



Fig. 4.3: **Regression forest: the ensemble model.** The regression forest posterior is simply the average of all individual tree posteriors  $p(\mathbf{y}|\mathbf{v}) = \frac{1}{T} \sum_{t=1}^T p_t(\mathbf{y}|\mathbf{v})$ .

actual value. Thus for prediction we can use a probability density function over the continuous variable  $\mathbf{y}$ . So, given the  $t^{\text{th}}$  tree in a forest and an input point  $\mathbf{v}$ , the associated leaf output takes the form  $p_t(\mathbf{y}|\mathbf{v})$ . In the low-dimensional example in fig. 4.2c we assume an underlying linear model of type  $y = w_0 + w_1x$  and each leaf yields the conditional  $p(y|x)$ .

**The ensemble model.** Just like in classification, the forest output is the average of all tree outputs (fig. 4.3):

$$p(\mathbf{y}|\mathbf{v}) = \frac{1}{T} \sum_t^T p_t(\mathbf{y}|\mathbf{v})$$

A practical justification for this model was presented in section 2.2.5.

**Randomness model.** Like in classification here we use a randomized node optimization model. Therefore, the amount of randomness is controlled during training by the parameter  $\rho = |\mathcal{T}_j|$ . The random subsets of split parameters  $\mathcal{T}_j$  can be generated on the fly when training