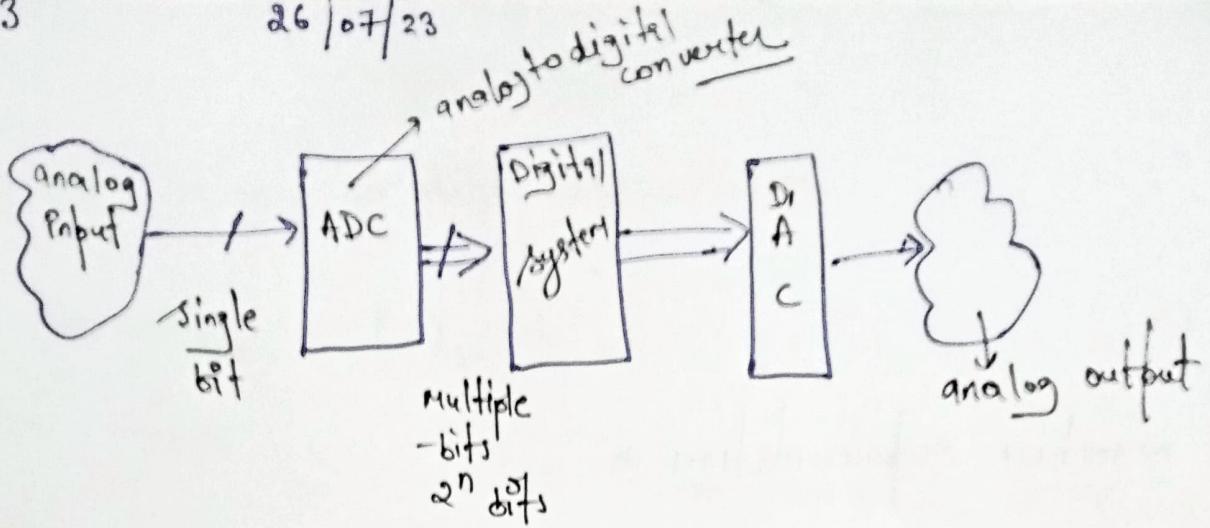


26/07/23



### Digital system →

Computer, Calculator, Digital clock,  
Digital voltmeter (measurement instrument)

How complex a system going to be depends on application.

e.g. take recent processor (speed is in GHz and complexity is enormous) and for washing machine (controller inside) is less.

### Basic Building Block of computer →

CPU, memory

input, output unit

cpu → ALU → ADD, sub, multiplier  
(Arithmetic)  
→ logic, control unit

systems → subsystems → modules

## Number Representation →

### Assumptions

1. we work with voltage (0 to 5V)

'0' → 0V switch off  
'1' → 5V switch on

for 3 switch,  $2^3 = 8$  level.

for  $n=2$ ,  $= 2^2 = 4$

00 → off off  
01 → off on  
10 → on off  
11 → on on

to ↑ accuracy ↑ no. of switch.

# Digital electronics

conversion a no. in diff base number.

Ex

$$(45.625)_{10} = (?)_2 = (?)_{10}$$

↓      ↓  
 45      0.625

	$x \rightarrow 2$	45	$\rightarrow 1$
2		22	$\rightarrow 0$
2		11	$\rightarrow 1$
2		5	$\rightarrow 1$
2		2	$\rightarrow 0$
2		1	$\rightarrow 1$

$$0.625 \times 2 = 1.250$$

$$1 \leftarrow 1.250$$

$$\Leftrightarrow 0.250 \times 2$$

$$0 \leftarrow 0.500$$

$$\cancel{0.500 \times 2} \rightarrow (0.625)_{10}$$

$$4 \leftarrow 1.00$$

$$= (0.101)_2$$

$$(45)_{10} = (101101)_2 = (231)_4$$

Now

$$(45.625) = (101101.101)_2$$

Binary to decimal system  $\rightarrow$

$$(101101.101)_2 = (?)_{10}$$

$$\begin{aligned}
 & 1 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \\
 & \times 0 \times 2^{-1} + 1 \times 2^{-2} \\
 & 32 + 8 + 4 + 1 + (0.5 + 0.025)
 \end{aligned}$$

$$(45.625)_{10}$$

$$\left\{
 \begin{array}{l}
 \text{eg. } (231.22)_4 = (?)_{10} \\
 \text{Binary} \\
 (101101.1010)_2 \\
 \text{or} \\
 2 \times 4^2 + 3 \times 4^1 + 1 \times 4^0 \\
 2 \times 4^{-1} + 2 \times 4^{-2} \dots
 \end{array}
 \right.$$

$$32 + 12 + 1 \cdot \frac{2}{4} + \frac{2}{16}$$

$$= 45.625$$

$x = \text{Base} \rightarrow$  always +ve integer.

$$(45)_{10} = (1011\ 01)_2$$

$$45 \quad = \quad x^5 + x^3 + x^2 + 1$$

## Representation of Number →

$\Rightarrow$  unsigned number  $8 + 8 = 8 = 1000.$

→ signed numbers → used in digit system (microprocessor)

$$9. \quad +8 = \textcircled{0} \overset{+ve}{1} 000$$

$$-8 = \begin{array}{|c|} \hline 1 \\ \hline \end{array} 1000 \quad \text{sign no. forget karne ke liye}\\ \text{-ve} \quad \text{Excess bit ki jostagi hogi.}$$

three method to rep signed number.

- 1) signed magnitude form
  - 2) 1's compliment form
  - 3) 2's compliment form

for binary.  
(base 2)

$(x-1)$ 's comp.

