

Semiconductor

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Intrinsic Semiconductor \Rightarrow

Semiconductor without any impurities.

Ex. Si, Ge, \rightarrow Pure Crystals.

forbidden gap $\approx 1\text{ eV}$.

there are two possibilities for disappearance of
 e^-p from valence band to conduction band.

Applying

\rightarrow Electric field

\rightarrow thermal excitation.

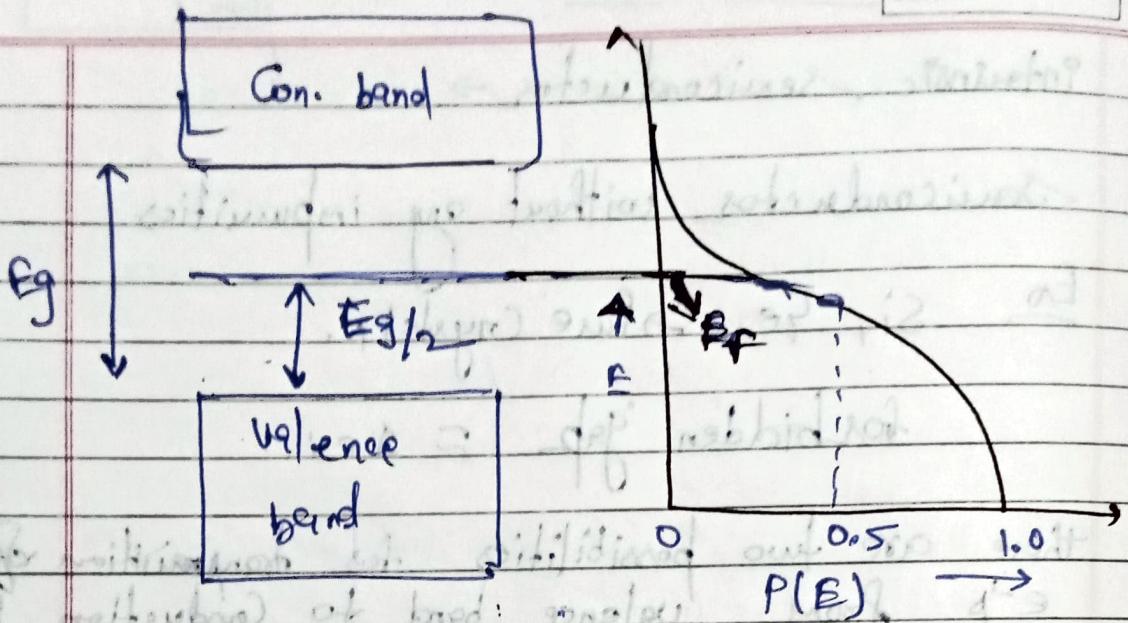
At room temp., the thermal energy that is available can excite a limited no. of electrons across the energy gap.

This limited no. of e^- accounts for semi-conduction.

No. of e^- excited given by
Fermi-Dirac probability distribution \rightarrow

$$f_0 = P(E) = \frac{1}{1 + e^{(E - E_F)/kT}}$$

E_F lies midway in forbidden gap for semiconductors.



Now we can conclude that

$$\therefore E - E_F = \frac{E_g}{2}$$

therefore

$$\therefore P(E) = N \exp\left[\frac{-E}{2KT}\right]$$

Probability
of finding
 e^-
let.

$$P(E) = n$$

{ 1 can be neglected
as it is very small
in comparison to exp

then

$$\therefore n = N \exp\left[\frac{-E_g}{2KT}\right]$$

no. of e^-
available for
excitation.

The promotion of some of e^- across the gap leaves some vacant e^- sites in valence band. These are called holes.

$$N_e = N_h$$

Mobility = $\frac{\text{drift velocity}}{\text{field gradient}}$

$$\begin{cases} J_e = -n_e e \mu_e E \\ J_h = n_h e \mu_h \end{cases} \rightarrow J = \vec{J} = \vec{e} \vec{E}$$

$J_e = + n_e e \mu_e E \rightarrow$ dir of flow of e^- opposite to electric field.

$J_h = n_h e \mu_h E \rightarrow$ dir of hole (+ve charge) same as electric field.

$$\Rightarrow J = J_e + J_h$$

$$J = (n_e \mu_e + n_h \mu_h) e E \rightarrow \text{current density in semi-conductor}$$

$$(n_e = n_h) J = (n_e + n_h) n_e E \rightarrow \text{intrinsic semi-conductor}$$

- No. of charge carriers (e^- & holes) is given by eq ...

- This no. depends on temp. in an exponential way, therefore \uparrow very rapidly with \uparrow in temp.

