



SOLID PROPULSION PROGRESS REPORT: WEEKS 1 & 2

Week 1 Objectives

- **Orientation**
- **Go through the theory of solid motors**
- **Help in N3.5 launch preparation**
- **Understand N3.5 propulsion system**

Tasks completed in week 1

- Attending orientation meetings
- Reading solid motor theory - Richard Nakka
- Helped N3.5 team prepare for launch
- Installation and training on necessary software - Solidworks, Open Motor, Ansys, etc
- Solid propulsion system characterization for N3.5



Week 2 Objectives

- **Benchmarking solid motor designs**
- **Estimation of required impulse for target apogee**
- **Casing Design**
- **Design of grains and nozzle parameters using Open Motor**
- **Ansys Simulation of flow through nozzle**
- **Design of grain casting tools**
- **Improvements and SA Cup Requirements**
- **Design of Casting Tools**

Impulse estimation

Utilization of work-energy equations

Initial Grain Estimation.

Expected apogee $\approx 3.2 \text{ km} \pm 0.2 \text{ km}$
 Estimated total mass $\approx 22.5 \text{ kg} \pm 2.5 \text{ kg}$.
 Estimated burn time $\approx 2.5 \text{ seconds}$.

$$F(z_1 - z_0) = mg(z_2 - z_0) \quad \because z_0 = 0$$

$$Fz_1 = mgz_2 \quad \text{where } z_2 = \text{Apogee}$$

$z_1 = \text{Altitude at burnout.}$
 $F = \text{Average thrust.}$

$$z_2 = \frac{Fz_1}{mg} \quad \text{Unknown}$$

$$z_1 = \frac{1}{2} \left(\frac{F}{m} - g \right) t^2 \quad t = \text{burn time.}$$

$$V_1 = \sqrt{\frac{2z_1}{m} (F - mg)} \quad \sim \text{max velocity at Burnout.}$$

$$1. F = 1909.55 \text{ N}$$

```
Grain estimation.jl > interpolate_Fz
1 using Interpolations
2 using Plots
3
4 m = 22.5 #estimated mass (kg)
5 t = 3.6 #estimated burn time (s)
6 g = 9.8 #gravitational acceleration (m/s^2)
7 cd = 0.4 #drag coefficient
8 D = 11 #max rocket diameter (cm)
9 md = 17.5 #estimated rocket mass without grains (kg)
10
11 N_values = [0.0, 100, 200, 300, 400, 500, 600, 700, 800, 900, 1000]
12 Fz_values = [1.0, 0.82, 0.7, 0.62, 0.56, 0.52, 0.48, 0.44, 0.4, 0.38, 0.38]
13
14 # Create quadratic interpolation function
15 itp = LinearInterpolation(N_values, Fz_values)
16
17 # Define a function to interpolate Fz for any given N
18 function interpolate_Fz(N)
19     return itp(N)
20 end
21
22
23 #altitude at burnout
24 function burnout(F, m, g, t)
25     z1 = 0.5 * ((F / m) - g) * t^2
26     return z1
27 end
28
29 #Maximum altitude (apogee)
30 function apogee(F, z1, m, g)
31     z2 = (F * z1) / (m * g)
32     return z2
33 end
34
```

Apogee Estimation Results

```
Iteration80.0  
Thrust: 2000  
Altitude at burnout: 512.496  
Maximum altitude (apogee): 3163.933399184551  
velocity at burnout v1: 284.71999999999997  
Drag influence number N: 224.20395168914283
```

```
Iteration81.0  
Thrust: 2025  
Altitude at burnout: 519.696  
Maximum altitude (apogee): 3224.2658809073023  
velocity at burnout v1: 288.72  
Drag influence number N: 230.54783648914292
```

```
Iteration82.0  
Thrust: 2050  
Altitude at burnout: 526.89600000000001  
Maximum altitude (apogee): 3284.0852572420786  
velocity at burnout v1: 292.72  
Drag influence number N: 236.9802241462858
```

