

# CS-225: Discrete Structures in CS

## Assignment 10

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### Canvas Problems

1

Step	$S$	$L(b)$	$L(a)$	$L(c)$	$L(d)$	$L(e)$	$L(f)$	$L(g)$	$L(h)$	$L(i)$	$L(j)$	$L(z)$
0	$\emptyset$	0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
1	$\{b\}$	$0, b$	$3, b$	$2, b$	$\infty$	$5, b$	$7, b$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
2	$\{b, c\}$	$0, b$	$3, b$	$2, (b, c)$	$5, (b, c)$	$5, b$	$4, (b, c)$	$8, (b, c)$	$\infty$	$\infty$	$\infty$	$\infty$
3	$\{b, c, a\}$	$0, b$	$3, (b, a)$	$2, (b, c)$	$5, (b, c)$	$5, b$	$4, (b, c)$	$8, (b, c)$	$7, (b, a, h)$	$\infty$	$\infty$	$\infty$
4	$\{b, c, a, f\}$	$0, b$	$3, (b, a)$	$2, (b, c)$	$5, (b, c)$	$5, b$	$4, (b, c, f)$	$8, (b, c)$	$7, (b, a, h)$	$8, (b, c, f)$	$7, (b, c, f)$	$\infty$
5	$\{b, c, a, f, e\}$	$0, b$	$3, (b, a)$	$2, (b, c)$	$5, (b, c)$	$5, (b, e)$	$4, (b, c, f)$	$8, (b, c)$	$7, (b, a, h)$	$8, (b, c, f)$	$7, (b, c, f)$	$\infty$
6	$\{b, c, a, f, e, d\}$	$0, b$	$3, (b, a)$	$2, (b, c)$	$5, (b, c, d)$	$5, (b, e)$	$4, (b, c, f)$	$8, (b, c)$	$7, (b, a, h)$	$8, (b, c, f)$	$7, (b, c, f)$	$7, (b, c, d)$
7	$\{b, c, a, f, e, d, j\}$	$0, b$	$3, (b, a)$	$2, (b, c)$	$5, (b, c, d)$	$5, (b, e)$	$4, (b, c, f)$	$8, (b, c)$	$7, (b, a, h)$	$8, (b, c, f)$	$7, (b, c, f, j)$	$7, (b, c, d)$

The shortest path from  $b$  to  $j$  is  $b \rightarrow c \rightarrow f \rightarrow j$  and is of length 7.

2

Step	$S$	$L(a)$	$L(b)$	$L(c)$	$L(d)$	$L(e)$	$L(f)$	$L(g)$	$L(h)$	$L(i)$	$L(j)$	$L(z)$
0	$\emptyset$	0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
1	$a$	$0, a$	$2, a$	$6, a$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
2	$\{a, b\}$	$0, a$	$2, (a, b)$	$6, a$	$5, (a, b)$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
3	$\{a, b, d\}$	$0, a$	$2, (a, b)$	$6, a$	$5, (a, b, d)$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$7, (a, b, d)$	$\infty$
4	$\{a, b, d, c\}$	$0, a$	$2, (a, b)$	$6, (a, c)$	$5, (a, b, d)$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$7, (a, b, d)$	$\infty$
5	$\{a, b, d, c, j\}$	$0, a$	$2, (a, b)$	$6, (a, c)$	$5, (a, b, d)$	$\infty$	$12, (a, b, d, j)$	$\infty$	$10, (a, b, d, j)$	$9, (a, b, d, j)$	$7, (a, b, d, j)$	$\infty$
6	$\{a, b, d, c, j, i\}$	$0, a$	$2, (a, b)$	$6, (a, c)$	$5, (a, b, d)$	$\infty$	$10, (a, b, d, j, i)$	$\infty$	$10, (a, b, d, j)$	$9, (a, b, d, j, i)$	$7, (a, b, d, j)$	$\infty$
7	$\{a, b, d, c, j, i, h\}$	$0, a$	$2, (a, b)$	$6, (a, c)$	$5, (a, b, d)$	$\infty$	$10, (a, b, d, j, i)$	$\infty$	$10, (a, b, d, j, h)$	$9, (a, b, d, j, i)$	$7, (a, b, d, j)$	$\infty$
8	$\{a, b, d, c, j, i, h, f\}$	$0, a$	$2, (a, b)$	$6, (a, c)$	$5, (a, b, d)$	$12, (a, b, d, j, i, f)$	$10, (a, b, d, j, i, f)$	$14, (a, b, d, j, i, f)$	$10, (a, b, d, j, h)$	$9, (a, b, d, j, i)$	$7, (a, b, d, j)$	$13, (a, b, d, j, i, f)$
8	$\{a, b, d, c, j, i, h, f, z\}$	$0, a$	$2, (a, b)$	$6, (a, c)$	$5, (a, b, d)$	$12, (a, b, d, j, i, f)$	$10, (a, b, d, j, i, f)$	$14, (a, b, d, j, i, f)$	$10, (a, b, d, j, h)$	$9, (a, b, d, j, i)$	$7, (a, b, d, j)$	$13, (a, b, d, j, i, f, z)$

The shortest path from  $a$  to  $z$  is  $a \rightarrow b \rightarrow d \rightarrow j \rightarrow i \rightarrow f \rightarrow z$  and is of length 13.