# Hypothesis tests and z-scores

HYPOTHESIS TESTING IN PYTHON



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# A/B testing

- In 2013, Electronic Arts (EA) released
   SimCity 5
- They wanted to increase pre-orders of the game
- They used A/B testing to test different advertising scenarios
- This involves splitting users into control and treatment groups



<sup>&</sup>lt;sup>1</sup> Image credit: "Electronic Arts" by majaX1 CC BY-NC-SA 2.0



# Retail webpage A/B test

Control:



**Treatment:** 



## A/B test results

- The treatment group (no ad) got 43.4% more purchases than the control group (with ad)
- Intuition that "showing an ad would increase sales" was false
- Was this result statistically significant or just chance?
- Need EA's data to determine this
- Techniques from Sampling in Python + this course to do so

# Stack Overflow Developer Survey 2020

```
import pandas as pd
print(stack_overflow)
```

```
respondent
                 age_1st_code ...
                                          hobbyist
                                     age
           36.0
                         30.0
                              ... 34.0
0
                                               Yes
           47.0
                         10.0 ... 53.0
                                               Yes
           69.0
                         12.0 ... 25.0
                                               Yes
3
          125.0
                         30.0 ... 41.0
                                               Yes
          147.0
                         15.0 ... 28.0
                                                No
                                               Yes
2259
        62867.0
                         13.0
                              ... 33.0
                         13.0 ... 28.0
2260
        62882.0
                                               Yes
[2261 rows x 8 columns]
```

# Hypothesizing about the mean

A hypothesis:

The mean annual compensation of the population of data scientists is \$110,000

The point estimate (sample statistic):

```
mean_comp_samp = stack_overflow['converted_comp'].mean()
```

119574.71738168952

# Generating a bootstrap distribution

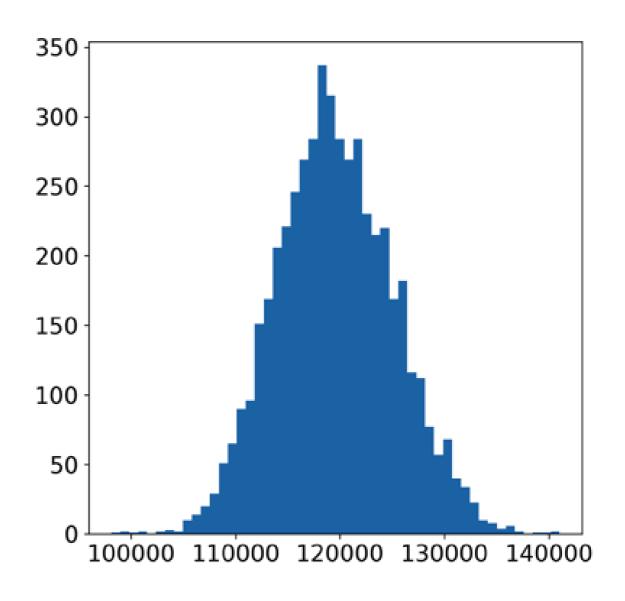
```
import numpy as np
# Step 3. Repeat steps 1 & 2 many times, appending to a list
so_boot_distn = []
for i in range(5000):
  so_boot_distn.append(
    # Step 2. Calculate point estimate
    np.mean(
        # Step 1. Resample
        stack_overflow.sample(frac=1, replace=True)['converted_comp']
```

<sup>&</sup>lt;sup>1</sup> Bootstrap distributions are taught in Chapter 4 of Sampling in Python



# Visualizing the bootstrap distribution

```
import matplotlib.pyplot as plt
plt.hist(so_boot_distn, bins=50)
plt.show()
```



## Standard error

```
std_error = np.std(so_boot_distn, ddof=1)
```

5607.997577378606



#### **z-scores**

$$\frac{\text{standardized value}}{\text{standard deviation}} = \frac{\text{value} - \text{mean}}{\text{standard deviation}}$$

$$z = \frac{\text{sample stat} - \text{hypoth. param. value}}{\text{standard error}}$$

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stack\_overflow['converted\_comp'].mean()

#### 119574.71738168952

 $mean\_comp\_hyp = 110000$ 

std\_error

#### 5607.997577378606

z\_score = (mean\_comp\_samp - mean\_comp\_hyp) / std\_error

#### 1.7073326529796957



# Testing the hypothesis

- Is 1.707 a high or low number?
- This is the goal of the course!