1's comp.

decimal	unsigned	signed	10's comp
+0	0 0	00	$\rightarrow +0$
+1	0 1	01	$\rightarrow +1$
+2	1 0	10	$\rightarrow -0$
+3	1 1	11	$\rightarrow -1$

first digit  $\rightarrow$  sign. neg.

1. signed magnitude form →

$$\text{e.g. } +4 = \begin{array}{c} 0 \\ \downarrow \text{sign} \\ 100 \end{array} \text{ & } -4 = \begin{array}{c} 1 \\ \downarrow \text{sign} \\ 100 \end{array} \text{ mag.}$$

→ sign. mag. form

$$\begin{array}{c} 0 \\ \downarrow \text{sign} \\ 101 \end{array} = +5 \quad \& \quad \begin{array}{c} 1 \\ \downarrow \text{sign} \\ 101 \end{array} = -5.$$

7 bit  
in 8 bit.      4 bit  
                to 8 bit

$$+5 = \begin{array}{c} 0 \\ \downarrow \text{sign} \\ 0000101 \end{array} \text{ & } -5 = \begin{array}{c} 1 \\ \downarrow \text{sign} \\ 0000101 \end{array} \text{ mag.}$$

Range of number →

$n=2$  bit → 4 binary possible

Binary	Decimal	Range → -1 to 1
0 0	+0	= (-1, -0, +0, +1)
0 1	+1	
1 0	-0	
1 1	+2	

$$\boxed{\text{for } n \text{ bit} = -(2^{n-1}-1) \text{ to } +(2^{n-1}-1)}$$

Range.

for  $n=3$  bit.

Range -3 to +3

$$= -3, -2, -1, -0, +0, +1, +2, +3.$$

but for unsigned

$$0 \rightarrow +7.$$

so always we should use

→ signed type.

Q. To rep.  $-4$  in signed form how much bit require. 6. ④

$$n=4 \quad \text{range} = -7 \text{ to } +7$$

$$n=5 \quad \text{range} = -15 \text{ to } +15$$

To rep.  $-4$  by signed mag. form, minimum 4-bit is required.

$$-4 = 1100 = 10000100$$

4 bit                    8 bit.

Disadvantage  $\rightarrow$

1. Two rep. different representation of zero +0, -0.
2. Calculation op not easy.

Ex.

$$\begin{array}{r} x = 1100 = -4 \text{ min. bit } = 4 \\ 0011 = +3 \text{ min. bit } = 3 \\ \hline 1111 \quad \hline -1 = 1001 = 11 = 101 \end{array}$$

$-7 \rightarrow$  wrong. ans.

Now to sol.

$$\begin{array}{r} x = -4 = 1100 \\ + y = -5 = 1101 \\ \hline = \underline{-9} \quad \hline \text{min.} \\ \text{5 bit} \\ \text{if neg.} \end{array}$$

2).  $(2^n - 1)$ 's or 1's complement  $\rightarrow$

$$+x = +x$$

$$-x = +\bar{x}$$

$$\text{eg. } +x = 0101 = x$$

$$+\bar{x} = 1010 = \bar{x}$$

$$\begin{array}{r} \bar{x} = \\ -0101 \leftarrow \text{given} \\ \hline 1010 \end{array}$$

↑  
 $\bar{x}$

let

$$x = +4 = 0100 \quad \text{4 bit.}$$

$$\bar{x} = -4 = 1011$$

8 bit

6 bit

$$00000100$$

copy of ↑

$$11111011$$

copy of ↑

$$000100$$

6 bit.

$$111011$$

In 1's complement form,  
signed magnitude }  $\rightarrow$  +ve no. = MSB = 0  
1's comp. } -ve no. = MSB = 1.

Range of 1's Complement  $\rightarrow$

for  $n=3$  bit

-3 to 3

$$= -3, -2, -1, -0, +0, +1, +2, +3.$$

for

$n$  bit = same as signed mag. form.

$$-(2^{n-1} - 1) \text{ to } + (2^{n-1} - 1)$$

• Glutation. possible.

disadvantage  $\rightarrow$

- Two diff' rep. of zero i.e.  $+0 \neq -0$
- Extra addition if neg. if carry is generated at time of addition operation.

(9-1)'s complement.

Q. 2)

$$(\text{62})_{10} \xrightarrow{\substack{9's \\ \text{comp.}}} \begin{array}{r} 99 \\ - 62 \\ \hline 37 \end{array}$$

$$\text{Q. 3)} (\text{62})_8 \xrightarrow{\substack{7's \\ \text{comp.}}} \begin{array}{r} 77 \\ - 62 \\ \hline 15 \end{array}$$

3). 2's complement form  $\rightarrow$  (9's complement).  $\rightarrow$   
(by 1)

$$+x = +x$$

$$-x = \overline{+x} + 1 = 1's \text{ comp.} + 1$$

$$\begin{array}{rcl} +7 & = & 0111 \\ +8 & = & 01000 \end{array} \left\{ \rightarrow \text{same as signed and 1's complement} \right.$$

g.

$$-7 = \overline{+7} + 1 = \overline{0111} + 0001 = 1000 + 0001$$

$$\boxed{-7 = 1001}$$

Binary Number → (2's comp)	decimal no.
	+0
00	+1
01	-2
10	-1
11	-1

$$(11000)_2 \underset{\substack{\downarrow \\ \text{2's comp}}}{} = (?)_{10}$$

-ve

$$= -x = \overline{+x} + 1 = y$$

$$+x = +x = y$$

$$-x = +\overline{x} = y - 1$$

$$x = \overline{y - 1}$$

for  $n = 2$  bit.

