



# **Outline**

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### Introduction

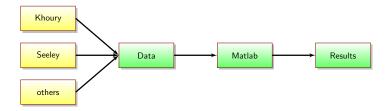


Figure 1: Diagram of our work [khoury13 ] [seeley95 ].

# **Description of the Standard Model**

It consists of four differential equations:

- Change of brood number
- Change of hive bee number
- Change of forager bee number
- Change of food

# **Description of the Standard Model**

Let's look into one equation: Change of brood number

$$\frac{dB}{dt} = LS(H, f) - \phi B \tag{1}$$

- ullet L is the laying rate of the queen
- S is the survival rate
- *H* is the amount of hive bees
- f is the amount of food
- $\bullet \hspace{0.1in} \phi$  is the adult bee emerging factor

# **Environmental Influences**

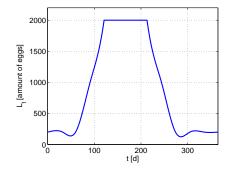


Figure 2: The laying rate of the bee queen plotted over a year.

#### **Environmental Influences**

Comparison between the environment dependent equation and the standard one:

- $\bullet$  static equation:  $\frac{dB}{dt} = LS(H,f) \phi B$
- ullet dynamic equation:  $rac{dB}{dt} = L_t S(H,f) \phi B$
- $\longrightarrow$  small changes in the formulae have significant effects (cf. Discussion).

# Advanced model: Environment simulation

#### Model overview

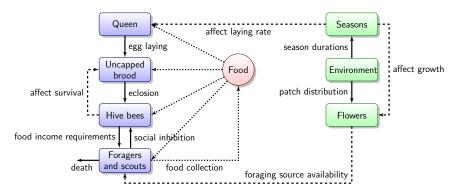


Figure 3: Honey bee social dynamics and environmental influences covered by our advanced model.

# Agents: Assigning jobs

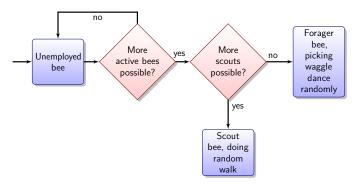


Figure 4: Assigning jobs to unemployed bees. Scouts and foragers are possible.

## Foragers' distribution across flower patches

- Bees will focus on newly reported and then on the most profitable food sources
- Driving factors for evaluating a patch (p < q):
  - 1. Patch quality  $(b_w)$
  - 2. Distance from the hive  $(d_w)$
  - 3. Patch size  $(A_w)$
- Relative evaluation based on what other foraging sources are available

## **Agents: Scout bees**

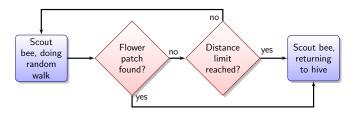


Figure 5: Scouting behaviour until a flower patch is found or the maximum distance is reached.

The path a scout bee walks is recorded in a vector of x and y coordinates:

$$\begin{pmatrix} x_0 & x_1 & \dots & x_n \\ y_0 & y_1 & \dots & y_n \end{pmatrix}$$

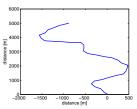


Figure 6: Example of a random walk executed by a scout bee.

### Agents: Forager bees

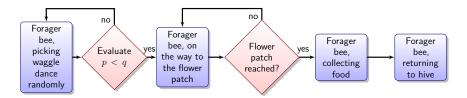


Figure 7: Foraging behaviour.

# Path optimization

- Bees are able to orientate themselves in the environment with sun positioning [seeley95]
- Every second way point is skipped
- Starting- and endpoints are preserved
- $\bullet$  Triangle inequality  $\Rightarrow L^2$  norm of the distance can only become smaller

$$\begin{pmatrix} x_0 & x_1 & x_2 & x_3 & x_4 & \dots & x_{n-3} & x_{n-2} & x_{n-1} & x_n \\ y_0 & y_1 & y_2 & y_3 & y_4 & \dots & y_{n-3} & y_{n-2} & y_{n-1} & y_n \end{pmatrix}$$

$$\implies_{optimization} \begin{pmatrix} x_0 & x_2 & x_4 & \dots & x_{n-4} & x_{n-2} & x_n \\ y_0 & y_2 & y_4 & \dots & y_{n-4} & y_{n-2} & y_n \end{pmatrix}$$

## Path optimization

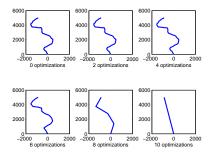


Figure 8: Example of path optimization used to short cut the path to flower patches.

