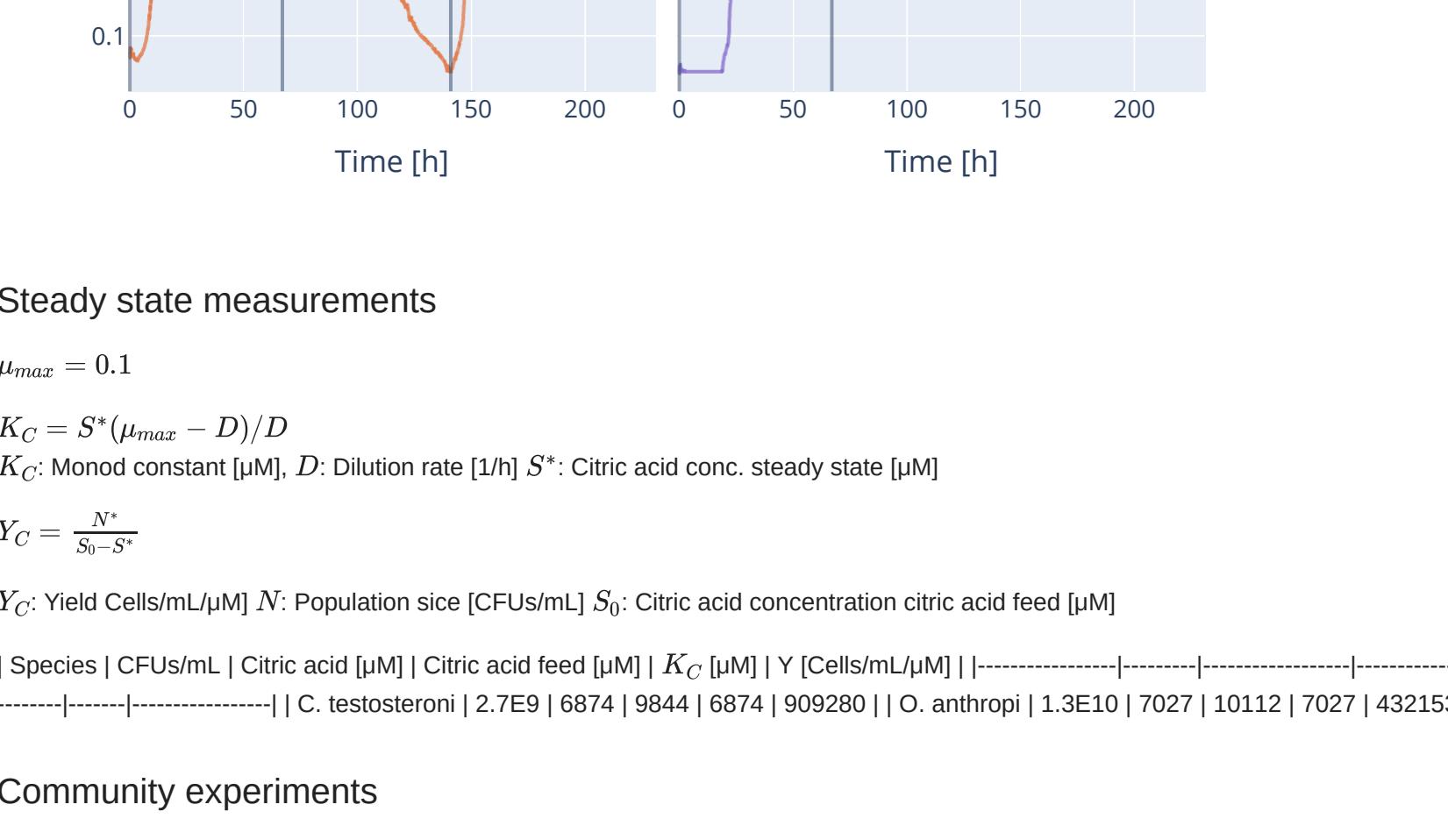
## Labmeeting 04.19.2023

### Citric acid Chemostat experiments

#### Mono-cutlure experiments

Mono culture experiments with 10 mM citric acid.

```
In [2]: fig = ct_oa()
fig.show()
#D: Dilution rate [1/h]
```