$$+ve = +0, +1$$

$$-ve = -1, -2$$

$$y = 11000$$

$$y-1 = 11000 - 00001$$

$$y-1 = 10111$$

$$x = \overline{y-1} = 01000$$

$$\boxed{-x = -8}$$

Range of number

$$-(2^{n-1}) \text{ to } (2^{n-1} - 1)$$

$$n = 2 \text{ bit} = -2 + 0 + 1$$

$$-2, -1, 0, 1$$

$$n = 4 \text{ bit} = -8 + 0 + 7$$

logic gates & Boolean Algebra →

one input logic gate →

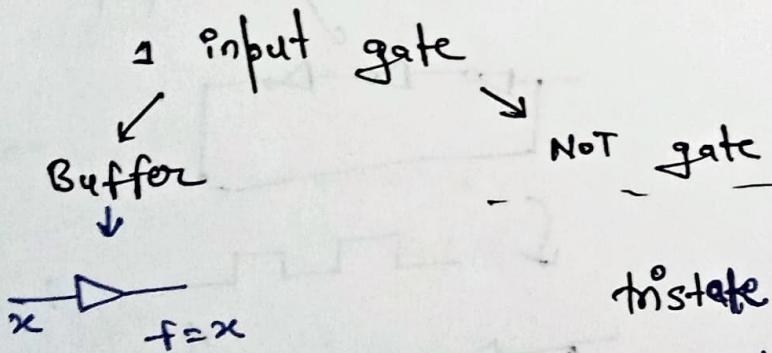
i/p x	f	f <sub>1</sub>	f <sub>2</sub>	f <sub>3</sub>	f <sub>4</sub>
0	0	0	1	1	0
0	1	0	0	0	1
1	1	0	1	0	0
1	0	1	0	0	1

→ <sup>no logic gate</sup>  
four ckt possible.

for n bit input  $2^n$  or  $2^{2n}$  output possible.

$$f \begin{cases} \rightarrow f_1 = 0 \\ \rightarrow f_2 = x \\ \rightarrow f_3 = \bar{x} \\ \rightarrow f_4 = 1 \end{cases}$$

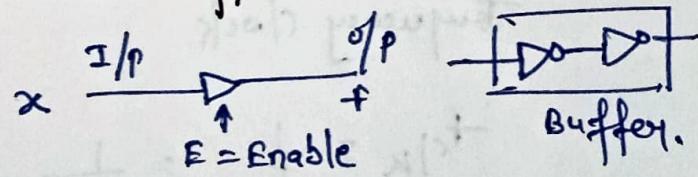
<sup>x</sup>  
<sup>Buffer</sup>  
<sup>not gate</sup>  
<sup>x</sup>



Truth table →

i/p	o/p
x	f
0	0
1	1

tristate buffer →



Enable E	I/p x	o/p f
0	0	Hi-Z
0	1	Hi-Z
1	0	0
1	1	1

} 3 state

• Provide delay

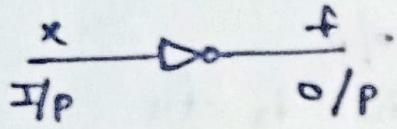
T.P.D.

• P.D. = Propagation

Delay

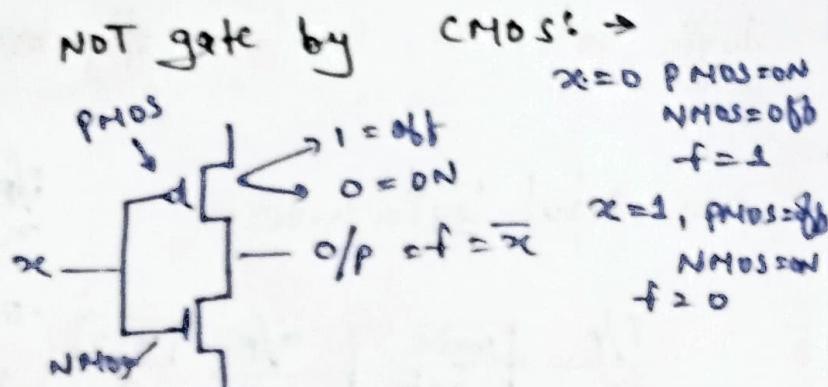
• if multiple buffers are arranged then effective will be sum.

ii. NOT gate: →



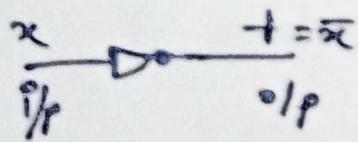
Truth Table

x	f = $\bar{x}$
0	1
1	0



$$\begin{aligned} \text{1 not gate} &= 1 \text{ PMOS} + 1 \text{ NMOS} \\ &= 1 \text{ CMOS} \\ &= 2 \text{ MOSFETs} \end{aligned}$$