## Agents: Returning to the hive

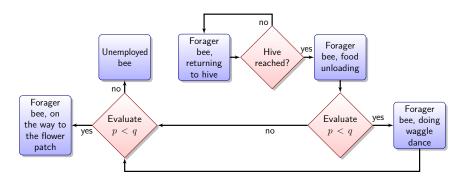


Figure 9: Forager bee, returning from foraging.

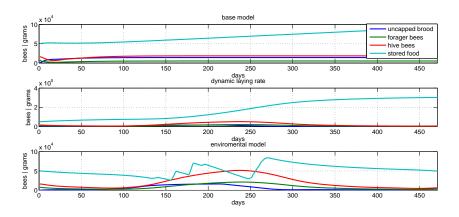
# Agent based model: recorded sample clips

- Day 158, recorded sample with scouts displayed
- Day 158, recorded sample without scouts displayed
- Two different runs, not the same flower patches are being selected

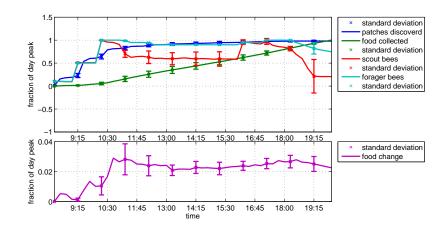
# Simulation results and analysis

- Evolution of the model
- Missing flower season comparison
- Critical points in the fall season

#### **Evolution of the model**



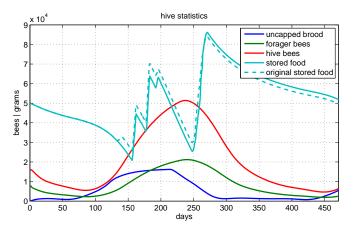
## **Daily simulation**



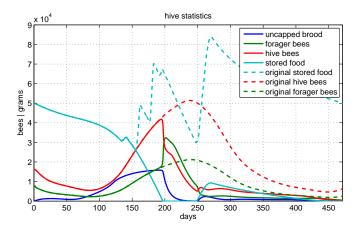
# Missing flower season comparison

- Eliminate non critical seasons
- Study effects of missing season
- Observe the hives compensation measures

# **Spring**



#### Summer

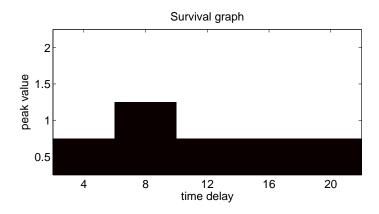


### Critical points in the fall season

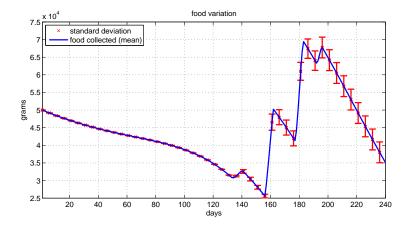
#### Death criteria:

- Less than 1000 bees at day 400
- Less than 20 kg of stored food at day 400

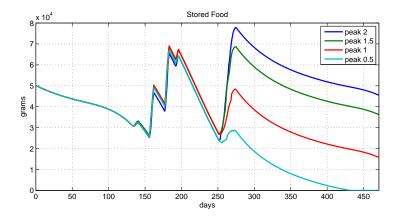
#### Overview



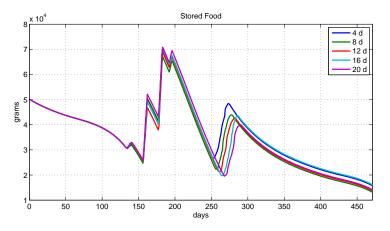
#### Stored food variation before fall



#### Peak value influence



### Delay influence around breaking point



# **Summary**

- Standard Model after D.S. Khoury.
- Advanced Model: Environment simulation
- Autumnal shift is indifferent
- Hive is rather stable
- Model restrictions

