

This is a precursor to the real class.

An example of the use of modelling, in a somewhat humourous approach is through the use of a girl and boy's love story.

Let's take two functions $G(t)$ and $B(t)$. These functions output the 'feelings' of the girl and the boy.

Then,

$$\begin{aligned}\frac{dG(t)}{dt} &= cG(t) + dB(t) \\ \frac{dB(t)}{dt} &= aB(t) \pm bG(t)\end{aligned}$$

These constants represent some influence on the change in the feelings due to the current feelings you and your significant other can have.

Here's another example:

Model chocolate consumption and the way it leads to happiness. State the variables:

$C(t)$ – Chocolates consumed at a given day

$H(t)$ – Happiness on a given day

The model for these would work like this.

$$\begin{aligned}\frac{dC(t)}{dt} &= \alpha C(t) + \beta H(t) \\ \frac{dH(t)}{dt} &= \delta C(t) + \gamma H(t)\end{aligned}$$

The amount of chocolate depends on our happiness as well as the chocolates already consumed.

0.1 Course Overview

1. Introduction to Modelling
2. Bond graph modelling
3. Basic System Models

Introduction to Modelling

1.1 Terminology

1. **Modelling** - Refers to the development of a mathematical representation of a system.
2. **Simulation** - Refers to the procedure of solving the equations that result from model development.
3. **Mechanics** - Study of the physics of moving and static objects
4. **Dynamics** - Study of moving objects

The steps in the design of dynamic systems involve:

- A physical system, which is represented using an engineering model
- The engineering model, is represented using a bond graph technique, block diagrams or classical method.
- This model is then represented using differential equations
- The equations are solved using simulation software.

This course is mainly going to use the bond graph technique.

1.2 System

A system is an aggregation or assemblage of objects joined in some regular interaction or interdependence. This definition holds good for static systems, and our course focuses on dynamic systems. Systems consist of objects, with certain defined properties. These properties lead to interactions which causes a change in the system. Such objects of interest are known as entities, the properties of these entities are known as attributes, process that causes change in the system are known as activities and the complete description of entities attributes activities is known as the state.

The environment containing the system and surrounding it is known as the system environment. Endogenous describes activities occurring inside the system. Exogeneous describes activities in the environment that affect the system.

A closed system is a system with no exogeneous activity. An open system is a system with exogeneous activities. If the outcomes are predictable, it's deterministic. If they are random and vary with a set probability, they are said to be stochastic. If the outcomes are smooth, then it's said to be continuous. If the outcomes are discontinuous, then it's said to be discrete.