

Projet CPS 2018

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Contents

1 Services 3

1.1 Map Service 3

1.2 EditMap Service 4

1.3 Environement Service 5

1 Services

1.1 Map Service

Service: Map
Types: bool, int, Cell
Observers: **const** Height: $[Map] \rightarrow int$
const Width: $[Map] \rightarrow int$
CellNature: $[Map] \times int \times int \rightarrow Cell$
pre CellNature(M, x, y) **requires** $0 \leq x < Width(M)$ and $0 \leq y < Height(M)$
Constructors: **init:** $int \times int \rightarrow [Map]$
pre init(w, h) **requires** $0 \leq w$ and $0 \leq h$
Operators: **OpenDoor:** $[Map] \times int \times int \rightarrow [Map]$
pre OpenDoor(M, x, y) **requires** CellNature(M, x, y) $\in DNC, DWC$
CloseDoor: $[Map] \times int \times int \rightarrow [Map]$
pre CloseDoor(M, x, y) **requires** CellNature(M, x, y) $\in \{DNO, DWO\}$
Observation:
[Invariant]: \top
[Init]: Height(init(h, w)) = h
Width(init(h, w)) = w
[OpenDoor]: CellNature(M, x, y) = DWC **implies** CellNature(OpenDoor(M, x, y), x, y) = DWO
CellNature(M, x, y) = DNC **implies** CellNature(OpenDoor(M, x, y), x, y) = DNO
forall $u \in [0; Width(M)-1]$ **forall** $v \in [0; Height(M)-1]$ ($u \neq x$ **or** $v \neq y$)
implies CellNature(OpenDoor(M, x, y), u, v) = CellNature(M, u, v)
[CloseDoor]: CellNature(M, x, y) = DWO **implies** CellNature(OpenDoor(M, x, y), x, y) = DWC
CellNature(M, x, y) = DNO **implies** CellNature(OpenDoor(M, x, y), x, y) = DNC
forall $u \in [0; Width(M)-1]$
forall $v \in [0; Height(M)-1]$ ($u \neq x$ **or** $v \neq y$)
implies CellNature(OpenDoor(M, x, y), u, v) = CellNature(M, u, v)

1.2 EditMap Service

Service: EditMap refine Map

Types: bool, int, Cell

Observers: isReachable: $[EditMap] \times int \times int \times int \times int \rightarrow bool$
pre isReachable(M,x1,y1,x2,y2) **requires** CellNature(M,x1,y1) \neq WLL **and** CellNature(M,x2,y2) \neq WLL
 isReady: $[EditMap] \rightarrow bool$

Constructors: \emptyset

Operators: SetNature: $[EditMap] \times int \times int \times Cell \rightarrow [EditMap]$
pre SetNature(M,x,y) **requires** $0 \leq x \leq Width(M)$ **and** $0 \leq y \leq Height(M)$

Observations:

[Invariants]: isReachable(M,x1,y1,x2,y2) = **exists** P **in** Array[int,int], P[0] = (x1,y1)
and P[size(P)-1] = (x2,y2)
and forall i **in** [1;size(P)-1], (P[i-1]=(u,v) **and** P[i]=(s,t)) **implies** $(u-s)^2 + (v-t)^2 = 1$
and forall i **in** [1;size(P)-2], P[i-1]=(u,v) **implies** CellNature(M,u,v) \neq WLL
 isReady(M) = **exists** xi,yi,xo,yo **in** int^4 , CellNature(M,xi,yi) = IN
and CellNature(M,xi,yi) = OUT
and isReachable(M,xi,yi,xo,yo)
and forall x,y **in** int^2 , $x \neq xi$ **or** $y \neq yi$ **implies** CellNature(M,x,y) \neq IN
and forall x,y **in** int^2 , $x \neq xo$ **or** $y \neq yo$ **implies** CellNature(M,x,y) \neq OUT
forall x,y **in** int, CellNature(M,x,y) $\in \{DNO, DNC\}$
implies CellNature(M,x+1,y) = CellNature(M,x-1,y) = EMP
and CellNature(M,x,y-1) = CellNature(M,x,y+1) = WLL
forall x,y **in** int, CellNature(M,x,y) $\in \{DWO, DWC\}$
implies CellNature(M,x+1,y) = CellNature(M,x-1,y) = WLL
and CellNature(M,x,y-1) = CellNature(M,x,y+1) = EMP
[SetNature]: CellNature(SetNature(M,x,y,Na),x,y) = Na
forall u,v **in** int^2 , $u \neq x$ **or** $v \neq y$
implies CellNature(SetNature(M,x,y),u,v) = CellNature(M,u,v)