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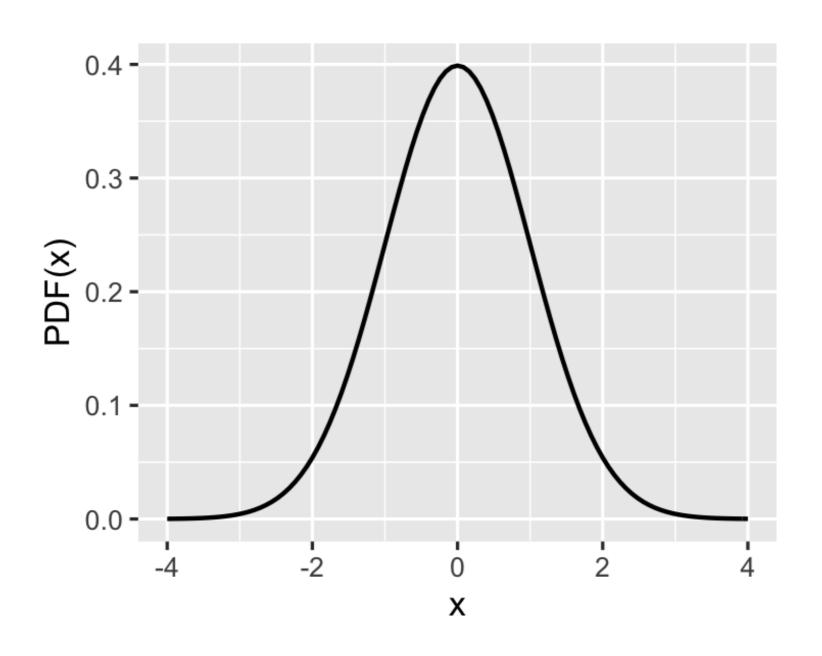
#### Hypothesis testing use case:

Determine whether sample statistics are close to or far away from expected (or "hypothesized" values)



# Standard normal (z) distribution

Standard normal distribution: normal distribution with mean = 0 + standard deviation = 1



# Let's practice!

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# p-values HYPOTHESIS TESTING IN PYTHON



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## **Criminal trials**

- Two possible true states:
  - 1. Defendant committed the crime
  - 2. Defendant did not commit the crime
- Two possible verdicts:
  - 1. Guilty
  - 2. Not guilty
- Initially the defendant is assumed to be not guilty
- Prosecution must present evidence "beyond reasonable doubt" for a guilty verdict

# Age of first programming experience

- age\_first\_code\_cut classifies when Stack Overflow user first started programming
  - "adult" means they started at 14 or older
  - "child" means they started before 14
- Previous research: 35% of software developers started programming as children
- Evidence that a greater proportion of data scientists starting programming as children?

## **Definitions**

A hypothesis is a statement about an unknown population parameter

A hypothesis test is a test of two competing hypotheses

- The *null hypothesis* ( $H_0$ ) is the existing idea
- The alternative hypothesis ( $H_A$ ) is the new "challenger" idea of the researcher

For our problem:

- ullet  $H_0$ : The proportion of data scientists starting programming as children is 35%
- ullet  $H_A$ : The proportion of data scientists starting programming as children is greater than 35%

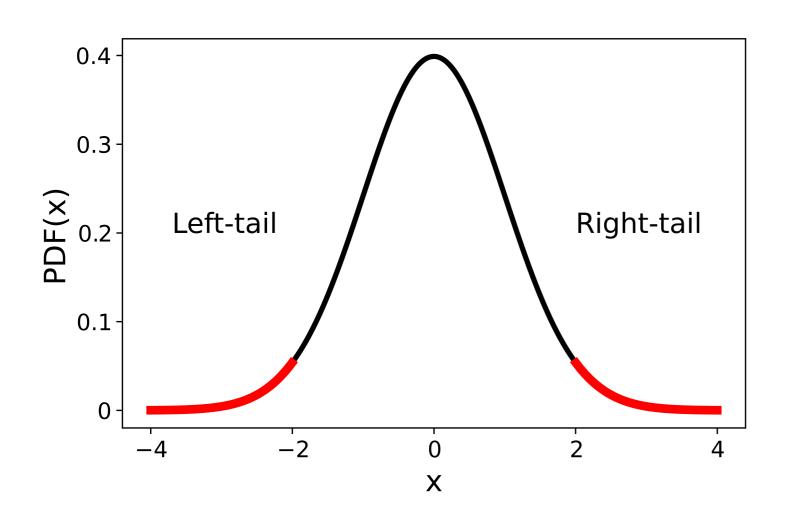
<sup>&</sup>lt;sup>1</sup> "Naught" is British English for "zero". For historical reasons, "H-naught" is the international convention for pronouncing the null hypothesis.