#### Steady state measurements

$$\mu_{max} = 0.1$$

$$K_C = S^*(\mu_{max} - D)/D$$

$K_C$ : Monod constant [ $\mu\text{M}$ ],  $D$ : Dilution rate [1/h]  $S^*$ : Citric acid conc. steady state [ $\mu\text{M}$ ]

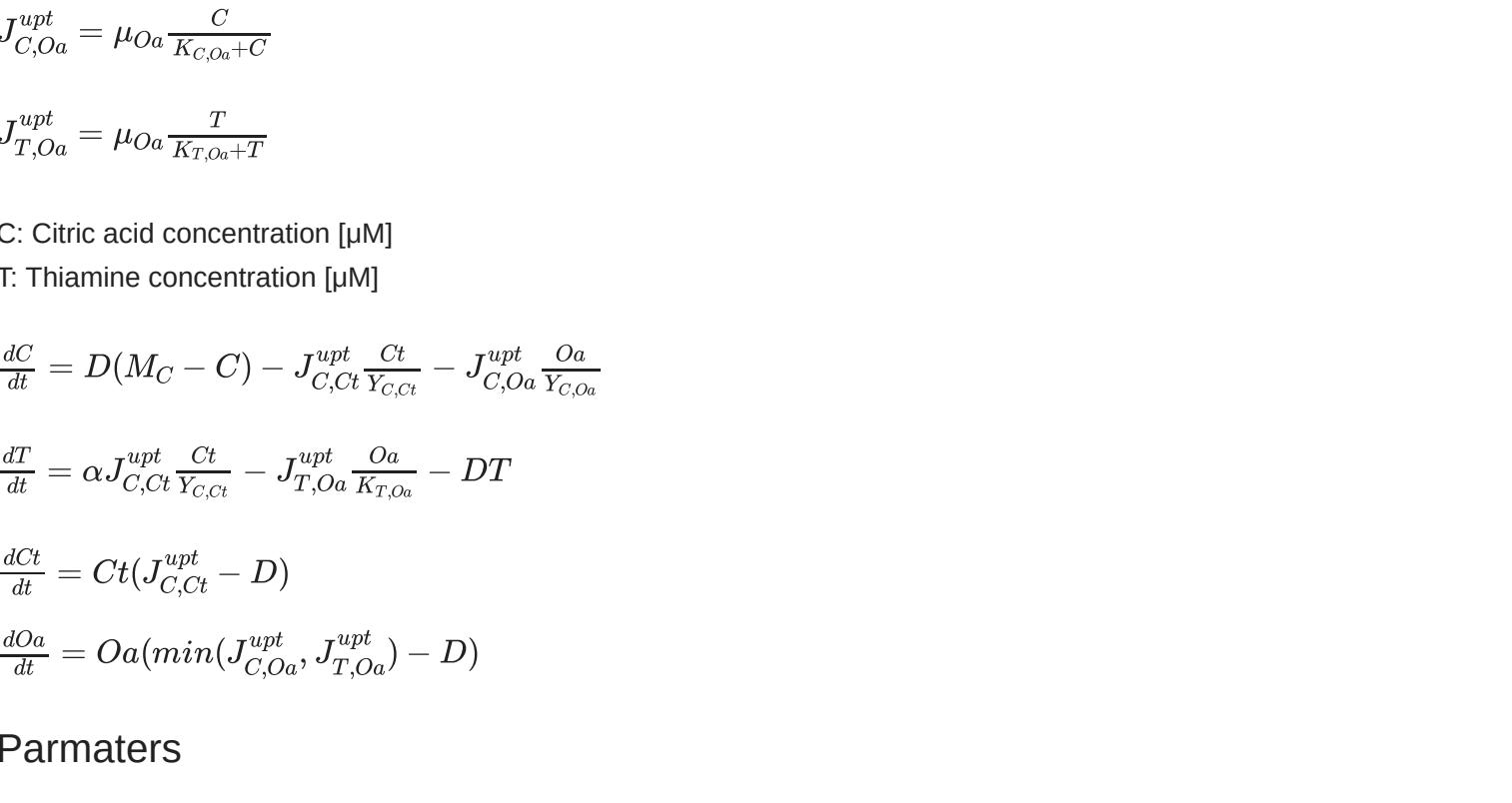
$$Y_C = \frac{N^*}{S_0 - S^*}$$

$Y_C$ : Yield Cells/mL/ $\mu\text{M}$   $N$ : Population size [CFUs/mL]  $S_0$ : Citric acid concentration citric acid feed [ $\mu\text{M}$ ]

| Species | CFUs/mL | Citric acid [ $\mu\text{M}$ ] | Citric acid feed [ $\mu\text{M}$ ] |  $K_C$  [ $\mu\text{M}$ ] |  $Y$  [Cells/mL/ $\mu\text{M}$ ] | ----- | ----- | ----- | ----- |  
----- | ----- | ----- | C. testosteroni | 2.7E9 | 6874 | 9844 | 6874 | 909280 | O. anthropi | 1.3E10 | 7027 | 10112 | 7027 | 4321535 |

