

EE302 Homework 1

Nail Tosun - 2094563 -Section 5
Electric and Electronic Engineering Department, METU

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1)
a)

Table 1: Routh-Hurwitz Table for part-a

| | | | |
|-------|-----|-----|---|
| s^3 | 1 | 10 | 0 |
| s^2 | 20 | 400 | 0 |
| s | -10 | 0 | 0 |
| 1 | 400 | 0 | |

There are two positive root therefore system is unstable. b)

Table 2: Routh-Hurwitz Table for part-b

| | | | |
|-------|-------------------|------|---|
| s^5 | 1 | 2 | 3 |
| s^4 | 3 | 6 | 1 |
| s^3 | $\epsilon = 0.01$ | 2.67 | 0 |
| s^2 | -794 | 1 | 0 |
| s | 2.67 | 1 | 0 |
| 1 | 1 | 0 | 0 |

There are two positive root therefore system is unstable.
c)

Table 3: Routh-Hurwitz Table for part-c

| | | | |
|-------|----|----|----|
| s^4 | 1 | 2 | -8 |
| s^3 | -1 | -4 | 0 |
| s^2 | -2 | -4 | 0 |
| s | 4 | 0 | |
| 1 | -8 | | |

There are three positive root therefore system is unstable.

Table 4: Routh-Hurwitz Table for part-d

| | | | |
|-------|---|----|-----|
| s^5 | 1 | 16 | 100 |
| s^4 | 2 | 32 | 200 |
| s^3 | 0 | 0 | 0 |
| s^2 | | | |
| s | | | |
| 1 | | | |

Entire row is zero. Therefore i take derivative of upward equation and added its coefficients to zero row.

$$\frac{d}{ds}(2s^4 + 32s^2 + 200)$$

$$8s^3 + 64s$$

then new table become;

Table 5: Routh-Hurwitz Table for part-d ver2

| | | | |
|-------|------|-----|-----|
| s^5 | 1 | 16 | 100 |
| s^4 | 1 | 8 | 0 |
| s^3 | 8 | 100 | 0 |
| s^2 | -4.5 | 0 | 0 |
| s | 100 | 0 | 0 |
| 1 | 0 | | |

4) Matlab script to finding roots;

```
p1 = [1 20 10 400];
p2 = [1 3 2 6 3 1];
p3 = [1 -1 2 -4 -8];
```

```
p4 = [1 2 16 32 100 200];
roots1 = roots(p1);
roots2 = roots(p2);
roots3 = roots(p3);
roots4 = roots(p4);
```

Results are (in 2 significant digit); polynomial 1 has roots at

$$\lambda_1 = -20,47 + 0,00i$$

$$\lambda_2 = 0,23 + 4,41i$$

$$\lambda_3 = 0,23 - 4,41i$$

polynomial 2 has roots at

$$\lambda_1 = -2,91$$

$$\lambda_2 = 0,23 + 1,33i$$

$$\lambda_3 = 0,23 - 1,33i$$

$$\lambda_4 = -0,28 + 0,34i$$

$$\lambda_5 = -0,28 - 0,34i$$

polynomial 3 has roots at

$$\lambda_1 = 2.00$$

$$\lambda_2 = 2.00i$$

$$\lambda_3 = -2.00i$$

$$\lambda_4 = -1.00$$

polynomial 4 has roots at

$$\lambda_1 = 1,00 + 3,00i$$

$$\lambda_2 = 1,00 - 3,00i$$

$$\lambda_3 = -1,00 + 3,00i$$

$$\lambda_4 = -1,00 - 3,00i$$

$$\lambda_5 = -2,00$$