# Criminal trials vs. hypothesis testing

- Either  $H_A$  or  $H_0$  is true (not both)
- ullet Initially,  $H_0$  is assumed to be true
- ullet The test ends in either "reject  $H_0$ " or "fail to reject  $H_0$ "
- If the evidence from the sample is "significant" that  $H_A$  is true, reject  $H_0$ , else choose  $H_0$  Significance level is "beyond a reasonable doubt" for hypothesis testing

### One-tailed and two-tailed tests



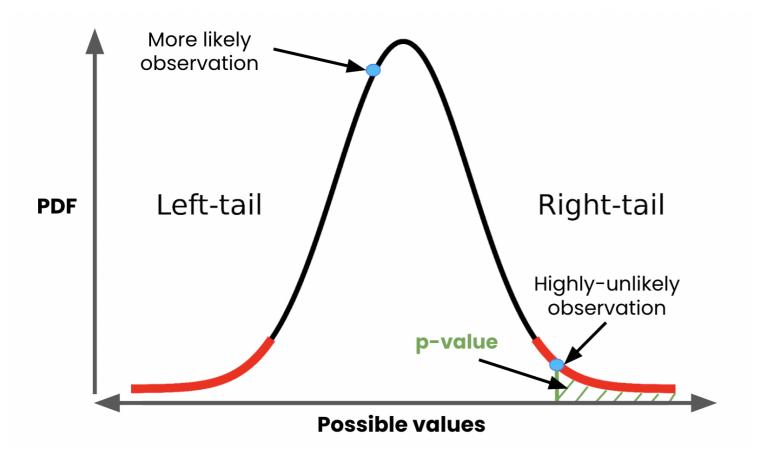
Hypothesis tests check if the sample statistics lie in the tails of the **null distribution** 

Test	Tails
alternative different from null	two-tailed
alternative <i>greater than</i> null	right-tailed
alternative <i>less than</i> null	left-tailed

 $H_A$ : The proportion of data scientists starting programming as children is **greater than** 35%

This is a **right-tailed** test

# p-values



**p-values**: probability of obtaining a result, assuming the null hypothesis is true

- ullet Large p-value, large support for  $H_0$ 
  - Statistic likely **not in** the tail of the *null* distribution
- ullet Small p-value, strong evidence against  $H_0$ 
  - Statistic likely in the tail of the null distribution
- "p" in p-value → probability
- "small" means "close to zero"

# Calculating the z-score

```
prop_child_samp = (stack_overflow['age_first_code_cut'] == "child").mean()
```

#### 0.39141972578505085

```
prop_child_hyp = 0.35
```

```
std_error = np.std(first_code_boot_distn, ddof=1)
```

#### 0.010351057228878566

```
z_score = (prop_child_samp - prop_child_hyp) / std_error
```

#### 4.001497129152506



# Calculating the p-value

- norm.cdf() is normal CDF from scipy.stats.
- Left-tailed test → use norm.cdf().
- Right-tailed test → use 1 norm.cdf().

```
from scipy.stats import norm
1 - norm.cdf(z_score, loc=0, scale=1)
```

3.1471479512323874e-05



# Let's practice!

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# Statistical significance

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# p-value recap

- p-values quantify evidence for the null hypothesis
- Large p-value → fail to reject null hypothesis
- Small p-value → reject null hypothesis
- Where is the cutoff point?

# Significance level

The *significance level* of a hypothesis test  $(\alpha)$  is the threshold point for "beyond a reasonable doubt"

- ullet Common values of lpha are 0.2, 0.1, 0.05, and 0.01
- If  $p \leq lpha$ , reject  $H_0$ , else fail to reject  $H_0$
- $\alpha$  should be set **prior** to conducting the hypothesis test

# Calculating the p-value

```
alpha = 0.05
prop_child_samp = (stack_overflow['age_first_code_cut'] == "child").mean()
prop_child_hyp = 0.35
std_error = np.std(first_code_boot_distn, ddof=1)
z_score = (prop_child_samp - prop_child_hyp) / std_error
p_value = 1 - norm.cdf(z_score, loc=0, scale=1)
```

3.1471479512323874e-05



# Making a decision

```
alpha = 0.05
print(p_value)
```

#### 3.1471479512323874e-05

p\_value <= alpha</pre>

#### True

Reject  $H_0$  in favor of  $H_A$ 

### Confidence intervals

For a significance level of  $\alpha$ , it's common to choose a confidence interval level of 1 -  $\alpha$ 

•  $\alpha = 0.05 \rightarrow 95\%$  confidence interval

```
import numpy as np
lower = np.quantile(first_code_boot_distn, 0.025)
upper = np.quantile(first_code_boot_distn, 0.975)
print((lower, upper))
```

(0.37063246351172047, 0.41132242370632466)

# Types of errors

	Truly didn't commit crime	Truly committed crime
Verdict not guilty	correct	they got away with it
Verdict guilty	wrongful conviction	correct

	actual $H_0$	actual $H_A$
chosen $H_0$	correct	false negative
chosen $H_A$	false positive	correct

False positives are *Type I errors*; false negatives are *Type II errors*.

# Possible errors in our example

If  $p \leq \alpha$ , we reject  $H_0$ :

- A false positive (Type I) error: data scientists didn't start coding as children at a higher rate If  $p>\alpha$ , we fail to reject  $H_0$ :
- A false negative (Type II) error: data scientists started coding as children at a higher rate

# Let's practice!

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