

# Assignment 2 Notebook

Prateek Naharia

## RocketFuel

**Remember to write out your answers in words, don't just output R statistics.**

### 1.1 What is the ATE hat of the ads on conversion?

Test Group = Receiving advertisements Control Group = Not receiving advertisements  
ATE hat, after splitting the data set in test & control, we subtract the mean of both the groups( $\text{test}==0$  &  $\text{test}==1$ ) for 'converted'.

```
data_test <- ads_data[test == 1]
data_control <- ads_data[test == 0]
mean_converted_test <- mean(data_test$converted)
mean_converted_control <- mean(data_control$converted)
ATE_hat <- mean_converted_test - mean_converted_control
ATE_hat
```

```
[1] 0.007690025
```

Obtained ATE hat is 0.007690025.

### 1.2 Did the campaign cause more purchases? Is this difference statistically significant?

Hint: Use the `t.test` function. For example, the code below conducts a t-test on the number of impressions. The p-value is .8274 and 95% CI is (-0.4972735 0.6217286).

```
t.test(ads_data[test == 1, tot_impr], ads_data[test == 0, tot_impr])
```

Welch Two Sample t-test

```
data: ads_data[test == 1, tot_impr] and ads_data[test == 0, tot_impr]
t = 0.2168, df = 25602, p-value = 0.8284
```

```

alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -0.4977312  0.6215331
sample estimates:
mean of x mean of y
 24.8277  24.7658

```

Modify the function above to get the right answer. Your answer in the code chunk below

```
t.test(ads_data[test == 1, converted], ads_data[test == 0, converted])
```

#### Welch Two Sample t-test

```

data: ads_data[test == 1, converted] and ads_data[test == 0, converted]
t = 8.6523, df = 26376, p-value < 2.2e-16
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 0.005947966 0.009432084
sample estimates:
mean of x mean of y
0.02554869 0.01785866

```

Observation : 1. The p-value is less than  $2.2e-16$ ,  $p < 0.05$ . 2. The 95% CI, also provides a range of values for the difference that is likely to contain the true value with 95% certainty. - Thus results that the ad campaign cause more purchases & is statistically significant.

## 2.2 Was the campaign profitable?

### 2.2.a How much more profit did TaskaBella make by running the campaign (excluding advertising costs)

Hint: the profit per conversion is given on page 2 of the case.

```

# $40 converting user worth * dim[converted ==1]
ads_data_test_con <- sum(ads_data$test == 1)
ads_data_control_con <- sum(ads_data$test == 0)

con_test <- sum(ads_data$converted[ads_data$test == 1])
con_control <- sum(ads_data$converted[ads_data$test == 0])

test_rate_conversion <- con_test/ads_data_test_con
control_rate_conversion <- con_control/ads_data_control_con
test_group = sum(ads_data$test == 1)

```

```
more_profit <- (test_rate_conversion - control_rate_conversion) * test_group * 40
print(more_profit)
```

```
[1] 173650
```

```
print(paste0("More Profit: ", more_profit))
```

```
[1] "More Profit: 173649.994047113"
```

More Profit appears to be exactly as 173649.99, rounding off as 173650. Ans 2.2 -> Yes, Profitable

### 2.2.b What was the cost of the campaign (including the control group)?

Hint: The cost per thousand impressions is \$9

```
#14.5*10^6
cost_per_imp <- 9/1000
campaign_cost <- sum(ads_data[, tot_impr]) * cost_per_imp
print(paste0("The Cost of the campaign: ", campaign_cost))
```

```
[1] "The Cost of the campaign: 131385.798"
```

The Cost of the campaign appears to be \$131385.8.

### 2.2.c Calculate the ROI of the campaign (including the control group). Was the campaign profitable?

The ROI is calculated by (Effect on Profits per Person in Campaign - Cost of Ads per Person in Campaign) / (Cost of Ads per Person in Campaign)

```
roi <- (more_profit - campaign_cost)/campaign_cost
print(paste0("The ROI of the campaign is: ", roi))
```

```
[1] "The ROI of the campaign is: 0.321680095493372"
```

The ROI appears to be +ve as 0.32168 or 32%, hence is profitable.