If odd No. of NOT gate connected in cascade

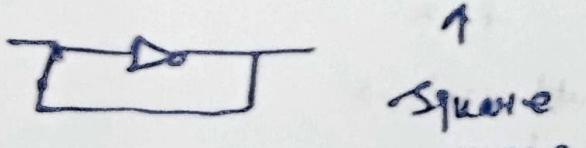
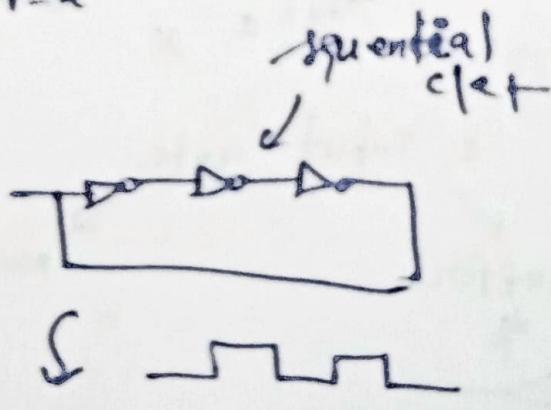


$$t = n \cdot t_{pd}$$

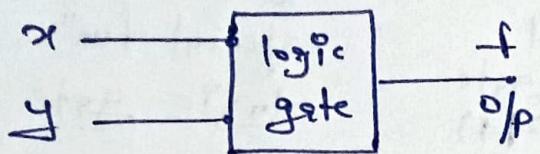
$\uparrow$   
avg

frequency clock

$$f_{clk} = \frac{1}{T_{clk}} = \frac{1}{2 \times n \times t_{pd}}$$



## 2 input logic gate



10<sup>th</sup> logic gate

Boolean functions  
 $2^{2n} = 16.$

as don't care logic gate

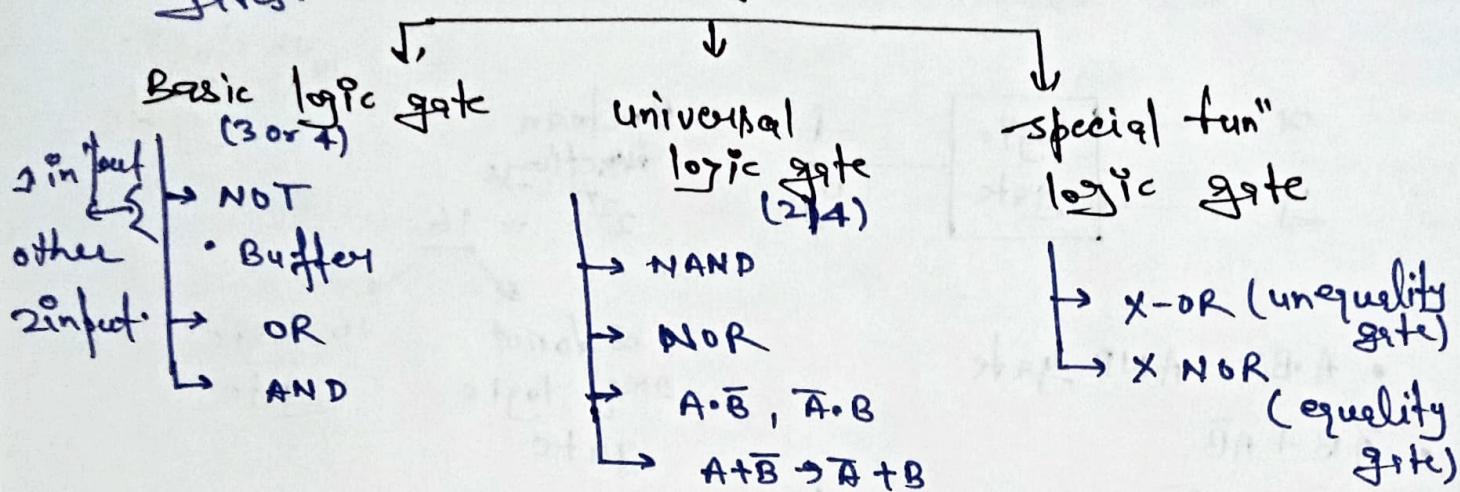
10 logic gate

- $A \cdot B = \text{AND gate}$
- $\bar{A}B + A\bar{B} = A \oplus B = X-\text{OR gate}$
- $A+B = \text{OR gate}$
- $\bar{A} \cdot \bar{B} = \overline{A+B} = \text{NOR gate}$
- $A \cdot B + \bar{A} \cdot \bar{B} = A \otimes B = X-\text{NOR gate}$
- $\bar{A} \cdot \bar{B} = \overline{A+B} = \text{NAND gate}$

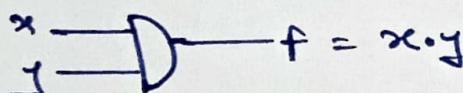
A	B	$f_1$	$f_2$	$f_3$	$f_4$	$f_5$	$f_6$	$f_7$	$f_8$						
0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1
0	1	0	0	0	1	1	1	0	0	0	0	1	1	1	1
1	0	0	0	1	1	0	0	1	0	0	1	1	0	0	1
1	1	0	1	0	1	0	1	1	0	1	0	1	0	1	0
		$A \cdot B$	$A \cdot \bar{B}$	$\bar{A} \cdot B$	$\bar{A} \cdot \bar{B}$	$\bar{A}B + A\bar{B}$	$\bar{A}B + A\bar{B} + AB$	$\bar{A}B + A\bar{B} + A\bar{B}$	$\bar{A}B + A\bar{B} + AB$	$\bar{A}B + A\bar{B} + AB + A\bar{B}$	$\bar{A}B + A\bar{B} + AB + A\bar{B} + AB$	$\bar{A}B + A\bar{B} + AB + A\bar{B} + AB + A\bar{B}$	$\bar{A}B + A\bar{B} + AB + A\bar{B} + AB + A\bar{B} + AB$	$\bar{A}B + A\bar{B} + AB + A\bar{B} + AB + A\bar{B} + AB + A\bar{B}$	$\bar{A}B + A\bar{B} + AB + A\bar{B} + AB + A\bar{B} + AB + A\bar{B} + AB$

~~2~~ 2 input logic gates.

logic gate

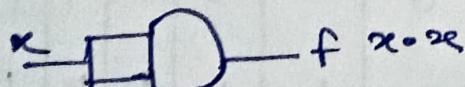


AND gate

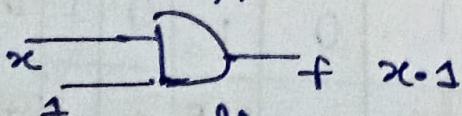


x	y	f = x·y
0	0	0
0	1	0
1	0	0
1	1	1

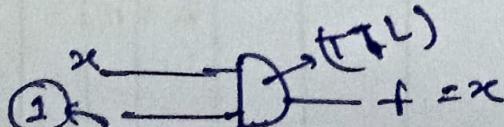
Majority o/p = 0



Buffer



Buffer.