1.3 Environement Service

Service: Environement **include** EditMap

Types: bool, int, Cell, Mob

Observers: CellContent: $\text{int} \times \text{int} \rightarrow \text{Option}[\text{Mob}]$

CellRessources: $\text{int} \times \text{int} \rightarrow \text{Option}[\text{Ressource}]$

mob : $\text{int} \times \text{int} \rightarrow \text{Mob}$

ressource : $\text{int} \times \text{int} \rightarrow \text{Ressource}$

Operators: CloseDoor: $[\text{Environment}] \times \text{int} \times \text{int} \times [\text{Environment}]$

pre CloseDoor(M,x,y) **requires** CellContent(M,x,y) = No

1.4 Mob Service

Service: Mob
Types: bool, int, Cell
Observers: Env: [Mob] \rightarrow Environment
Col: [Mob] \rightarrow int
Row: [Mob] \rightarrow int
Face: [Mob] \rightarrow Dir
Constructors: init: Environment \times int \times int \times Dir \rightarrow [Mob]
pre init(E,x,y,D) **requires** $0 \leq x \mid \text{Environment::Width}(E)$ **and** $0 \leq y \mid \text{Environment::Height}(E)$
Operators: Forward: [Mob] \rightarrow [Mob]
Backward: [Mob] \rightarrow [Mob]
TurnL: [Mob] \rightarrow [Mob]
TurnR: [Mob] \rightarrow [Mob]
StrafeL: [Mob] \rightarrow [Mob]
StrafeR: [Mob] \rightarrow [Mob]
Attack: [Mob] \rightarrow [Mob]

[**Observations**] :

[**invariant**] : $0 \leq \text{Col}(M) \mid \text{Environment::Width}(\text{Envi}(M))$
 $0 \leq \text{Row}(M) \mid \text{Environment::Height}(\text{Envi}(M))$
 $\text{Environment::CellNature}(\text{Envi}(M), \text{Col}(M), \text{Row}(M)) \notin \{WLL, DNC, DWC\}$

[**init**] : $\text{Col}(\text{init}(E, x, y, D)) = x$
 $\text{Row}(\text{init}(E, x, y, D)) = y$
 $\text{Face}(\text{init}(E, x, y, D)) = D$
 $\text{Envi}(\text{init}(E, x, y, D)) = E$

[**Forward**]: $\text{Face}(M)=S$ **implies**
 $\text{Environment::CellNature}(\text{Envi}(M), \text{Col}(M), \text{Row}(M)+1) \in \{EMP, DWO\}$
and $\text{Row}(M)+1 \mid \text{Environment::Width}(\text{Envi}(M))$
and $\text{Environment::CellContent}(\text{Envi}(M), \text{Col}(M), \text{Row}(M)+1) = \text{No}$
implies $\text{Row}(\text{Forward}(M)) = \text{Row}(M) + 1$
and $\text{Col}(\text{Forward}(M)) = \text{Col}(M)$

$\text{Face}(M)=S$ **implies**
 $\text{Environment::CellNature}(\text{Envi}(M), \text{Col}(M), \text{Row}(M)+1) \in \{EMP, DWO\}$
or $\text{Row}(M)+1 \geq \text{Environment::Width}(\text{Envi}(M))$
or $\text{Environment::CellContent}(\text{Envi}(M), \text{Col}(M), \text{Row}(M)+1) \neq \text{No}$
implies $\text{Row}(\text{Forward}(M)) = \text{Row}(M)$ **and** $\text{Col}(\text{Forward}(M)) = \text{Col}(M)$

