

Fig. 5.12: Regression from density forests. (a) 2D training points are shown in black. The green vertical line denotes the value  $x^*$  of the independent variable. We wish to estimate  $p(y|x=x^*)$ . (b) When testing a tree on the input  $x^*$  some split nodes cannot apply their associated split function and the data is sent to both children (see orange paths). (c) The line  $x=x^*$  intersects multiple cells in the partitioned feature space. (d) The line  $x=x^*$  intersects multiple leaf Gaussians. The conditional output is a combination of those Gaussians.

 $\int_{y} p_{t}(y|x=x^{*}) dy = 1$ , and can be computed as follows:

$$Z_{t,x^*} = \sum_{l \in \mathcal{L}_{t,x^*}} \pi_l \left( \phi_{t,l}(y_l^{\mathsf{T}} | x = x^*) - \phi_{t,l}(y_l^{\mathsf{B}} | x = x^*) \right)$$