(floating terminal) design by

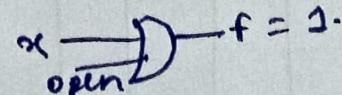
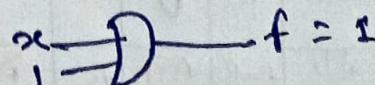
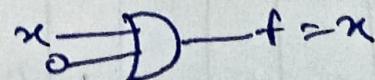
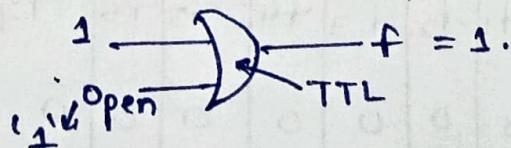
Can not define open output

OR gate



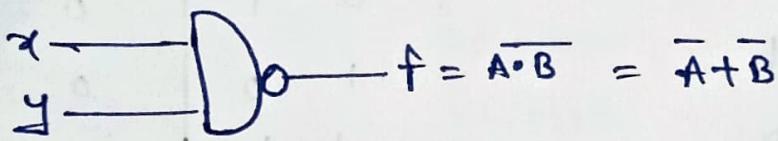
x	y	f = x+y
0	0	0
0	1	1
1	0	1
1	1	1

Majority o/p = 1.



## Universal logic gate

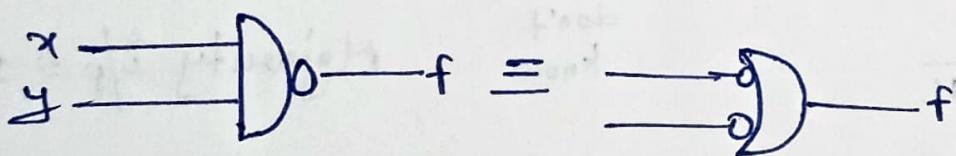
1.\* NAND gate →  
( AND + NOT )



$$f = \overline{A} + \overline{B} = \overline{A \cdot B}$$

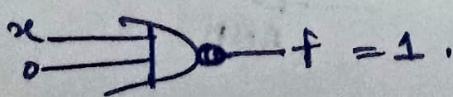
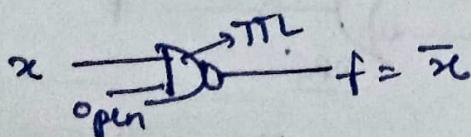
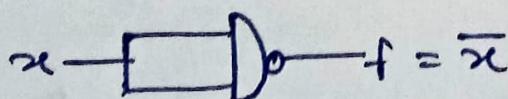
Bubbled (No)<sup>t</sup>) + OR

Bubbled or gate

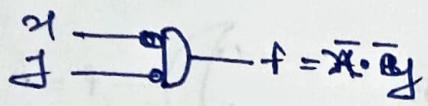
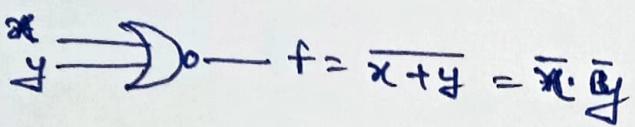


$x$	$Ax$	$f = \overline{Ax} + \overline{y}$
0	0	1
0	1	1
-1	0	1
1	-1	0

majority input = 0 = AND gate  
 (also).  
 ↓  
 O/P  
 ↓  
 1.  
 ↓  
 Here O/P  
 ↓  
 0

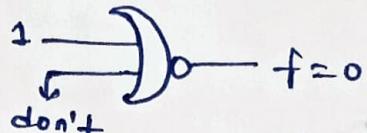
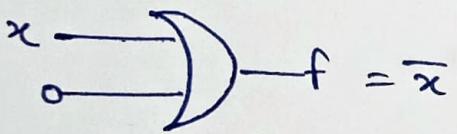


## Q2. NOR gate (OR + NOT) →



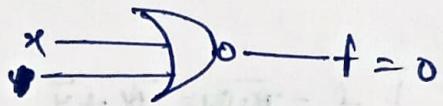
Bubbled AND

x	y	$f = \overline{x+y} = \overline{x} \cdot \overline{y}$
0	0	1
0	1	0
1	0	0
1	1	0

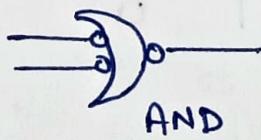
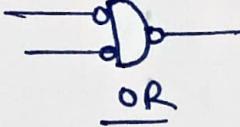


don't know

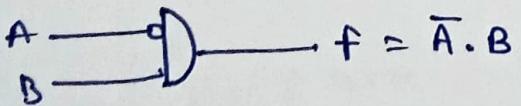
Majority  $i/p = 1$ .