$\text{Face}(M)=E$ **implies** $\text{Environment::CellNature}(\text{Envi}(M), \text{Col}(M)+1, \text{Row}(M)) \in \{EMP, DNO\}$
and $\text{Col}(M)+1 \mid \text{Environment::Height}(\text{Envi}(M))$
and $\text{Environment::CellContent}(\text{Envi}(M), \text{Col}(M)+1, \text{Row}(M)) = \text{No}$
implies $\text{Row}(\text{Forward}(M)) = \text{Row}(M)$ **and** $\text{Col}(\text{Forward}(M)) = \text{Col}(M) + 1$

$\text{Face}(M)=E$ **implies**
 $\text{Environment::CellNature}(\text{Envi}(M), \text{Col}(M)+1, \text{Row}(M)) \in \{EMP, DWO\}$
or $\text{Row}(M) \geq \text{Environment::Width}(\text{Envi}(M))$
or $\text{Environment::CellContent}(\text{Envi}(M), \text{Col}(M)+1, \text{Row}(M)) \neq \text{No}$
implies $\text{Row}(\text{Forward}(M)) = \text{Row}(M)$ **and** $\text{Col}(\text{Forward}(M)) = \text{Col}(M)$

$\text{Face}(M)=N$ **implies**
 $\text{Environment::CellNature}(\text{Envi}(M), \text{Col}(M), \text{Row}(M)-1) \in \{EMP, DWO\}$
and $\text{Col}(M)-1 \geq 0$
and $\text{Environment::CellContent}(\text{Envi}(M), \text{Col}(M), \text{Row}(M)+1) = \text{No}$
implies $\text{Row}(\text{Forward}(M)) = \text{Row}(M) - 1$ **and** $\text{Col}(\text{Forward}(M)) = \text{Col}(M)$

$\text{Face}(M)=N$ **implies**
 $\text{Environment::CellNature}(\text{Envi}(M), \text{Col}(M), \text{Row}(M)-1) \in \{EMP, DWO\}$ or $\text{Col}(M)-1 \mid 0$
or $\text{Environment::CellContent}(\text{Envi}(M), \text{Col}(M), \text{Row}(M)-1) \neq \text{No}$
implies $\text{Row}(\text{Forward}(M)) = \text{Row}(M)$ **and** $\text{Col}(\text{Forward}(M)) = \text{Col}(M)$

$\text{Face}(M)=W$ **implies**
 $\text{Environment::CellNature}(\text{Envi}(M), \text{Col}(M)-1, \text{Row}(M)) \in \{EMP, DNO\}$
and $\text{Row}(M)-1 \geq 0$
and $\text{Environment::CellContent}(\text{Envi}(M), \text{Col}(M)-1, \text{Row}(M)) = \text{No}$
implies $\text{Row}(\text{Forward}(M)) = \text{Row}(M)$ **and** $\text{Col}(\text{Forward}(M)) = \text{Col}(M) - 1$

$\text{Face}(M)=W$ **implies**
 $\text{Environment::CellNature}(\text{Envi}(M), \text{Col}(M)-1, \text{Row}(M)) \in \{EMP, DNO\}$
or $\text{Row}(M)-1 \mid 0$ or $\text{Environment::CellContent}(\text{Envi}(M), \text{Col}(M), \text{Row}(M)-1) \neq \text{No}$
implies $\text{Row}(\text{Forward}(M)) = \text{Row}(M)$ **and** $\text{Col}(\text{Forward}(M)) = \text{Col}(M)$

[Backward]: Face(M)=N **implies**

Environment::CellNature(Envi(M),Col(M),Row(M)+1) $\in \{EMP, DWO\}$
and Row(M)+1 \leq Environment::Width(Envi(M))
and Environment::CellContent(Envi(M),Col(M),Row(M)+1) = No
implies Row(Backward(M)) = Row(M) + 1
and Col(Backward(M)) = Col(M)