#### Community experiments

```
In [11]: od_citric_acid_comm()
```



#### Species abundance

D=0.1

| Species | CFUs/mL | Relative abundance | ----- | ----- | C. testosteroni | 2.5E9 | 0.45 | O. anthropi | 3.1E9 | 0.55 |

D=0.15

| Species | CFUs/mL | Relative abundance | ----- | C. testosteroni | 3E9 | 0.75 | O. anthropi | 1E9 | 0.25 |

#### Modelling

$$J_{C,Ct}^{upt} = \mu_{Ct} \frac{C}{K_{C,Ct} + C}$$

$$J_{C,Oa}^{upt} = \mu_{Oa} \frac{C}{K_{C,Oa} + C}$$

$$J_{T,Oa}^{upt} = \mu_{Oa} \frac{T}{K_{T,Oa} + T}$$

C: Citric acid concentration [ $\mu\text{M}$ ]

T: Thiamine concentration [ $\mu\text{M}$ ]

$$\frac{dC}{dt} = D(M_C - C) - J_{C,Ct}^{upt} \frac{Ct}{Y_{C,Ct}} - J_{C,Oa}^{upt} \frac{Oa}{Y_{C,Oa}}$$

$$\frac{dT}{dt} = \alpha J_{C,Ct}^{upt} \frac{Ct}{Y_{C,Ct}} - J_{T,Oa}^{upt} \frac{Oa}{Y_{T,Oa}} - DT$$

$$\frac{dCt}{dt} = Ct(J_{C,Ct}^{upt} - D)$$

$$\frac{dOa}{dt} = Oa(\min(J_{C,Oa}^{upt}, J_{T,Oa}^{upt}) - D)$$

#### Paramters

$K_{C,Ct} = 6874$  [ $\mu\text{M}$ ] Measured

$K_{C,Oa} = 7027$  [ $\mu\text{M}$ ] Measured

$K_{T,Oa} = 0.015$  [ $\mu\text{M}$ ] Based on literature

$r_{C,Ct} = 0.3$  [1/h] Estimated

$r_{C,Oa} = 0.32$  [1/h] Estimated

$Y_{C,Ct} = 909280$  [Cells/mL/ $\mu\text{M}$ ] Measured

$Y_{C,Oa} = 4321535$  [Cells/mL/ $\mu\text{M}$ ] Measured

$Y_{T,Oa} = 1E15$  [Cells/mL/ $\mu\text{M}$ ] Based on literature

$\alpha = 5E - 6$  Estimated

#### Constant Thiamine

$$\frac{dT}{dt} = D(M_T - T) - J_{T,Oa}^{upt} \frac{Oa}{Y_{T,Oa}}$$

```
In [12]: constant_thiamine()
# D=0.1 [1/h]
```



#### Thiamine cross-feeding

$$\frac{dT}{dt} = \alpha J_{C,Ct}^{upt} \frac{Ct}{Y_{C,Ct}} - J_{T,Oa}^{upt} \frac{Oa}{Y_{T,Oa}} - DT$$

```
In [13]: # D=0.1
fig,fig_T,fig_C,y = thiamine_cross_feeding(0.1,range(400))
```