$OR = NOR + NOT$
$AND = NAND + NOT$



## Q3. global 1 ( $A \cdot \overline{B}$ )



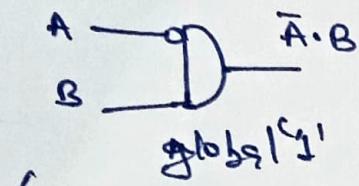
A	B	$f = \overline{A} \cdot B$
0	0	0
0	1	1
1	0	0
1	1	0

Majority  $i/p = NO$

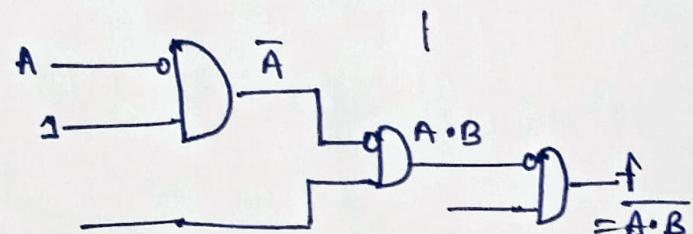
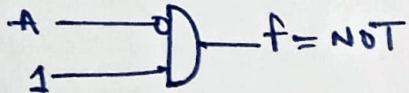
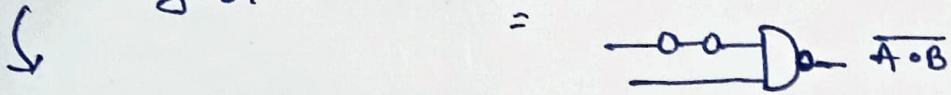
Can not define :-

$$\begin{aligned}
 & \overline{A} \cdot \overline{B} = \overline{A} \cdot \overline{B} \\
 & = \overline{A} \cdot \overline{B} \quad f \\
 & = \overline{A} \cdot f \\
 & = \overline{A} \quad f \\
 & = \text{OR} \\
 & = \text{AND}
 \end{aligned}$$

NAND gate by global '1'  $\rightarrow$

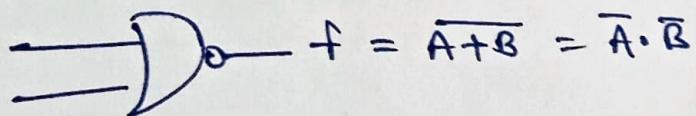


$$\text{NAND} = \overline{A \cdot B} = \bar{A} + \bar{B}$$

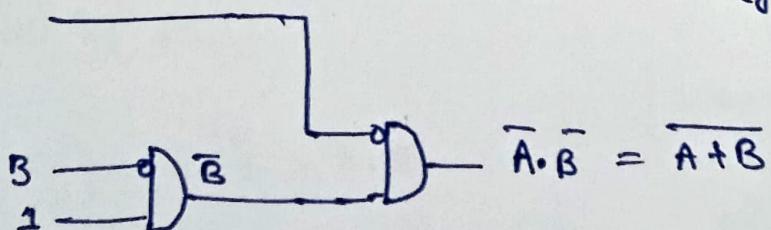


$$\text{NAND} = 2(\text{global '1'})$$

NOR gate by global '1'  $\rightarrow$



$$\text{NOR} = 2(\text{global '1'})$$



Special logic gates:-

$$\begin{array}{l} \text{Ex-OR} = X \oplus R \\ X \text{ NOR} \end{array} \Rightarrow f = A \oplus B$$

$f = A \odot B$

$$\overline{AB} + A\overline{B}$$

$$A\overline{B} + \overline{A}\overline{B}$$

5\*

$$XNOR = \overline{XOR}$$

$$X \text{ OR} = \overline{X \text{ NOR}}$$

Buffer = NOT  
 AND = NAND  
 OR = NOR

A	B	$A \oplus B$	$A \otimes B$	if { odd = 1 even = 0. }
0	0	0	1	
0	1	1	0	
1	0	1	0	
1	1	0	1	XOR

↓ equality  
inequality  
detector.

or

=

## Boolean Algebra →

### Boolean principle →

1. De Morgan's law →  $\overline{\overline{x}} = x$ ,  $\overline{x+y} = \overline{x} \cdot \overline{y}$

$$\overline{x+y} = \overline{x} \cdot \overline{y}$$

$$\overline{\overline{x+y}} = \overline{\overline{x} \cdot \overline{y}}$$

2. Idempotency law →

$$x+x = x \quad \left. \begin{array}{l} x \cdot x = x \\ 1+1 = 1 \end{array} \right\}$$

$$1+1 = 1 \quad \left. \begin{array}{l} 1 \cdot 1 = 1 \\ 0+0 = 0 \end{array} \right\}$$

$$0+0 = 0 \quad \left. \begin{array}{l} 0 \cdot 0 = 0 \\ x(\text{NAND})x = \overline{x} \end{array} \right\}$$

$$x(\text{NAND})x = \overline{x} \quad | \quad x(\text{NOR})x = \overline{x}$$

3. Commutative law →

$$\left. \begin{array}{l} x+y = y+x \\ x \cdot y = y \cdot x \end{array} \right\} \quad \left. \begin{array}{l} x(\text{NAND})y = y(\text{NAND})x \\ x(\text{NOR})y = y(\text{NOR})x \end{array} \right.$$

4. Associative law →

$$(x+y)+z = x+(y+z) \quad \left. \begin{array}{l} \text{NAND \& NOR} \\ \text{do not follow associative law.} \end{array} \right\}$$

$$(x \cdot y) \cdot z = x \cdot (y \cdot z) \quad \left. \begin{array}{l} \text{NAND \& NOR} \\ \text{do not follow associative law.} \end{array} \right\}$$