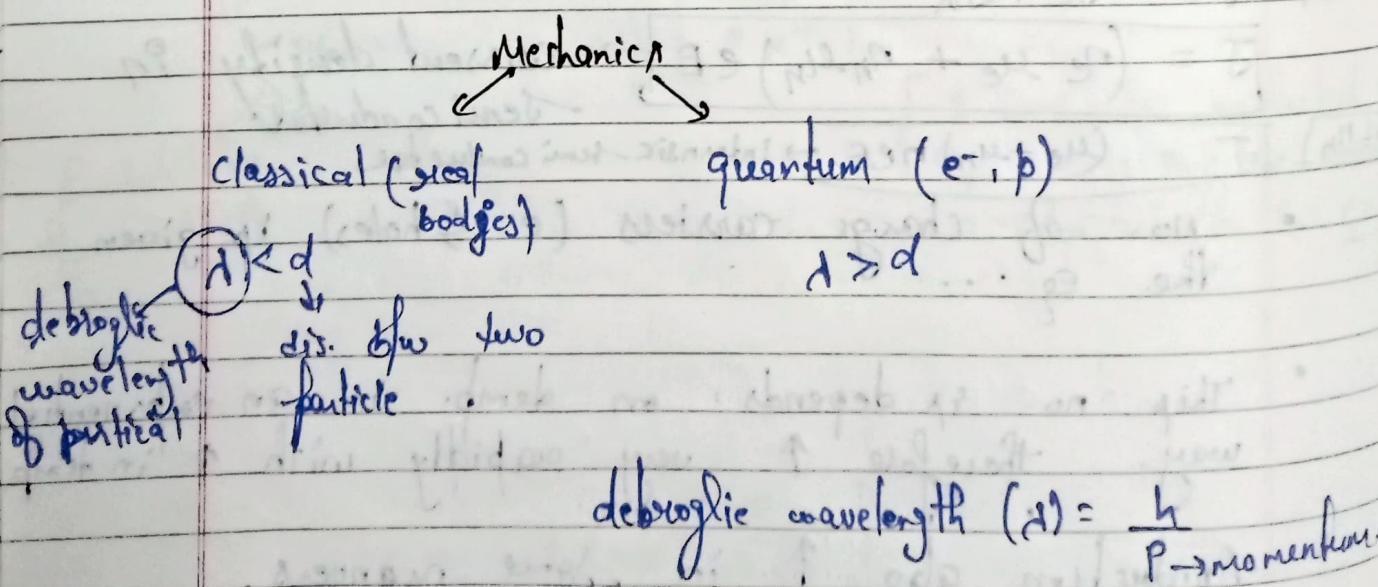
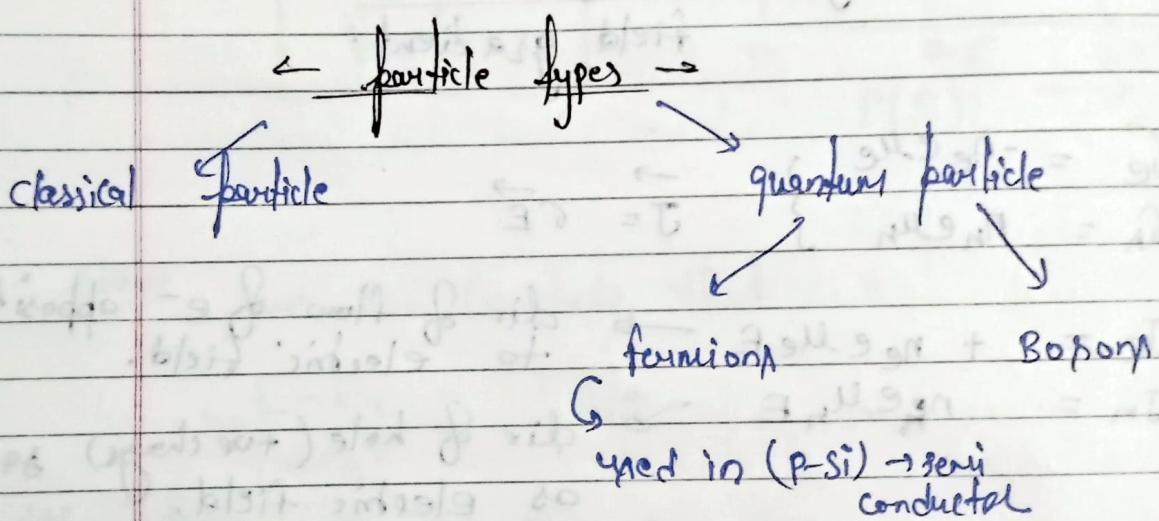
Conduction also \uparrow in same manner.