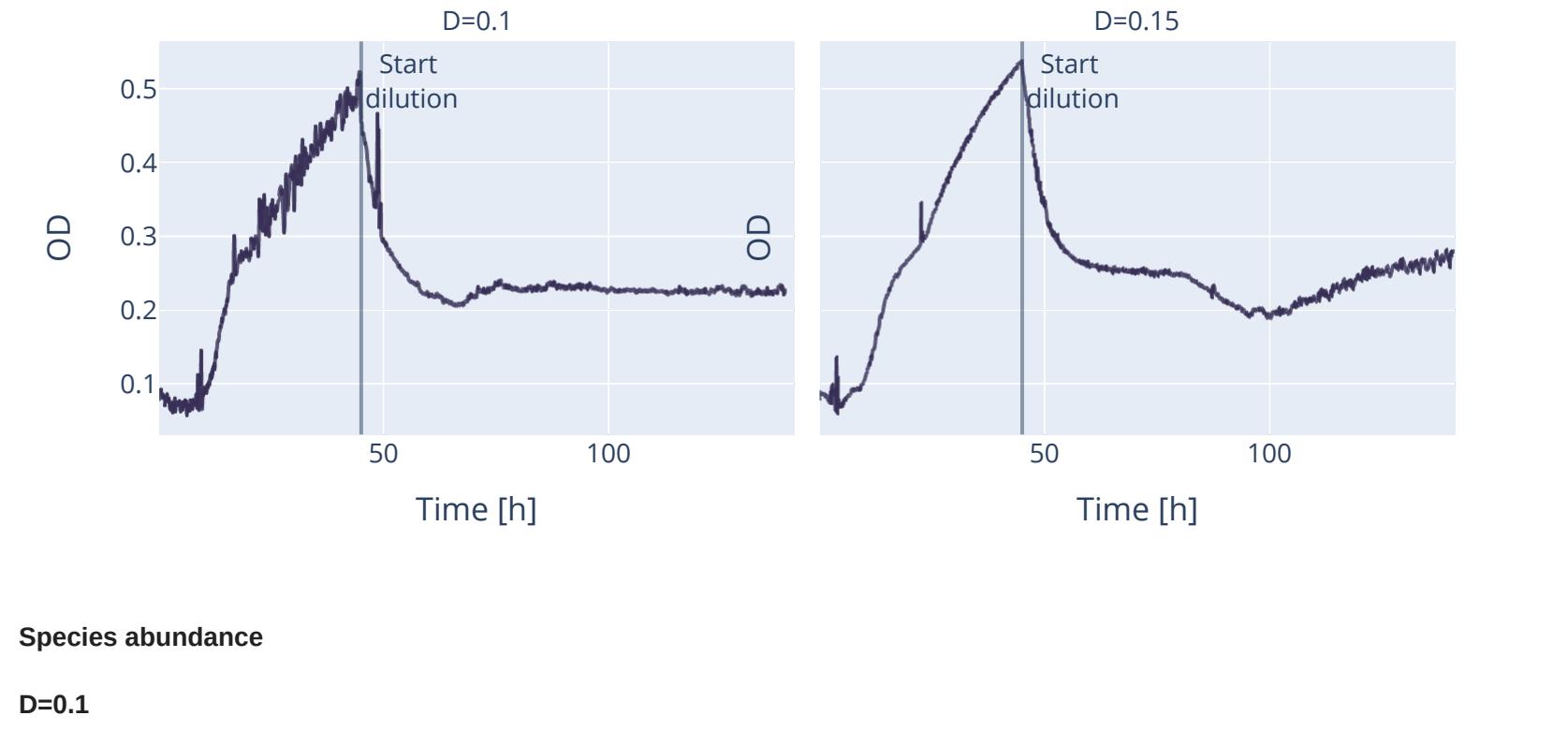
#### Thiamine cross-feeding

$$\frac{dT}{dt} = \alpha J_{C,Ct}^{upt} \frac{Ct}{Y_{C,Ct}} - J_{T,Oa}^{upt} \frac{Oa}{Y_{T,Oa}} - DT$$

```
In [14]: #fig_T.show()
```

```
#D=0.15
```

```
fig,fig_T,fig_C,y = thiamine_cross_feeding(0.15,range(400))
```