Face(M)=N **implies**

Environment::CellNature(Envi(M),Col(M),Row(M)+1) $\in \{EMP, DWO\}$
or Row(M)+1 \geq Environment::Width(Envi(M))
or Environment::CellContent(Envi(M),Col(M),Row(M)+1) \neq No
implies Row(Backward(M)) = Row(M) **and** Col(Backward(M)) = Col(M)

Face(M)=W **implies** Environment::CellNature(Envi(M),Col(M)+1,Row(M)) $\in \{EMP, DNO\}$

and Col(M)+1 \leq Environment::Height(Envi(M))

and Environment::CellContent(Envi(M),Col(M)+1,Row(M)) = No

implies Row(Backward(M)) = Row(M) **and** Col(Backward(M)) = Col(M) + 1

Face(M)=W **implies**

Environment::CellNature(Envi(M),Col(M)+1,Row(M)) $\in \{EMP, DWO\}$
or Row(M) \geq Environment::Width(Envi(M))

or Environment::CellContent(Envi(M),Col(M)+1,Row(M)) \neq No

implies Row(Backward(M)) = Row(M) **and** Col(Backward(M)) = Col(M) Face(M)=S **implies**

Environment::CellNature(Envi(M),Col(M),Row(M)-1) $\in \{EMP, DWO\}$

and Col(M)-1 \geq 0

and Environment::CellContent(Envi(M),Col(M),Row(M)+1) = No

implies Row(Backward(M)) = Row(M) - 1 **and** Col(Backward(M)) = Col(M)

Face(M)=S **implies**

Environment::CellNature(Envi(M),Col(M),Row(M)-1) $\in \{EMP, DWO\}$ or Col(M)-1 \leq 0

or Environment::CellContent(Envi(M),Col(M),Row(M)-1) \neq No

implies Row(Backward(M)) = Row(M) **and** Col(Backward(M)) = Col(M)

Face(M)=E **implies**

Environment::CellNature(Envi(M),Col(M)-1,Row(M)) $\in \{EMP, DNO\}$

and Row(M)-1 \geq 0

and Environment::CellContent(Envi(M),Col(M)-1,Row(M)) = No

implies Row(Backward(M)) = Row(M) **and** Col(Backward(M)) = Col(M) - 1

Face(M)=E **implies**

Environment::CellNature(Envi(M),Col(M)-1,Row(M)) $\in \{EMP, DNO\}$

or Row(M)-1 \leq 0 or Environment::CellContent(Envi(M),Col(M),Row(M)-1) \neq No

implies Row(Backward(M)) = Row(M) **and** Col(Backward(M)) = Col(M)

[StrafeR]: Face(M)=N **implies**

Environment::CellNature(Envi(M),Col(M)+1,Row(M)) $\in \{EMP, DNO\}$

and Col(M)+1 \leq Environment::Height(Envi(M))

and Environment::CellContent(Envi(M),Col(M)+1,Row(M)) = No

implies Row(StrafeR(M)) = Row(M) **and** Col(StrafeR(M)) = Col(M) + 1

Face(M)=N **implies**

Environment::CellNature(Envi(M),Col(M)+1,Row(M)) $\in \{EMP, DWO\}$

or Row(M) \geq Environment::Width(Envi(M))

or Environment::CellContent(Envi(M),Col(M)+1,Row(M)) \neq No

implies Row(StrafeR(M)) = Row(M) **and** Col(StrafeR(M)) = Col(M)

Face(M)=S **implies**

Environment::CellNature(Envi(M),Col(M)-1,Row(M)) $\in \{EMP, DNO\}$

and Row(M)-1 \geq 0

and Environment::CellContent(Envi(M),Col(M)-1,Row(M)) = No

implies Row(StrafeR(M)) = Row(M) **and** Col(StrafeR(M)) = Col(M) - 1 Face(M)=S **implies**

