



Fig. 2.2: **Basic notation.** (a) Input data is represented as a collection of points in the d -dimensional space defined by their feature responses (2D in this example). (b) A decision tree is a hierarchical structure of connected nodes. During testing, a split (internal) node applies a test to the input data \mathbf{v} and sends it to the appropriate child. The process is repeated until a leaf (terminal) node is reached (beige path). (c) Training a decision tree involves sending all training data $\{\mathbf{v}\}$ into the tree and optimizing the parameters of the split nodes so as to optimize a chosen energy function. See text for details.

$$\phi : \mathbb{R}^d \rightarrow \mathbb{R}^{d'}, \text{ with } d' \ll d.$$

2.1.3 Training and testing decision trees

At a high level, the functioning of decision trees can be separated into an off-line phase (training) and an on-line one (testing).

Tree testing (runtime). Given a previously unseen data point \mathbf{v} a decision tree hierarchically applies a number of predefined tests (see fig. 2.2b). Starting at the root, each split node applies its associated split function to \mathbf{v} . Depending on the result of the *binary* test the data is sent to the right or left child.¹ This process is repeated until the data point reaches a leaf node.

¹In this work we focus only on binary decision trees because they are simpler than n-ary ones. In our experiments we have not found big accuracy differences when using non binary trees.