5. Compensation law →

$$\left. \begin{array}{l} x+\overline{x} = 1 \\ x \cdot \overline{x} = 0 \end{array} \right\} \quad \left. \begin{array}{l} x(\text{NAND})\overline{x} = 1 \\ x(\text{NOR})\overline{x} = 0 \end{array} \right\} \quad \left. \begin{array}{l} \text{NOT law} \\ \text{extra.} \end{array} \right\}$$

6. Distributive law  $\rightarrow$ 

$$x(y+z) = xy + xz$$

$$x + yz = (x+y)(x+z)$$

7. Absorption law  $\rightarrow$ 

$$x + x'y = (x+x') (x+y) = x+y$$

$$x+xy = (x+x)(x+y) = x(1+y) = x$$

8. Consensus law  $\rightarrow$ 

$$xy + x'z + yz = xy + x'z$$

$$xy + xz + yz = xy + yz$$

9. Duality principle  $\rightarrow$ 

+ve level logic  
 1  $\rightarrow$  high  
 0  $\rightarrow$  low

-ve level logic  
 1  $\rightarrow$  low  
 0  $\rightarrow$  high

+ve level logic  $\leftrightarrow$  -ve level logic

Dual

AND	$\xrightarrow{\text{Dneg}}$	OR	$\left\{ \begin{array}{l} 0 \rightarrow 1 \\ 1 \rightarrow 0 \end{array} \right.$
NAND	$\xrightarrow{\text{Dneg}}$	NOR	$\left\{ \begin{array}{l} 1 \rightarrow 0 \\ 0 \rightarrow 1 \end{array} \right.$

$$\left\{ \begin{array}{l} f(x,y) = \overline{x \cdot y} \xrightarrow{\text{Dneg}} \text{AND} \\ f_0(x,y) = \overline{x+y} \xrightarrow{\text{Dneg}} \text{OR only} \\ f'(x,y) = \overline{x \cdot y} \end{array} \right.$$

$$\left\{ \begin{array}{l} f(x,y) = \overline{x+y} \xrightarrow{\text{Dneg}} \text{OR} \\ f'(x,y) = \overline{x \cdot y} \xrightarrow{\text{Dneg}} \text{NAND} \\ f_0(x,y) = \overline{x \cdot y} \xrightarrow{\text{Dneg}} \text{NOR} \end{array} \right.$$

## 10. complement of "fun"

let  $f(x,y,z) = xy + yz + xz$

to compliment in Boolean alg.

and to or

or to and

and compliment

of each variable.

canonical form  $\rightarrow$

Minterms  $\rightarrow$  [standard product term]

x	y	minterms = 1
0	0	$0 \rightarrow x'y'$
0	1	$1 \rightarrow x'y$
1	0	$2 \rightarrow xy'$
1	1	$3 \rightarrow xy$

$$f(x,y) = \sum_{(1,2)} (1,2) = \Sigma (1,2)$$

$\downarrow$

**SOP**

$$= x'y + xy'$$

**SOP = AND-OR Ckt**

**SOP = NAND-NAND Ckt**

Minterms: [standard sum form]  $\rightarrow$

x	y	Minterm = 0
0	0	$0 \quad x+y \rightarrow 0$
0	1	$1 \quad x+y' \rightarrow 1$
1	0	$1 \quad x'+y \rightarrow 2$
1	1	$1 \quad x'+y' \rightarrow 3$

$$f(x,y) = \overline{\Sigma} (0,3)$$

$$= (x+y)(x'+y')$$

**POS**  $\rightarrow$  product of sum

**POS = OR-AND Ckt**

**POS = NOR-NOR Ckt**

One.

$$f(x,y,z) = xy + yz + xz$$

write down sop & pos form of this boolean fun.

四

$$\begin{aligned}
 f(x,y,z) &= xy(z+z') + (x+x')yz + x(y+y')z \\
 &= xyz + xyz' + xy'z + x'y'z + xyz + xy'z \\
 &= xyz + xyz' + xy'z + x'y'z
 \end{aligned}$$

$$f(x_4y_1z) = \sum_n (3, s_{16}, 7)$$

$$\overline{A}_M(0,1,2,4)$$

$$f'(x,y,z) = \sum_{m=0,1,2,4}$$

Try (3, 5, 67)

another simple way →

$$f(x,y,z) = \cancel{xy} + \cancel{yz} + \cancel{xz}$$

The diagram illustrates a function  $f$  from three binary strings to six binary strings, which are then mapped to six integers. The arrows show the following correspondences:

- $11t \rightarrow 110 \rightarrow 6$
- $t11 \rightarrow 111 \rightarrow 7$
- $1t1 \rightarrow 011 \rightarrow 3$
- $1t1 \rightarrow 111 \rightarrow 7$
- $1t1 \rightarrow 101 \rightarrow 5$
- $1t1 \rightarrow 111 \rightarrow 7$

$$\Rightarrow f'(y_1 z) = \zeta_1(3, 5)$$

Ques.  $f(x,y,z) = (x+z')(y'+z') (x'+y)$  Ans. for  
Connice~~d~~ form

Ans

$$\begin{aligned}
 f(x,y,z) &= (x+y \cdot y'+z') (x \cdot x' + y'+z') + (x'+y+z \cdot z') \\
 &= \underbrace{(x+y+z')}_{001} \underbrace{(x+y'+z')}_{011} + \underbrace{(x+y'+z')}_{011} \underbrace{(x'+y'+z')}_{111} \\
 &\quad + \underbrace{(x'+y+z)}_{100} \underbrace{(x'+y+z')}_{101}
 \end{aligned}$$