Environment::CellNature(Envi(M),Col(M)-1,Row(M)) $\in \{EMP, DNO\}$

or Row(M)-1 \leq 0 or Environment::CellContent(Envi(M),Col(M),Row(M)-1) \neq No

implies Row(StrafeR(M)) = Row(M) **and** Col(StrafeR(M)) = Col(M)

[StrafeL]: Face(M)=S **implies**
 Environment::CellNature(Envi(M),Col(M)+1,Row(M)) $\in \{EMP, DNO\}$
and Col(M)+1 \leq Environment::Height(Envi(M))
and Environment::CellContent(Envi(M),Col(M)+1,Row(M)) = No
implies Row(StrafeL(M)) = Row(M) **and** Col(StrafeL(M)) = Col(M) + 1

Face(M)=S **implies**
 Environment::CellNature(Envi(M),Col(M)+1,Row(M)) $\in \{EMP, DWO\}$
 or Row(M) \geq Environment::Width(Envi(M))
 or Environment::CellContent(Envi(M),Col(M)+1,Row(M)) \neq No
implies Row(StrafeL(M)) = Row(M) **and** Col(StrafeL(M)) = Col(M)

Face(M)=N **implies**
 Environment::CellNature(Envi(M),Col(M)-1,Row(M)) $\in \{EMP, DNO\}$
and Row(M)-1 \geq 0
and Environment::CellContent(Envi(M),Col(M)-1,Row(M)) = No
implies Row(StrafeL(M)) = Row(M) **and** Col(StrafeL(M)) = Col(M) - 1

Face(M)=N **implies**
 Environment::CellNature(Envi(M),Col(M)-1,Row(M)) $\in \{EMP, DNO\}$
 or Row(M)-1 \geq 0 or Environment::CellContent(Envi(M),Col(M),Row(M)-1) \neq No
implies Row(StrafeL(M)) = Row(M) **and** Col(StrafeL(M)) = Col(M)

[TurnLeft]: Face(M)=N **implies** Face(TurnLeft(M))=W
 Face(M)=W **implies** Face(TurnLeft(M))=S
 Face(M)=S **implies** Face(TurnLeft(M))=E
 Face(M)=E **implies** Face(TurnLeft(M))=N

[TurnRight]: Face(M)=S **implies** Face(TurnRight(M))=W
 Face(M)=E **implies** Face(TurnRight(M))=S
 Face(M)=N **implies** Face(TurnRight(M))=E
 Face(M)=W **implies** Face(TurnRight(M))=N

1.5 Entity Service

Service: Entity **include** Mob
Observers: Hp: [Entity] \rightarrow int
Constructors: init: Environment \times int \times int \times Dir \times int \rightarrow [Entity]
pre init(E,x,y,D,h) **requires** h \geq 0
Operators: step: [Entity] \rightarrow [Entity]
Observations:
[init]: Hp(init(E,x,y,D,h)) = h
[attack]: Face(E) = N **and** Environment::CellContent(Envi(E),Col(E),Row(E)-1) \neq No
implies HP(Attack(Environment::CellContent(Envi(E),Col(E),Row(E)-1))) =
HP(Environment::CellContent(Envi(E),Col(E),Row(E)-1)) - 1

Face(E) = S **and** Environment::CellContent(Envi(E),Col(E),Row(E)+1) \neq No
implies HP(Environment::CellContent(Envi(E),Col(E),Row(E)+1)) =
HP(Environment::CellContent(Envi(E),Col(E),Row(E)+1))@pre - 1

Face(E) = E **and** Environment::CellContent(Envi(E),Col(E)+1,Row(E)) \neq No
implies HP(Environment::CellContent(Envi(E),Col(E)+1,Row(E))) =
HP(Environment::CellContent(Envi(E),Col(E)+1,Row(E)))@pre - 1