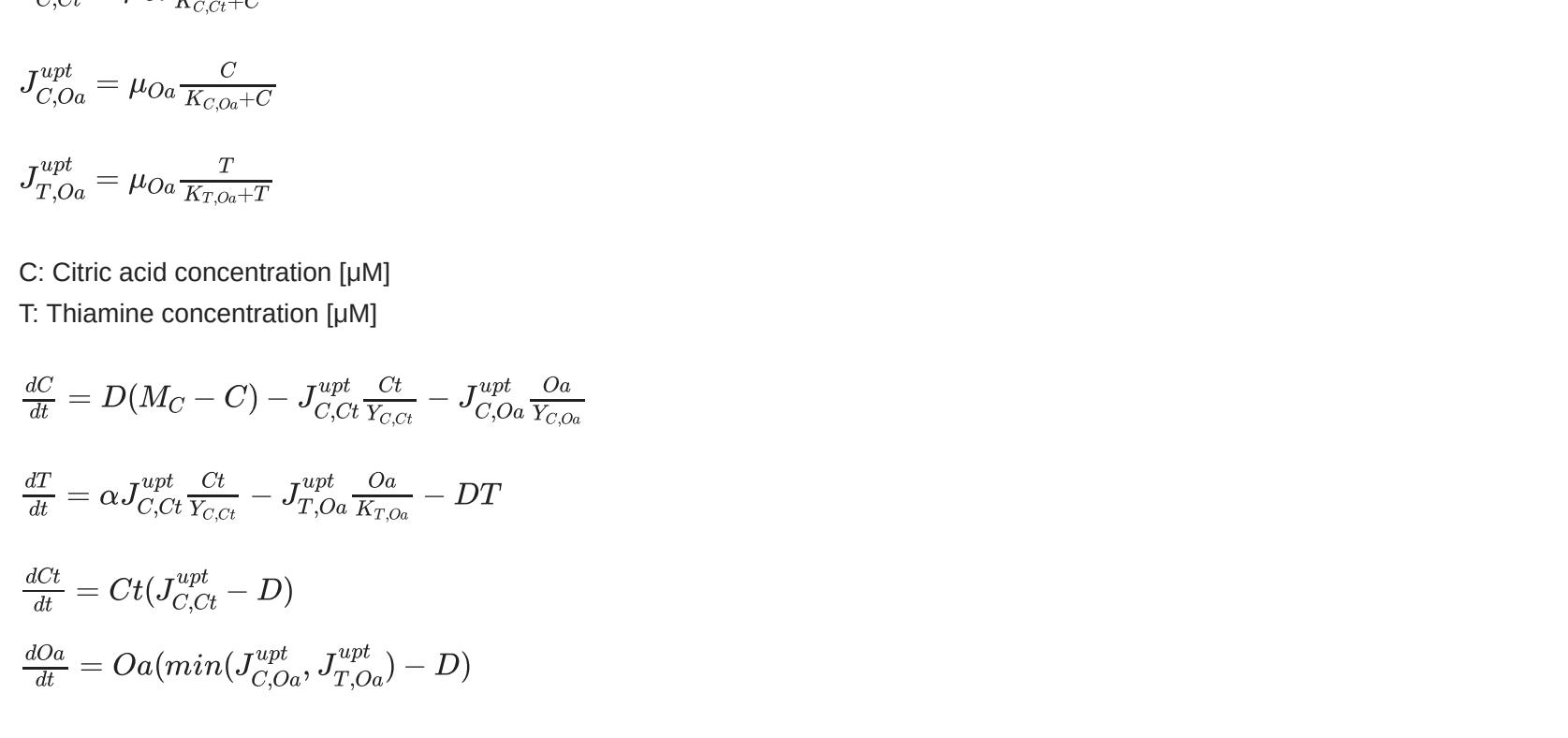


#### Thiamine cross-feeding

$$\frac{dT}{dt} = \alpha J_{C,Ct}^{upt} \frac{Ct}{Y_{C,Ct}} - J_{T,Oa}^{upt} \frac{Oa}{Y_{T,Oa}} - DT$$

```
In [15]: #D=0.15
```

```
fig,fig_T,fig_C,y = thiamine_cross_feeding(0.15,range(400))
```



#### Thiamine cross-feeding

$$\frac{dT}{dt} = \alpha J_{C,Ct}^{upt} \frac{Ct}{Y_{C,Ct}} - J_{T,Oa}^{upt} \frac{Oa}{Y_{T,Oa}} - DT$$

```
In [16]: #fig_T.show()
```

```
#D=0.15
```

```
fig,fig_T,fig_C,y = thiamine_cross_feeding(0.15,range(400))
```