- plot of logarithm of conductivity against the reciprocal of temp. yields straight line.

- slope of this st. line give energy gap

to make free e^- we require 0.025 eV energy
 and at room temp. we have thermal energy
 $= 0.026\text{ eV}$.

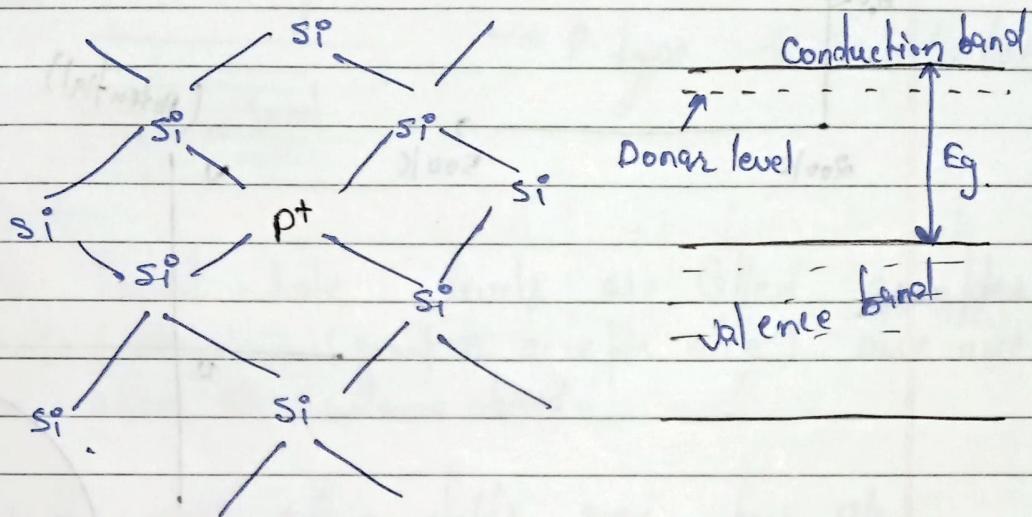
They we always have enough energy:



distribution function \rightarrow

$$f_{fd}(\epsilon) = \frac{1}{1 + e^{(\epsilon - \epsilon_f)/kT}} \rightarrow \text{finding of particle}$$

Extrinsic Semiconductor →
the conduction is due to the presence of extraneous impurities.



$n_e \neq n_n$

$$J = (n_e v_e + n_n v_n) e E$$

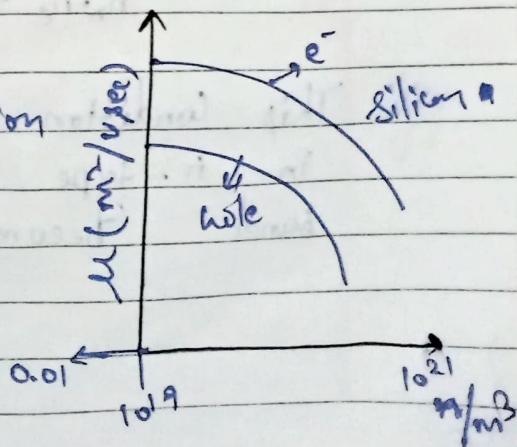
if $n_e > n_n \rightarrow n$ type
due to pentavalent