Burn time (estimate) = 3.6 s

Avg thrust required = 2025 N

Impulse required = 7290 Ns

Casing Design

Design and Burst Pressures for Rocket Motor Casing

[Input data in blue text, English or (SI) units]

Casing Dimensions and Design Factors

$D_o = 100$ in. (mm) Diameter, outside
 $t = 5$ in. (mm) wall thickness
 $S_D = 2$ Design Safety factor

Material Properties

$F_{ty} = 210$ ksi (MPa) Yield Strength
 $F_{tu} = 240$ ksi (MPa) Ultimate Strength
 $E = 68900$ Msi (MPa) Modulus of Elasticity
 $\nu = 0.33$ Poisson Ratio

$\beta = 0.875$ F_{ty}/F_{tu}
 $B = 1.284$ Burst factor

Design and Burst Pressures

$P_D = 10500$ psi (kPa) Design pressure
 $P_U = 26955$ psi (kPa) Burst pressure
 $S_U = 2.57$ Burst Safety Factor

Elastic Deformation under Pressure *

Casing
 Material: Aluminum 6063 T6
 Supplier: Keps Metal
 Yield strength $F_y = 210$ MPa
 Ultimate strength $F_u = 240$ MPa
 $E = 68900$ MPa
 $\nu = 0.33$

S_D (Design safety factor)
 $= 2$

Burst Factor, $B = 1.284$

$$\beta = \frac{F_y}{F_u} = 0.875$$

D_o (outside diameter) = 100 mm
 thickness, $t = 5$ mm

$$\text{Design pressure, } P_D = 2 \frac{t F_y}{D_o S_D}$$

$$P_D = \frac{2 \times 5 \times 210}{100 \times 1.284} = 16.35 \text{ MPa}$$

$$\text{Burst pressure, } P_U = 2 \times t \frac{F_u}{D_o} \cdot B$$

$$= \frac{2 \times 5 \times 240 \times 1.284}{100} = 30.82 \text{ MPa}$$

Check:

$$P_D = 10500 \text{ psi} \quad \therefore 10500 \times 10.5 = \frac{2 \times t \times 210}{100 \times 1.284}$$

