

23MAT204 – Mathematics for Intelligent Systems - 3

Practise Sheet-10

(Feasible Region)

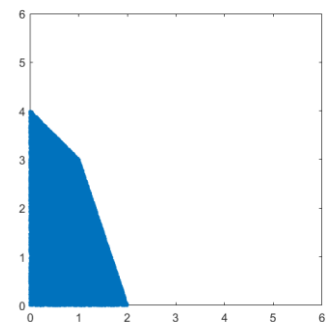
Plotting the feasible region of a constrained optimization problem:

Example 1:

If constraints of the Optimization problem are: $x + y \leq 4$, $3x + y \leq 6$, $x \geq 0$, $y \geq 0$, plot the feasible region

```
N=200000; % number (x,y) points in domain
x = rand(N,1)*6; % generates values in (0,6)
y = rand(N,1)*6; % generates values in (0,6)
f1 = x+y-4; % An array of N fn values in domain
ind1 = (f1<0); % An N array of logical 0s and 1s
f2 = 3*x+y-6; % An array of N fn values in domain
ind2 = (f2<0); % An N_array of logical 0s and 1s
ind3=and(ind1,ind2); % An N_array of logical 0s and 1s
a = [x(ind3),y(ind3)];% points which are in feasible
region
figure
plot(a(:,1),a(:,2),'.', 'MarkerSize',10);
axis equal
xlim([0 6])
ylim([0 6])
```

Output:



%third and forth constraints, x and y are positive are already considered since by using 'rand' command, we randomly generate points only between 0 and 1.

Note:

If we have to generate x in the interval (a,b), the formula to be used is:

$$x = a + (b - a)\text{rand}(N, 1)$$

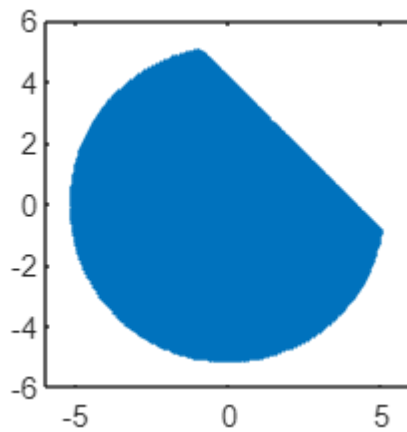
In previous example x and y were generated from (0,6), hence a=0, b=6 in above formula was used.

Example 2:

Plot the region: $x + y \leq 4$, $x^2 + y^2 \leq 25$

```
N=200000; % number (x,y) points in domain
x = -6+12*rand(N,1); % generates values in (-6,6)
y = -6+12*rand(N,1); % generates values in (-6,6)
f1 = x+y-4; % An array of N fn values in domain
ind1 = (f1<0); % An N array of logical 0s and 1s
f2 = x.^2+y.^2-25; % An array of N fn values in domain
ind2 = (f2<0); % An N_array of logical 0s and 1s
ind3=and(ind1,ind2); % An N_array of logical 0s and 1s
a = [x(ind3),y(ind3)];% points which are in feasible region
figure
plot(a(:,1),a(:,2),'.', 'MarkerSize',10);
axis equal
xlim([-6 6])
ylim([-6 6])
```

Output:



Practice questions:

1. Plot the following regions using MATLAB.

(a)
$$\begin{aligned} 3x + y &\leq 1 \\ 2x - 3y &\leq 3 \\ x &\geq 0, y \geq 0 \end{aligned}$$

(b)
$$\begin{aligned} \frac{x^2}{1} + \frac{y^2}{4} &\leq 1 \\ x + y &\leq 1 \end{aligned}$$

(c)
$$\begin{aligned} x + y &\leq 4 \\ 2x + x^2 + y^2 &\leq 15 \\ x &\geq 0, y \geq 0 \end{aligned}$$

(d)
$$\begin{aligned} x^2 + y^2 &= 1 \\ x + y &\geq 1 \end{aligned}$$

(e)
$$\begin{aligned} x^2 + y^2 &\leq 1 \\ x + y &\geq 1 \end{aligned}$$

(f)
$$\begin{aligned} (x - 1)^2 + (y - 1)^2 &\leq 1 \\ x &\leq 1 \\ y &\leq 1 \end{aligned}$$

2. Draw the feasible region for the given problems. Also mention the points where the optimum will exist

(a) Maximize $-6x + 9y$
subject to $x - y \leq 2$
 $3x + y \leq 1$
 $2x - 3y \leq 3$

(b) Minimize $x+y$
subject to $x + y \leq 4$
 $2x + x^2 + y^2 \leq 15$

(c) Minimize $x+y$
subject to $x^2 - y \leq 0$
 $y^2 - x \leq 0$