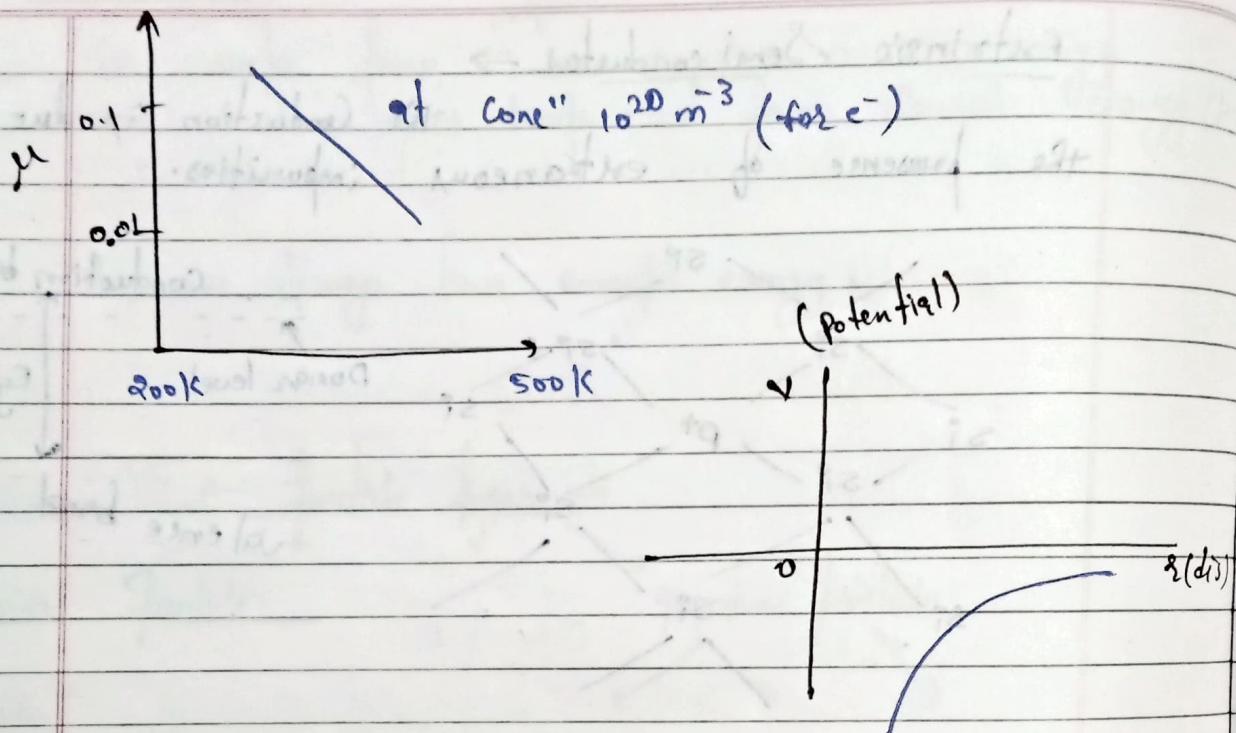
$n_n > n_e \rightarrow p$ type
due to divalent
impurity

$$\mu_I \propto T^{3/2} \quad \& \quad \mu_L \propto T^{-3/2}$$

mobility depends upon →

- (i) impurity concentration
- (ii) temperature





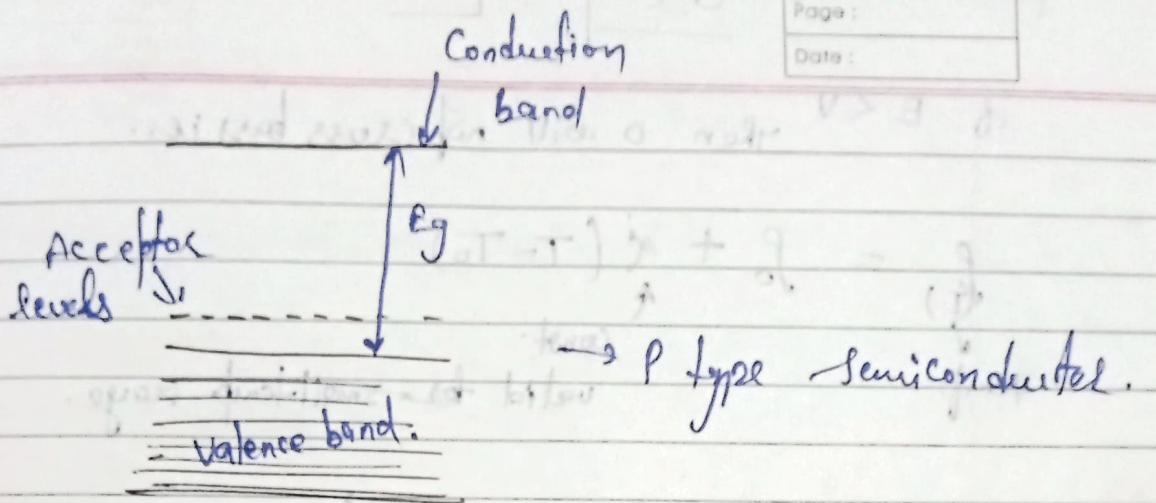
- Silicon atoms in diamond cubic structure. four of five electrons in the outermost orbital of the phosphorous atom take part in the tetrahedral bonding with the four silicon bonding.