## 2.2.d What was the opportunity cost of including a control group — how much more could TaskaBella have made by not having a control group at all?

```
data_test = sum(ads_data$test == 1) ##reference from question 1.1
data_control = sum(ads_data$test == 0) ## reference from question 1.1

conv_rate_treatment <- sum(ads_data$converted[ads_data$test == 1]) / data_test
conv_rate_control <- sum(ads_data$converted[ads_data$test == 0]) / data_control

control_group <- sum(ads_data$test == 0)

opportunity_cost <- (conv_rate_treatment - conv_rate_control) * control_group * 40
print(paste0("The Opportunity Cost of including a control group is: ",opportunity_cost))

[1] "The Opportunity Cost of including a control group is: 7234.16038120206"
```

Opportunity Cost : 7234.16038120206

## 3 Based on the above figure, can we say that more impressions cause more conversions? (No more than 2 sentences)

Ans Q3: No, Based on the above figure we cannot say as its directly proportional, but correlated also, The causality cannot be established without considering the assumptions of casual inference.

## 4 Calculate the power of this experiment.

### 4.1 Calculate cohen's D. Cohen's D in this case is the estimated average treatment effect on conversion divided by the standard deviation of conversion.

Hint, the standard deviation function is: sd

```
test_data <- ads_data[test == 1, converted]
control_data <- ads_data[test == 0, converted]

mean_data_test <- mean(test_data)
mean_data_control <- mean(control_data)

standard_deviation_control = sd(control_data)
cohen_d = (mean_data_test - mean_data_control)/standard_deviation_control
cohen_d

[1] 0.05806402
```

```

#cohens_d = ATE_hat/standard_deviation_control
#cohens_d / Alternatively for results (cohen's d)

print(paste0("The value of mean of test group: ", mean_data_test))

[1] "The value of mean of test group: 0.0255486865179884"

print(paste0("The value of mean of control group: ", mean_data_control))

[1] "The value of mean of control group: 0.0178586614508036"

print(paste0("The value of standard deviation of control group: ", standard_deviation_control))

[1] "The value of standard deviation of control group: 0.132440460184666"

print(paste0("The value of cohen's d: ", cohen_d))

[1] "The value of cohen's d: 0.0580640165132491"

```

Cohen's D value is 0.0580640165132491 Standard Deviation appears to be: 0.132440460184666

#### 4.2 Use the `pwr.t2n.test` function to calculate the power of the experiment:

Hint, we can calculate the number of individuals in a subset of the data like this:

```
ads_data[test == 1, .N]
```

```

pwr.t2n.test(n1 = sum(ads_data[test == 1, .N]),
n2 = sum(ads_data[test == 0, .N]),
d = cohen_d,
sig.level = .05,
power = NULL)

```

t test power calculation

```

      n1 = 564530
      n2 = 23518
      d = 0.05806402
sig.level = 0.05
  power = 1
alternative = two.sided

```

Here in above treatment with moderate effect size, the power appears to be 1 or 100% probability of detecting an effect if exists.

### 4.3 What would the power be instead if the true effect had a Cohen's D of .01?

Hint: Copy the above function and modify accordingly.

```
pwr.t2n.test(n1 = sum(ads_data[test == 1, .N]),
             n2 = sum(ads_data[test == 0, .N]),
             d = 0.01,
             sig.level = .05,
             power = NULL)
```

t test power calculation

```
      n1 = 564530
      n2 = 23518
      d = 0.01
sig.level = 0.05
power = 0.3239638
alternative = two.sided
```

power = 0.3239638: This states, experiment has a 32.4% chance of detecting the true effect if it exists, Also it will consider both positive and negative differences between treatment and control group.

### 4.4 What would the power be instead if the true effect had a Cohen's of .01 and the sample was equally split between treatment and control?

Hint: Copy the above function and modify accordingly.

```
size = ads_data[, .N]/2
pwr.t2n.test(n1 = size,
             n2 = size,
             d = 0.01,
             sig.level = .05,
             power = NULL)
```

t test power calculation

```
      n1 = 294024
      n2 = 294024
      d = 0.01
sig.level = 0.05
power = 0.9695516
alternative = two.sided
```

Power: 0.9695516, or approx 97%.

**5 Case Writeup + Case Discussion in Class, be prepared to discuss!**

I would discuss the real-world examples & importance of online advertising and its impact on the business. Having opportunity (\$7234) for including control group & +ve ROI, does holds a scope of online advertising. It is also seen that, an increase profit of \$173650 is enough for advertising campaign to be considered.

**How long did this assignment take you to do (hours)? How hard was it (easy, reasonable, hard, too hard)?**

The assignment took a day, & hard.