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Quick Sort Trace: Array
[34, 7, 23, 32, 5, 62]

Step 1: Choose 34 as pivot (first element is a common strategy).

Partition: (less than 34), 34, (greater than 34).

Step 2: Recursively Quick Sort. Pivot: 7.

(less), 7, (greater).

Step 3: , Pivot: 23.

[] (less), 23, (greater).

Combine in order:, 34, 62.

Pivots chosen in each step: 34, 7, and 23.

Bottom-Up Heap Construction: Array
[20, 15, 30, 5, 10]

Heap is built level by level.

Representation as a binary tree:

text

20

/ \

15 30

/ \

5 10

Start from last parent (15 at index 1):
No need to swap-children $5, 10 < 15$.

Move to root (20 at index 0): Children
15, 30. Largest is 30, so swap 20 and
30.

Intermediate:

text

30

/ \

15 20

/ \

5 10

15's children unchanged (5, 10).

Final heap:.

Merge Sort vs Quick Sort: Complexity

Algorithm Complexity	Time Complexity Notes	Space
Merge Sort cases	$O(n \log n)$ all $O(n)$	Requires auxiliary array
Quick Sort worst pivot causes worst	$O(n \log n)$ avg, $O(n^2)$ $O(\log n)$	In-place, but bad
Quick sort is faster in practice but can degrade if pivots are poorly chosen.		

Merge sort has predictable performance but higher space usage.

Hybrid Merge + Insertion Sort (for small subarrays)

Approach: During Merge Sort, use Insertion Sort on subarrays smaller than a threshold (e.g., 10 elements) to reduce recursive calls and exploit Insertion Sort's efficiency on small, partially sorted datasets.

Process:

During merge sort split, before recursively sorting a subarray, check its size.

If size \leq threshold, use insertion sort directly.

Merge Sort for Linked List: Steps and Analysis

Divide: Use slow and fast pointers to find the midpoint and split the list.

Conquer: Recursively sort each half. \rightarrow due to halving and merging at each recursive level.

Auxiliary Space:

$O(\log n)$

$O(\log n)$ stack for recursion,

$O(1)$

$O(1)$ extra.

Insertion Sort Effectiveness: Nearly

Sorted Dataset

Best-case Time Complexity:

$O(n)$

$O(n)$ when nearly sorted, each insert is minimal movement.

Justification: Fewer shifts are required.

General: Insertion Sort is highly efficient for small/n nearly sorted data.

Sorting with Many Duplicates: Algorithm

Approach: Use 3-way partitioning Quick Sort.

Why: It groups elements == pivot together, reducing unnecessary comparisons.

Time Complexity:

$O(n \log n)$ average,
 $O(n^2)$ worst, but typically faster for
duplicates.

MergeSort Modification for Large Datasets

Modification: Use iterative/bottom-up Merge Sort (avoiding recursion) or parallel merge, and consider external sort for huge data.

Impact: Reduces stack space requirements, may improve cache efficiency or support out-of-core sorting.

Space Complexity: Still $O(n)$ for merging; time remains $O(n \log n)$.

Hashing Definition

Hashing refers to computing a hash

code or key index from data, enabling fast insertion, deletion, and lookup in data structures like hash tables.

Hash Table Index Calculation

For table size 10 and

$$h(k) = k \bmod 10:$$

$$53 \bmod 10 = 3$$

$$21 \bmod 10 = 1$$

$$87 \bmod 10 = 7$$

$$44 \bmod 10 = 4$$

Binary Search for 13: Array

[2, 5, 8, 13, 17, 19]

Step 1: Start: left=0, right=5. mid=2 (8).
8).

Step 2: 13 > 8, search right half.
left=3, right=5. mid=4 (

17

17).

Step 3: $13 < 17$, search left half. $\text{left}=3$,
 $\text{right}=3$, $\text{mid}=3$ (

13

13).

Found at index 3.

3rd Smallest by Quick Sort: Array

[11, 5, 8, 9, 3, 10]

Pivot selection and partition finds kth element. After partitioning, 8 will be the third smallest:

Partition: less than 11.

Next, partition with 5 as pivot.

Remaining list after sorting: 3, 5, 8, 9,
10, 11. 3rd smallest is 8.

Straight Sequential Search for 18:
Array
[10, 15, 18, 25, 30]

Comparisons: 10 (no), 15 (no), 18 (yes,
found at third element).

Total comparisons: 3

Selection Sort: Array
[14, 7, 9, 3, 12]; Steps and Swaps

Iter 1: min is 3. Swap 14 and 3: (1 swap)

Iter 2: min is 7-already in place.

Iter 3: min is 9-already in place.

Iter 4: min is 12. Swap 14 and 12: (2nd
swap)

Total swaps: 2

Binary Search: Avg and Worst-Case
Analysis

Case	Comparisons	Occurrence
Average	$O(\log n)$	Most searches; divides search intervals.
Worst	$O(\log n)$	When the element is not present or last
		Both cases are $O(\log n)$; practical implications are negligible, but performance is degraded if used on unsorted or non-random-access data.

Optimized Sequential Search: Search 7 in [4,2,9,5,7,1]

Compare each element till 7:
comparisons = 5.

Time Complexity:
 $O(n)$