Acc. to law of mass action, the product of no. of e^- in the conduction band and the no. of holes in the valence band must be constant.

i.e.

$$n \cdot n_e = \text{constant}$$

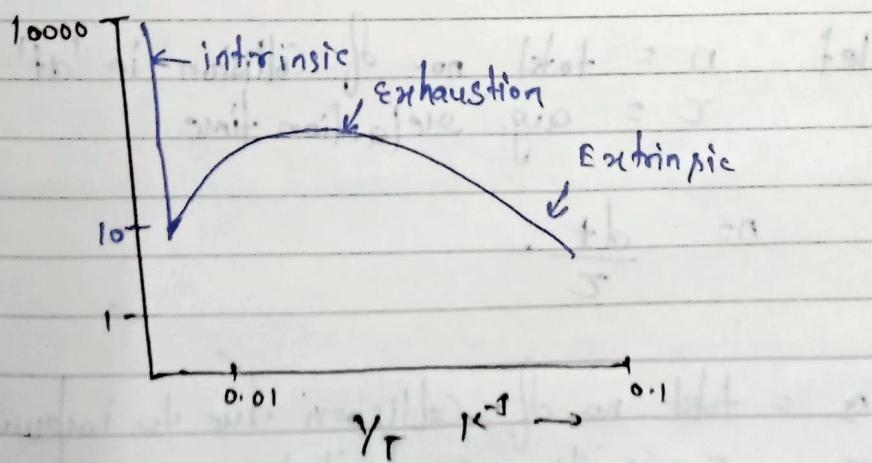
This condition drastically reduces the no. of hole in n-type semiconductor. e^- in conduction band become the majority charge carriers.



The bound-hole levels are called acceptor levels (Aluminium (group 13) accepts an e^-) are just above the valence band.

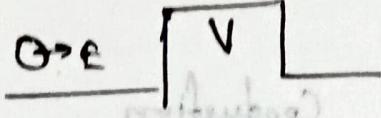
- law of mass action holds good here also.

A typical plot of the logarithm of conductivity against temp.



from the slope of st. lines ionization energy of the impurities can be calculated.

Quantum tunneling



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If $E < V$ then σ will not cross barrier.

$$\rho_t = \rho_0 + \alpha (T - T_0)$$

↑ const.

valid for small-temp range.

due to impurity / lattice vibration

additive nature of resistivity \rightarrow

$$\rho = \rho_I + \rho_L + \rho_D$$

$$\rho = \frac{1}{\sigma} = \frac{1}{neu} = \frac{E}{nev} = \frac{\tau}{e}$$

Resistance \rightarrow come due to scattering of charge carriers

let n = total no. of collision in 'dt' time:
 τ = avg. relaxation time

$$n = \frac{dt}{\tau}$$

n_I = total no. of collision due to impurity in time
 τ_I = avg. time (impurity)

$$n_I = \frac{dt}{\tau_I}$$

similarly n_L & τ_L for lattice

$$n_L = \frac{dt}{\tau_L}$$

$$n = n_I + n_L$$

$$\frac{dt}{\tau} = \frac{dt}{\tau_I} + \frac{dt}{\tau_L} = \frac{1}{\tau} = \frac{1}{\tau_I} + \frac{1}{\tau_L}$$

Extra: other than this class.