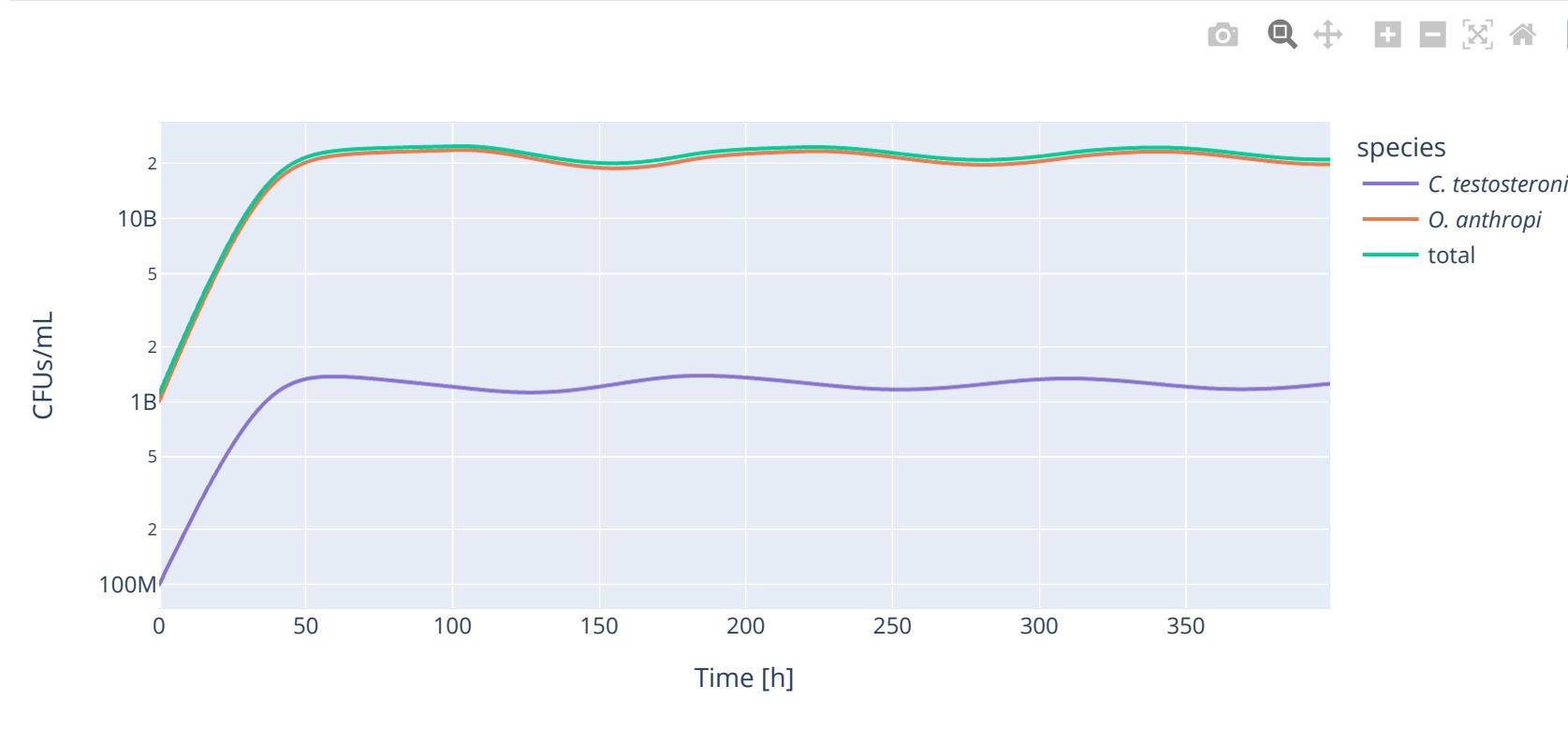
#### Thiamine cross-feeding

$$\frac{dT}{dt} = \alpha J_{C,Ct}^{upt} \frac{Ct}{Y_{C,Ct}} - J_{T,Oa}^{upt} \frac{Oa}{Y_{T,Oa}} - DT$$

```
In [17]: #fig_T.show()
```

```
#D=0.15
```

```
fig,fig_T,fig_C,y = thiamine_cross_feeding(0.15,range(400))
```



#### Thiamine cross-feeding

$$\frac{dT}{dt} = \alpha J_{C,Ct}^{upt} \frac{Ct}{Y_{C,Ct}} - J_{T,Oa}^{upt} \frac{Oa}{Y_{T,Oa}} - DT$$

```
In [18]: #fig_T.show()
```

```
#D=0.15
```

```
fig,fig_T,fig_C,y = thiamine_cross_feeding(0.15,range(400))
```