Face(E) = W **and** Environment::CellContent(Envi(E),Col(E)-1,Row(E)) \neq No
implies HP(Environment::CellContent(Envi(E),Col(E)-1,Row(E))) =
HP(Environment::CellContent(Envi(E),Col(E)-1,Row(E)))@pre - 1

1.6 Cow Service

Service: Cow **include** Entity
Constructors: init: Environment \times int \times int \times Dir \times int \rightarrow [Entity]
pre init(E,x,y,D,h) **requires** 4 \geq h \geq 3
Operators: Chase: [Cow] \rightarrow [Cow]
Observations:
[step]: Col(M) - 1 \leq Col(step(M)) \leq Col(M) + 1
Row(M) - 1 \leq Row(step(M)) \leq Row(M) + 1

1.7 Player Service

Service: Player **include** Entity

Observers: LastCom: [Player] \rightarrow Option[Command]
 Content: [Player] \times int \times int \rightarrow Option[Mob]
pre Content(P,x,y) **requires** $x \in \{-1, 0, 1\}$ and $y \in \{-1, +3\}$
 Nature: [Player] \times int \times int \rightarrow Cell
pre Nature(P,x,y) **requires** $x \in \{-1, 0, 1\}$ and $y \in \{-1, +3\}$
 Viewable: [Player] \times int \times int \rightarrow Cell
pre Nature(P,x,y) **requires** $x \in \{-1, 0, 1\}$ and $y \in \{-1, +3\}$
 Ressource : [Player] \rightarrow Ressource
 Key: [Player] \rightarrow boolean
 Win: [Player] \rightarrow boolean
pre Win(P) **requires** Ressource(P) = TREASOR
 Dead: [Player] \rightarrow boolean
pre Dead(P) **requires** Hp(P) ≤ 0

Operators:

openDoor:[Player] \rightarrow [Player]

pre OpenDoor(P) **require** Key(P) = true **and**

Face(P) = N **implies** Environement::CellNature(Envi(P), Col(p), Row(p) - 1) $\in \{DWC\}$
and Environement::CellContent(Envi(P), Col(p), Row(p) - 1) = NO

Face(P) = E **implies** Environement::CellNature(Envi(P), Col(p) + 1, Row(p)) $\in \{DNC\}$
and Environement::CellContent(Envi(P), Col(p) + 1, Row(p)) = NO

Face(P) = S **implies** Environement::CellNature(Envi(P), Col(p), Row(p) + 1) $\in \{DWC\}$
and Environement::CellContent(Envi(P), Col(p), Row(p) + 1) = NO

Face(P) = W **implies** Environement::CellNature(Envi(P), Col(p) - 1, Row(p)) $\in \{DNC\}$
and Environement::CellContent(Envi(P), Col(p) - 1, Row(p)) = NO

CloseDoor:[Player] \rightarrow [Player]

pre CloseDoor(P) **require**

Face(P) = N **implies** Environement::CellNature(Envi(P), Col(p), Row(p) - 1) $\in \{DWO\}$
and Environement::CellContent(Envi(P), Col(p), Row(p) - 1) = NO

Face(P) = E **implies** Environement::CellNature(Envi(P), Col(p) + 1, Row(p)) $\in \{DNO\}$
and Environement::CellContent(Envi(P), Col(p) + 1, Row(p)) = NO

Face(P) = S **implies** Environement::CellNature(Envi(P), Col(p), Row(p) + 1) $\in \{DWC\}$
and Environement::CellContent(Envi(P), Col(p), Row(p) + 1) = NO

Face(P) = W **implies** Environement::CellNature(Envi(P), Col(p) - 1, Row(p)) $\in \{DNC\}$
and Environement::CellContent(Envi(P), Col(p) - 1, Row(p)) = NO

Observations:

[**Invariants**]: $\text{Face}(P) = N$
 implies $\text{Content}(P,u,v) = \text{Environment:CellContent}(\text{Envi}(P), \text{Col}(P)+u, \text{Row}(P)+v)$
 $\text{Face}(P) = N$
 implies $\text{Nature}(P,u,v) = \text{Environment:CellNature}(\text{Envi}(P), \text{Col}(P)+u, \text{Row}(P)+v)$
 $\text{Face}(P) = S$
 implies $\text{Content}(P,u,v) = \text{Environment:CellContent}(\text{Envi}(P), \text{Col}(P)-u, \text{Row}(P)-v)$
 $\text{Face}(P) = S$
 implies $\text{Nature}(P,u,v) = \text{Environment:CellNature}(\text{Envi}(P), \text{Col}(P)-u, \text{Row}(P)-v)$
 $\text{Face}(P) = E$
 implies $\text{Content}(P,u,v) = \text{Environment:CellContent}(\text{Envi}(P), \text{Col}(P)+v, \text{Row}(P)-u)$
 $\text{Face}(P) = E$
 implies $\text{Nature}(P,u,v) = \text{Environment:CellNature}(\text{Envi}(P), \text{Col}(P)+v, \text{Row}(P)-u)$
 $\text{Face}(P) = W$
 implies $\text{Content}(P,u,v) = \text{Environment:CellContent}(\text{Envi}(P), \text{Col}(P)-v, \text{Row}(P)+u)$
 $\text{Face}(P) = W$
 implies $\text{Nature}(P,u,v) = \text{Environment:CellNature}(\text{Envi}(P), \text{Col}(P)-v, \text{Row}(P)+u)$
 forall u,v in $[-1,1] \times [-1,1]$, not $\text{Viewable}(P,u,v)$
 $\text{Viewable}(P,-1,2) = \text{Nature}(P,-1,1) \notin \{WALL, DWC, DNC\}$
 $\text{Viewable}(P,0,2) = \text{Nature}(P,0,1) \notin \{WALL, DWC, DNC\}$
 $\text{Viewable}(P,1,2) = \text{Nature}(P,1,1) \notin \{WALL, DWC, DNC\}$
 $\text{Viewable}(P,-1,3) = \text{Nature}(P,-1,2) \notin \{WALL, DWC, DNC\}$ and $\text{Viewable}(P,-1,2)$
 $\text{Viewable}(P,0,3) = \text{Nature}(P,0,2) \notin \{WALL, DWC, DNC\}$ and $\text{Viewable}(P,0,2)$
 $\text{Viewable}(P,1,3) = \text{Nature}(P,1,2) \notin \{WALL, DWC, DNC\}$ and $\text{Viewable}(P,1,2)$

[**openDoor**]: $\text{Key}(\text{OpenDoor}(P)) = \text{true}$
 $\text{Face}(P) = N$ **implies** $\text{Environement::CellNature}(\text{Envi}(P), \text{Col}(p), \text{Row}(p) - 1) \in \{DWO\}$
 $\text{Face}(P) = E$ **implies** $\text{Environement::CellNature}(\text{Envi}(P), \text{Col}(p) + 1, \text{Row}(p)) \in \{DNO\}$
 $\text{Face}(P) = S$ **implies** $\text{Environement::CellNature}(\text{Envi}(P), \text{Col}(p), \text{Row}(p) + 1) \in \{DWO\}$
 $\text{Face}(P) = W$ **implies** $\text{Environement::CellNature}(\text{Envi}(P), \text{Col}(p) - 1, \text{Row}(p)) \in \{DNO\}$

[**ClooseDoor**]: $\text{Key}(\text{OpenDoor}(P)) = \text{Key}(p)$
 $\text{Face}(P) = N$ **implies** $\text{Environement::CellNature}(\text{Envi}(P), \text{Col}(p), \text{Row}(p) - 1) \in \{DWC\}$
 $\text{Face}(P) = E$ **implies** $\text{Environement::CellNature}(\text{Envi}(P), \text{Col}(p) + 1, \text{Row}(p)) \in \{DNC\}$
 $\text{Face}(P) = S$ **implies** $\text{Environement::CellNature}(\text{Envi}(P), \text{Col}(p), \text{Row}(p) + 1) \in \{DWC\}$
 $\text{Face}(P) = W$ **implies** $\text{Environement::CellNature}(\text{Envi}(P), \text{Col}(p) - 1, \text{Row}(p)) \in \{DNC\}$