force on e-

$$F = -eE = m_e^* \frac{dv}{dt}$$

$$\int_0^V dv = \int_0^T \frac{-eE dt}{m_e^*} \Rightarrow$$

$$V = \frac{-eET}{m_e^*}$$

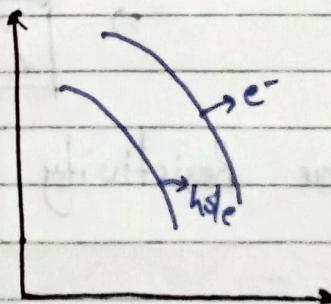
$$V_d = \frac{-eET}{m_e^*}$$

drift
velocity

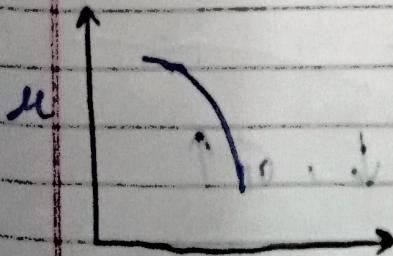
$$u_I \propto T^{3/2}$$

$$\& u_L \propto T^{-3/2}$$

$$\begin{matrix} u \\ \uparrow \\ \text{overall} \end{matrix}$$



concentration



$$\frac{1}{\tau} = \frac{1}{\tau_I} + \frac{1}{\tau_L}$$

avg. velo
time

$$\frac{1}{\tau} = \frac{1}{\tau_I} + \frac{1}{\tau_L}$$

$$\frac{1}{\mu_{M^*}} = \frac{1}{\mu_I(\text{e})} + \frac{1}{\mu_L(\text{e})}$$

$$\Rightarrow \boxed{\frac{1}{\mu} = \frac{1}{\mu_I} + \frac{1}{\mu_L}}$$

$$V_d = \frac{-eE\tau}{n*}$$

$$\tau = \frac{V_d \cdot N^*}{-eE}$$

$$\tau = -\left(\frac{V_d}{E}\right) \cdot \frac{N^*}{e}$$

$$\boxed{\tau = -\frac{\mu_{M^*}}{e}}$$

$$\boxed{\mu = \frac{n_I n_L}{n_I + n_L}}$$

$$\frac{1}{n \mu e} = \frac{1}{n_I \mu I e} + \frac{1}{n_L \mu L e}$$

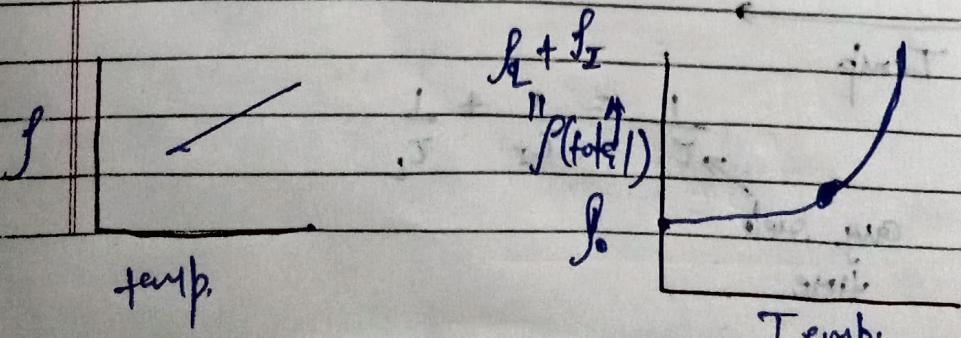
$$\Rightarrow \frac{1}{\sigma} = \frac{1}{\sigma_I} + \frac{1}{\sigma_L} \quad (\because \sigma = \frac{1}{n \mu e})$$

$$\Rightarrow \boxed{\rho = \rho_I + \rho_L}$$

Hence Resistivity is additive in nature.

$$\rho_E = \frac{1}{n_e e \mu} \propto \mu \propto \frac{1}{T^{3/2}}$$

as temp. \downarrow $\mu \uparrow$ & $\rho_L \downarrow$, $\sigma_L \uparrow$



$$\mu_I = T^{3/2}$$

N_I

if remain almost const.
at all temp. or
have a minor change
can be neglected.

* Velocity of e^- in 'moving' (v)

$$= \sqrt{\frac{3kT}{m_e}}$$

$$f = ma$$

$$-eE = Ma$$

$$a = -\frac{eE}{m}$$

Acc. when we
apply electric field

u = initial velocity of e^-
 v = velocity of e^-

$$v = u + at$$

$$u + \left(-\frac{eE}{m}\right)t$$

$$\langle v \rangle = \langle u \rangle + \left(-\frac{eE}{m}\right)\langle t \rangle$$

V_d

$$\Rightarrow V_d = \left(-\frac{eE}{m_e^*}\right)\tau$$

ohm's law \rightarrow

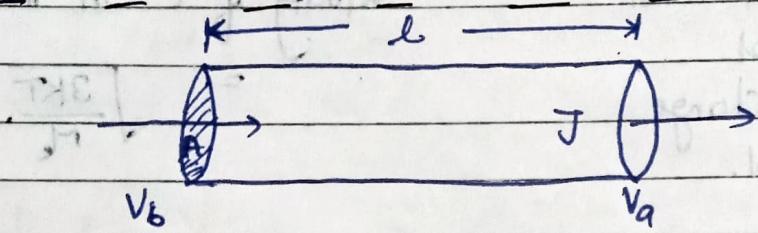
$$J = \sigma E \quad (i)$$

$$= -neuF = -nevD$$

$$J = -ne \left(-\frac{eE}{m_e^*}\right)\tau = \frac{ne^2 F \tau}{m_e^*}$$

$$\Rightarrow J = \left(\frac{ne^2 \tau}{m_e^*}\right) F \quad (ii)$$

$$\sigma = \frac{n e^2 \tau}{M e^*} \rightarrow \text{debye Model.}$$



$$\Delta V = v_b - v_a = \int_{a}^{b} E \cdot dl = E(l)$$

$$\Rightarrow \sigma = \frac{\Delta V}{E}$$

$$J = \sigma E$$

$$J = \frac{\sigma \cdot \Delta V}{l} \Rightarrow \Delta V = \frac{J \cdot l}{\sigma} = \frac{I \cdot l}{A \cdot \sigma} = I \left(\frac{l}{A} \right)$$

$$\Rightarrow \Delta V = IR$$

Conductivity

or

$$J = \sigma E \Rightarrow J \propto E$$

$$\text{When } \sigma = \frac{n e^2 \tau}{M e^*}$$

$$\frac{I}{A} = \sigma \frac{\Delta V}{l} \Rightarrow \Delta V = \left(\frac{pl}{A} \right) I$$