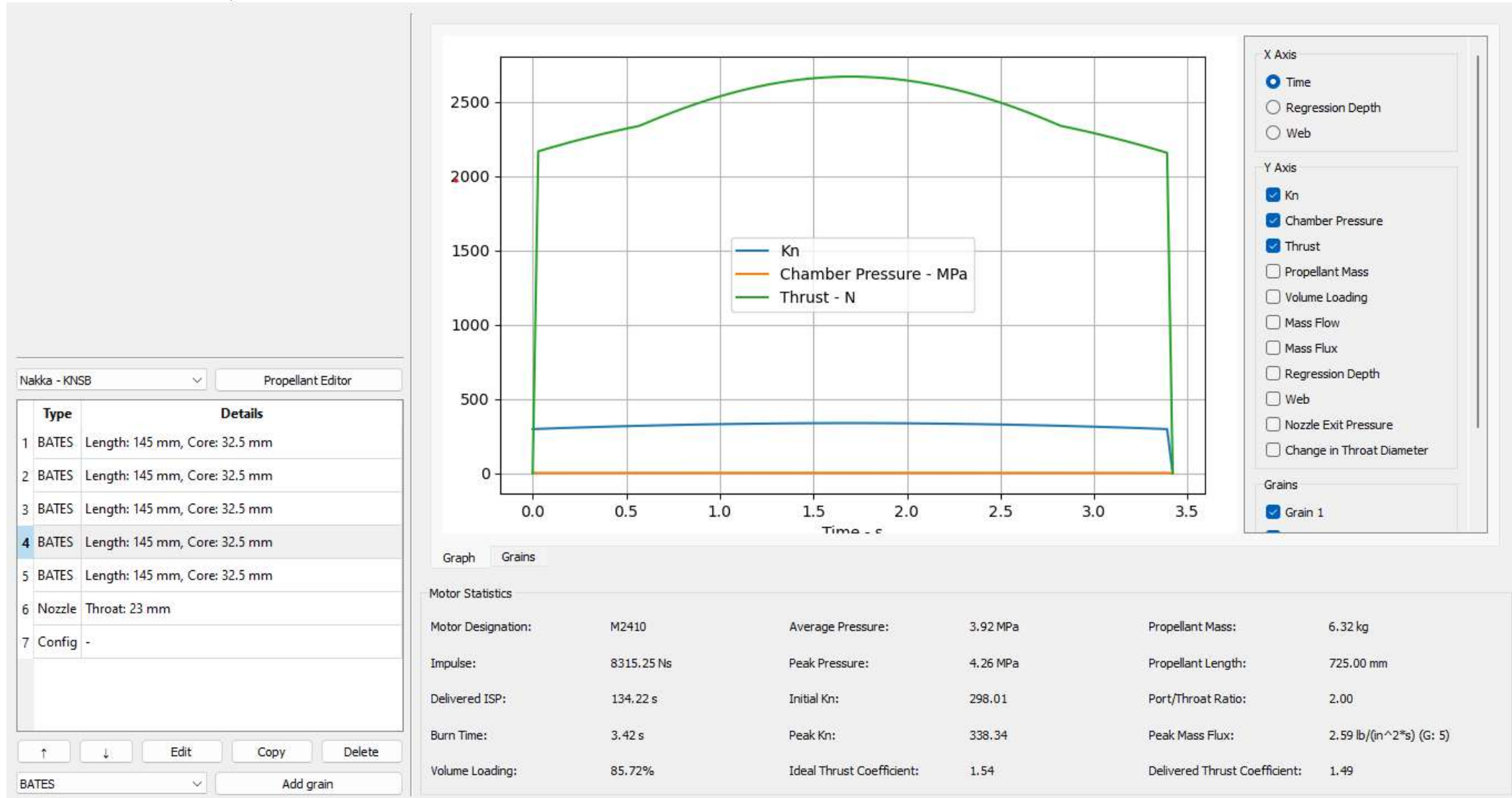
$$\therefore t = 8.21 \text{ mm}$$

$$P_U = 26955 \text{ kPa} \quad \therefore 26.96 = \frac{2 \times t \times 240 \times 1.284}{100}$$

$$\therefore t = 4.37 \text{ mm}$$

Aluminum 6063 T6

Design of Grains and Nozzle Parameters



Design of Grains and Nozzle Parameters

Chamber Pressure = 3.92 MPa

$$I_{sp} = \frac{I}{g \cdot m_p} = \frac{8345.25}{9.81 \times 2.32} = 134.22 \text{ (Open Motor)}$$

Mass flow rate: $\dot{m} = \frac{I}{I_{sp} \times g}$

$$\dot{m} = \frac{2431.36}{134.22 \times 9.81} = 1.8466 \text{ Kg/s}$$

Throat Area

$$A_t = \frac{\dot{m}}{P_c} \sqrt{\frac{R T_c}{\gamma}} \left(1 + \frac{\gamma - 1}{2} \right)^{\frac{\gamma + 1}{2(\gamma - 1)}}$$

$P_c = 3.92$

$Z = \frac{P_c}{M} \quad M = 33.618$

$R = \frac{8314}{33.618} = 215.238 \text{ J/kgK}$

$T_c = 1779 \text{ K}$

$\gamma = 1.1306$

$$A_t = \frac{1.8466}{3.92 \times 10^6} \sqrt{\frac{215.238 \times 1779}{1.1306}} \times \left(1 + \frac{0.1306}{2} \right)^{\frac{2.1306}{2(0.1306)}}$$

$$A_t = 0.0004593 = \frac{\pi d^2}{4}$$

$$d = \sqrt{\frac{4 \times 0.0004593}{\pi}} = 0.02419 \approx 24.18 \text{ mm}$$

$$\frac{A^*}{A_e} = \left(\frac{1.1306 + 1}{2} \right)^{\frac{1}{0.1306}} \left(\frac{0.101325}{3.92} \right)^{\frac{1}{1.1306}} \times \sqrt{\frac{2.1306}{0.1306} \left(1 + \frac{0.101325}{3.92} \right)^{\frac{0.1306}{1.1306}}}$$