[**step**]: $\text{LastCom}(P)=FF$ **implies** $\text{step}(P) = \text{Forward}(P)$
 $\text{LastCom}(P)=BB$ **implies** $\text{step}(P) = \text{Backward}(P)$
 $\text{LastCom}(P)=LL$ **implies** $\text{step}(P) = \text{StrafeLeft}(P)$
 $\text{LastCom}(P)=RR$ **implies** $\text{step}(P) = \text{StrafeRight}(P)$
 $\text{LastCom}(P)=TL$ **implies** $\text{step}(P) = \text{TurnLeft}(P)$
 $\text{LastCom}(P)=TR$ **implies** $\text{step}(P) = \text{TurnRight}(P)$
 $\text{LastCom}(P)=C$ **implies** $\text{step}(P) = \text{Attack}(P)$
 $\text{LastCom}(P)=CLOSE$ **implies** $\text{step}(P) = \text{ColseDoor}(P)$
 $\text{LastCom}(P)=OPEN$ **implies** $\text{step}(P) = \text{OpenDoor}(P)$

1.8 Engine Service

Service: Engine

Observer: Envi: [Engine] \rightarrow Environment
Entities: [Engine] \rightarrow Array[Entity]
getEntity: [Engine] \times int \rightarrow Entity

Constructor: init: Environment \rightarrow [Engine]

Operator: removeEntity: [Engine] \times int \rightarrow [Engine]
 pre removeEntity(E,i) **requires** $0 \leq i < \text{size}(\text{Entities}(E))$
addEntity: [Engine] \times Entity \rightarrow [Engine]
step: [Engine] \rightarrow [Engine]
 pre step() **requires**
 forall i in $[0; \text{size}(\text{Entities}(E)) - 1]$, Entity::Hp(getEntity(E,i)) > 0

Observations:

[invariant]: **forall** i in $[0; \text{size}(\text{Entities}(E)) - 1]$, Entity::Envi(getEntity(E,i)) = Envi(E)
 forall i in $[0; \text{size}(\text{Entities}(E)) - 1]$, Entity::Col(getEntity(E,i)) = x
 and Entity::Row(getEntity(E,i)) = y
 implies Environment::CellContent(Envi(E), x, y) = getEntity(E,i)

[removeEntity]: **size**(Entities(removeEntity(E,i))) = **size**(Entities(E)) - 1
 forall k in $[0, i-1]$, getEntity(removeEntity(E,i), k) = getEntity(E, k)
 forall k in $[i, \text{size}(\text{Entities}(E)) - 2]$,
 getEntity(removeEntity(E,i), k) = getEntity(E, k+1)

[addEntity]: **size**(Entities(addEntity(E,e))) = **size**(Entities(E)) + 1
 forall k in $[0, \text{size}(\text{Entities}(E)) - 1]$, getEntity(addEntity(E,e), k) = getEntity(E, k)
 getEntity(addEntity(E,e), **size**(Entities(E))) = e

1.9 Ressources Service

Service: Ressources

Observers : Col : [Ressources] \rightarrow int
Row : [Ressources] \rightarrow int
Row : [Ressources] \rightarrow Environnement

Constructors: init : Environnement \rightarrow [Ressources]
 pre init(e) **requires** 0;Col(S);EnvironnementService::Width(K,getEnv(K))
 0;Row(S);EnvironnementService::Height(K,getEnv(K))

Observations

Invariants: Environnement::CellNature(getEnv(K),Col(S), Row(K)) in EMP
Environnement::CellNature(Envi(S),u,v) in IN
 implies Environnement::isReachable(Envi(S),u,v, Col(S), Row(S))

[init]: Envi(init(e)) = e
Environnement::CellNature(Envi(S), Col(s), Row(S) in {EMP,DNC,DWC}

Service: Key refine Ressources