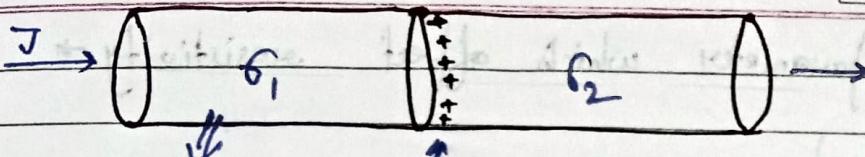
$$\Delta V = IR$$

$$J = \sigma E$$

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$$\sigma_1 > \sigma_2$$

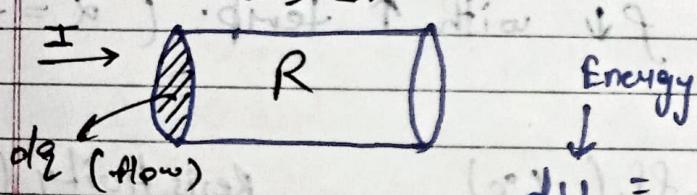


will have more

no. of charge carriers.
i.e. e^-

$$J = \sigma_2 E_2 = \sigma_1 E_1$$

$$E_2 = \frac{\sigma_1 E_1}{\sigma_2}$$



$$dU = dq \cdot \Delta V$$

$$P = \frac{dU}{dt} = \left(\frac{dq}{dt} \right) \cdot \Delta V = I \cdot \Delta V$$

$$P = T \cdot I R$$

$$P = I^2 R$$

** Some values.

$$\sigma_{Cu} = 5.81 \times 10^7 \text{ S/m}$$

$$\sigma_{Al} = 3.55 \times 10^7 \text{ S/m}$$

The parameter which affect resistivity →

(i) Temperature →

ρ will change with temp. acc. to given relation.

$$\rho(T) = \rho(T_0) [1 + \alpha (T - T_0)]$$

for metal $\rightarrow \rho \uparrow$ with \uparrow temp. ($\alpha = -ve$)

for semiconductor $\rightarrow \rho \downarrow$ with \uparrow temp. ($\alpha = +ve$)

Metal	Temp. Coff. ($^{\circ}\text{C}$)	Resistivity (Ωm)
Silver	0.0061	1.59×10^{-8}
Copper	0.0068	1.69×10^{-8}
Gold	0.0034	2.44×10^{-8}
Aluminium	0.00429	2.65×10^{-8}
Graphite	- 0.0005	$\rho \uparrow$ very fastly.
Germanium	- 0.05	
Si	- 0.07	

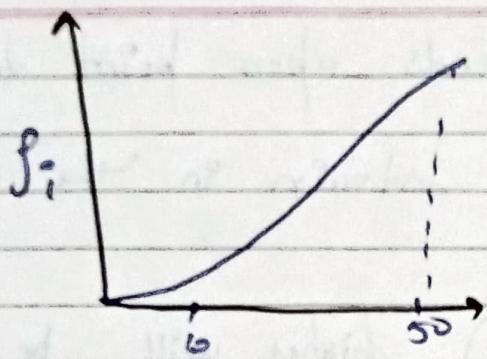
(ii) Alloying →

Alloy \rightarrow solid solution

$$f_i = A(1 - C_i) C_i \quad (C_i \rightarrow \% \text{ conc} \text{ of impurity added.})$$

(Cu-Ni)

$A = \text{Const.}$



(iii) Volume fraction \rightarrow

$$\rho = f_A V_A + f_B V_B$$

volume fraction

A & B are two phases of same metal. (e.g. non metal.)

$$E_n = \left(n + \frac{1}{2}\right) \hbar \omega \leftarrow \text{discrete energy}$$

$$\rho = \hbar \omega = \frac{\hbar}{2\pi} \cdot \frac{2\pi}{\lambda} \Rightarrow \rho = \frac{\hbar}{\lambda}, E = \frac{\rho^2}{2m}$$

$$\Rightarrow E = \frac{\hbar^2 k^2}{2m}$$

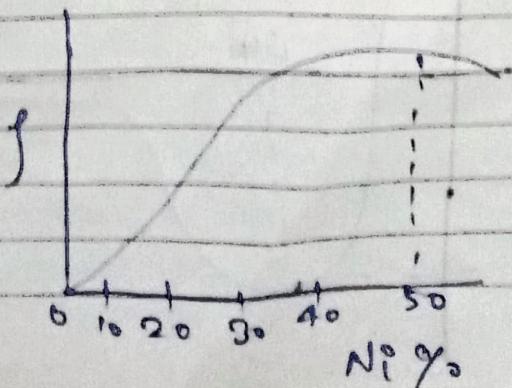
factors affecting Resistivity

impurity (i)

impurities \rightarrow

Ni in Cu

On adding impurities in metal it $\uparrow f_i$.



