Consider a group G, there are two canonically associated categories. The first

Let us look at a small category as

Mor

 $G \xrightarrow{G} \left(s = \operatorname{pr} \bigcup_{C} t = \operatorname{left\ mul}\right) \coloneqq EG$

th pair of objects
$$g,g'\in G$$
 $(g,g'g^{-1})$

Such that for each pair of objects $g, g' \in G$ (g,e) g' (g',e)

we have $\operatorname{Hom}_{EG}(g, g') \cong \{*\}$

we have
$$\operatorname{Hom}_{EG}(g, g') \cong \{*\}$$

The second is the usual category with only one object

 $BG \coloneqq \left(\begin{array}{c} G \\ \downarrow \\ G \end{array} \right)$

We have at the same time two pullbacks

$$\begin{pmatrix} \begin{pmatrix} G \\ | & | \\ G \end{pmatrix} & \longrightarrow EG \\ \downarrow & \downarrow \\ \begin{pmatrix} \{*\} \\ 1 \\ \{*\} \end{pmatrix} & \longrightarrow BG \end{pmatrix}$$

$$\begin{pmatrix} \{*\} \\ 1 \\ \{*\} \end{pmatrix} & \longrightarrow \begin{pmatrix} \{*\} \\ 1 \\ \{*\} \end{pmatrix} \\ \downarrow & \downarrow \\ \begin{pmatrix} \{*\} \\ 1 \\ \{*\} \end{pmatrix} & \longrightarrow BG$$

Remedy: Derived Functors