$$\bar{T}_M(1,3,4,5,7)$$

Note this is Maxterm

$$\bar{S}_M(0,2,6)$$

$x \rightarrow 0$   
 $x' \rightarrow 1$   
but in minterms

$x \rightarrow 1$   
 $x' \rightarrow 0$

another simple way →

$$f(x,y,z) = (x+y') (y'+z') (x'+y)$$

$$\begin{array}{ccc}
 0 \cdot y \cdot 1 & x \cdot 1 \cdot 1 & 1 \cdot 0 \cdot z \\
 \swarrow \quad \searrow & \swarrow \quad \searrow & \swarrow \quad \searrow \\
 001 & \frac{011}{3} & \frac{011}{3} \quad \frac{111}{7} \\
 & \overline{3} & \overline{7}
 \end{array}$$

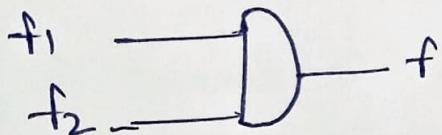
$$\bar{T}_M(1,3,4,5,7)$$

- How to process any boolean fun' from logic gates: →

→ NOT gate →

$$\begin{aligned}
 f(x_1, y_1, z) &\xrightarrow{\text{NOT}} f'(x_1, y_1, z) \\
 &= \sum_M(1, 2, 4, 7) \\
 &= \prod_M(0, 3, 5, 6)
 \end{aligned}$$

→ AND gate →



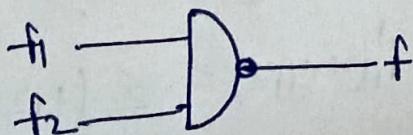
$$\begin{aligned}
 f_1(x_1, y_1, z) &= \sum(1, 2, 3, 4, 7) & f(x_1, y_1, z) = ? \\
 f_2(x_1, y_1, z) &= \sum(0, 1, 4, 6)
 \end{aligned}$$

ex: common term will be answer.

$$f(x_1, y_1, z) = \sum(1, 4) = \prod(0, 2, 3, 5, 6, 7) = g(x_1, y_1, z)$$

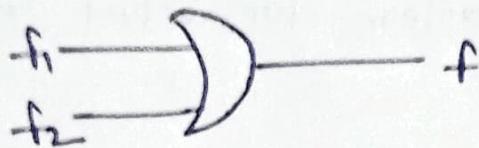
NOT pos ( $\prod_M$ ) से common नहीं होना है।

→ NAND gate →



$$\begin{aligned}
 f_1(x_1, y_1, z) &= \sum(1, 2, 3, 4, 7) \Rightarrow g(x_1, y_1, z) = \sum(1, 4) \\
 f_2(x_1, y_1, z) &= \sum(0, 1, 4, 6) \quad f(x_1, y_1, z) = \prod(1, 4) \\
 &\quad = \sum(0, 2, 3, 5, 6, 7)
 \end{aligned}$$

OR gate →



$$f_1(x,y,z) = \Sigma(0,2,3,6,7)$$

$$f_2(x,y,z) = \Sigma(1,2,6)$$

→ sum of both  
f<sub>1</sub> & f<sub>2</sub>.

$$f(x,y,z) = \Sigma(0,1,2,3,6,7) = g(x)y,z]$$

NOTE MAXTERM ( $\bar{M}$ ) में add  $\rightarrow$  करना

NOR gate →



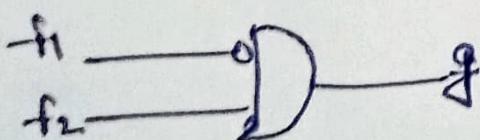
$$f_1(x,y,z) = \Sigma(0,2,3,6,7)$$

$$f_2(x,y,z) = \Sigma(1,2,6)$$

$$g(x,y,z) = \Sigma(0,1,2,3,6,7)$$

$$f(x,y,z) = \Sigma(4,5) = \bar{\Sigma}(0,1,2,3,6,7)$$

Global 1



$$f_1(x,y,z) = \Sigma(0,3,5,6)$$

$$f_2(x,y,z) = \Sigma(0,1,2,6)$$

$$g(x,y,z) = \Sigma(1,2)$$

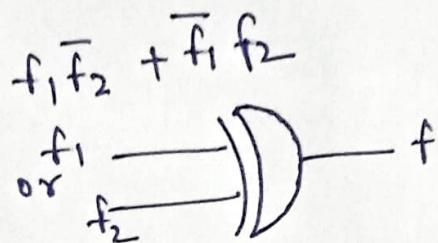
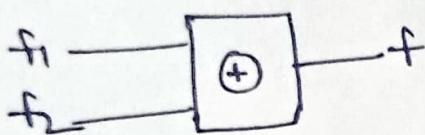
$$= \bar{\Sigma}(0,3,4,5,6,7)$$

Global 2



$$f_1(x,y,z) = \Sigma(1,2,4,7)$$

$$f(x,y,z) = \Sigma(0,1,2,4,6,7)$$

X-NOR gate

$$f_1(x,y,z) = \sum(0,1,6,7)$$

$$f_2(x,y,z) = \sum(0,1,2,3,4,5) \quad f'_2(x,y,z) = \sum(6,7)$$

$$f(x,y,z) = \sum(6,7) + \sum(2,3,4,5)$$

$$= \sum(2,3,4,5,6,7) = \overline{\sum(0,1)}$$

जैसे जो दोनों में common है और जो नहीं है उन्हे छोड़ दो।

But this is the "sof" for XNOR