$$\frac{A^*}{A_e} = 1.82312 \times 0.1037424 \times 2.37647 = 0.1517$$

$E_{cp} = 0.1517^{-1} = 6.5917$

$D_{eq} = \sqrt{6.5917 \times 24.18} = 62.08$

Code	WEIGHT	D-H	DENS	COMPOSITION
0 SUCROSE (TABLE SUGAR)	2212.000	-1550	0.05740	22 H 12 C 11 O
0 POTASSIUM NITRATE	4108.000	-1167	0.07670	1 N 3 O 1 K

THE PROPELLANT DENSITY IS 0.06862 LB/CU-IN OR 1.8995 GM/CC
 THE TOTAL PROPELLANT WEIGHT IS 6320.0000 GRAMS

NUMBER OF GRAM ATOMS OF EACH ELEMENT PRESENT IN INGREDIENTS

142.164400 H
 77.544200 C
 40.629820 N
 192.971600 O
 40.629820 K

*****CHAMBER RESULTS FOLLOW *****

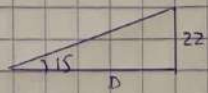
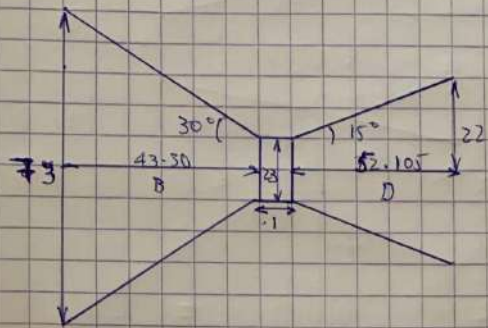
T(K)	T(F)	P(ATM)	P(PSI)	ENTHALPY	ENTROPY	CP/CV	GAS	RT/V
1703	2606	38.71	569.00	-8222.64	10660.18	1.1349151.569	0.255	

SPECIFIC HEAT (MOLAR) OF GAS AND TOTAL = 10.511 14.861
 NUMBER MOLS GAS AND CONDENSED = 151.569 18.878

5.000043e+001 H2O	3.368403e+001 CO	2.497893e+001 CO2	2.031121e+001 N2
1.972611e+001 H2	1.887710e+001 K2CO3*	2.665177e+000 KHO	1.788783e-001 K
1.427333e-002 K2H2O2	3.709072e-003 NH3	1.329761e-003 H	1.161684e-003 KH
5.974830e-004 KCN	1.795201e-004 HO	1.630892e-004 CH4	1.250677e-004 CH2O
0.000119285 CNH			

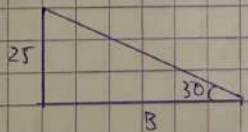
THE MOLECULAR WEIGHT OF THE MIXTURE IS 37.079