①) stress \rightarrow (it depends upon point defect)
 (gives rise to strain in the lattice)

More (higher strain) higher will be resistivity
 (due to twisting a metal piece)
 to solve the this problem

Annealing process \rightarrow

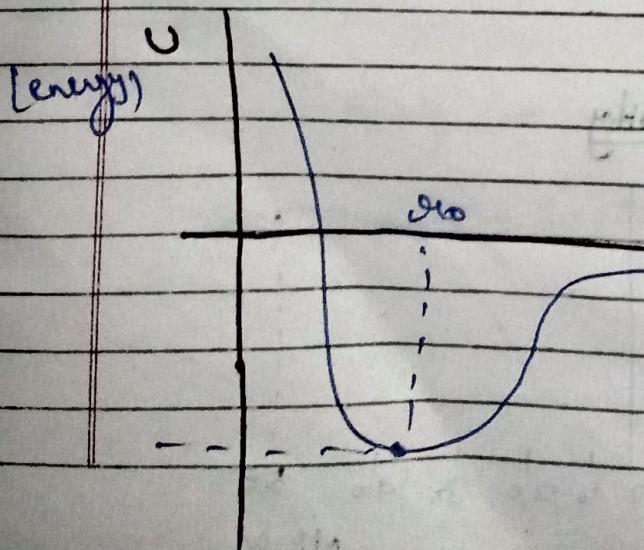
(used for)

to remove local strain
 if will decrease as strain is removed

^{twisted}
 \rightarrow heat metal at higher temp. below melting
 temp. and then cool it at room
 temp.

(Note Resistivity will be noted at room temp.)

atoms will such that they have lowest energy



cvi

Age Hardening →

after adding small amount of impurity and heating for a long time at lower temp than its melting point.

strength will be more than pure solid.

- 1st add impurity.
- heat at higher temp.
- get a solid sol"
- then cool down.

$f \uparrow$ \propto impurities \uparrow

NOTE → In alloys impurities may not homogeneous but here it is.

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$$\rho = \rho_p + \rho_I + \rho_d \rightarrow \text{deformation}$$

↓ ↓ ↓
phonons impurities

(S.No)	Metals	Symbol	Resistivity ($\mu\Omega\text{-cm}$)	Temp. C_0 ($^{\circ}\text{C}$)	Temp. C_f ($^{\circ}\text{C}$)	Thermal Conductivity
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$$\rho = \rho_0 [1 + \alpha(T - T_0)]$$

S.N.O.	Metals	Symbol	Resistivity ($\mu\Omega\text{-cm}$)	temp. C_0 ($^{\circ}\text{C}$)	Thermal conductivity (W/mK)	density (g/cm^3)	M.P ($^{\circ}\text{C}$)
1.	Silver	Ag	1.58	0.0038	429	10.49	962
2.	Copper	Cu	1.68	0.00386	385	8.96	1085
3.	Gold	Au	2.21	0.0034	310	19.3	1064
4.	Aluminium	Al	2.65	0.00429	205	2.7	660

making
(electro deposition).

refined
because it
is purified

used in R&D
(Research field)
(base metal fine)

Generally, Cu
can not be soldering.

Thermal
Expansion
(Coefficient
($^{\circ}\text{C}$))

Since on

Cu ← 0.0000167
After
Al ← 0.00429

inf rain ()
 }
 infrent
 print

Qul 2 - 2
 on 7th June

~~39~~ 05.23 Geost

~~mmmm~~ At
 used for
 power (electricity) instead
 lamp formation.

- Al → ~~and~~ also used in Aircraft (due to light weight)
- Cu → ^(wire) used in housing item.
- to ↑ strength of wire, impurities are added.
- alloy (Si + Cu) so that No corrosion and irregularities.
- train overhead wire (cd in Cu)
 - ↓
 - in very low %.
 (0.8 to 1)%
- Silver - Tungsten (good for mech. strength and co-operations.)

Good Conductors

Ag, Cu, Au, Al → making wires.