Design of Grains and Nozzle Parameters



$$\tan 15 = \frac{22}{D}$$

$$D = \frac{22}{\tan 15} = 52.105 \text{ mm}$$



$$B = \frac{25}{\tan 30} = 43.30$$

Motor dimensions estimation

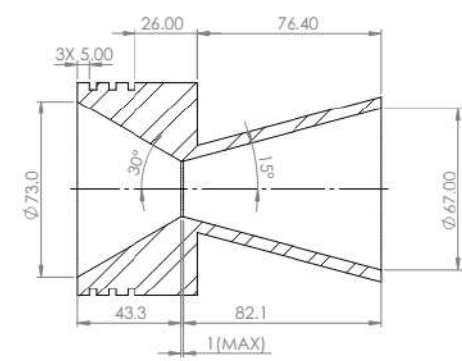
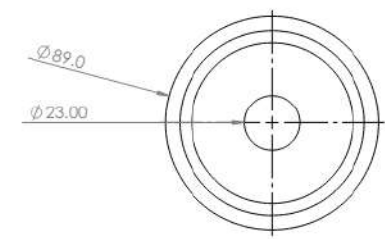
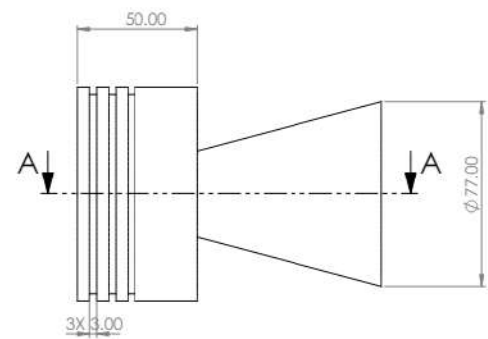
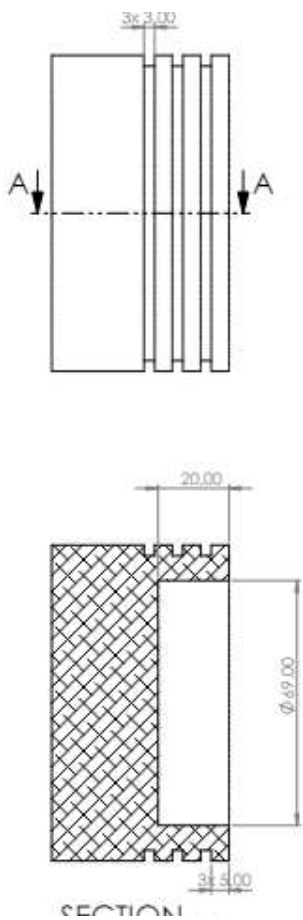
GRAIN SIZING				
Propellant	Number of grains	Outside diameter(mm)	Core diameter(mm)	Length $L = 1.5D + 0.5d$
KNSB	5	86	32.5	145.25

CASING SIZING			
Material	Outer diameter(mm)	Inner diameter(mm)	Length
Aluminum 6063 T6	100	90	825

BULKHEAD SIZING		
Material	Outer diameter(mm)	Length
Aluminum 6063 T6	89	50

NOZZLE SIZING					
Material	Outside diameter	Throat diameter	Exit diameter	Divergence half-angle	Convergence half angle
Mild Steel	89	23	67	15	30

Bulkhead and Nozzle drawing



UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS SURFACE FINISH TOLERANCES: LINEAR ANGULAR		FINISH	DIMENSIONAL TOLERANCES: SPECIFIC		REFERENCE
DESIGN	DATE	BY	DATE	BY	DATE
CHKD					
APP'D					
DATE					

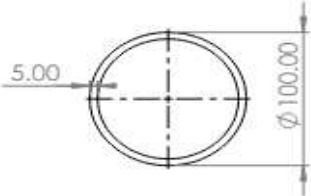
Motor Components

SECTION A-A
SCALE 1 : 1.5

UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS SURFACE FINISH TOLERANCES: LINEAR ANGULAR		FINISH	DIMENSIONAL TOLERANCES: SPECIFIC		REFERENCE
DESIGN	DATE	BY	DATE	BY	DATE
CHKD					
APP'D					
DATE					

Motor Components

Casing drawing



UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS SURFACE FINISH: TOLERANCES: UNLESS: ANGULAR:				FINISH:		DESIGN AND BREAK SHARP EDGES	DO NOT SCALE DRAWING		1
				NAME	SIGNATURE	DATE			
DESIGN	Oppendo		16/5/24				TITLE: Motor Assem		
CHECK									
APPROV									

Recommendations on N3.5 and SA Cup Requirements

Recommendations

- Measuring chamber pressure and temperature
- Measuring casing temperature
- Redesign of test stand
- Long storage and drying of grains

SA Cup Requirements

[SA Cup Requirements - Google Docs](#)

Challenges

- Simulation softwares
- Unergonomic seats

Next Week's Objectives

- Nozzle simulation (Ansys) and characterization
- Coming up with a components budget
- Procurements of casing, nozzle and bulkhead materials
- Test stand design
- Research on grain storage
- Design and 3D printing of Casting tools



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Credit: Andres Victorero