

Overview

Classification Problem

In general, we want our classifier to have lowest generalized error.

- Data $(X,Y) \in \mathbb{R}^p \times \{0,1\}$.
- \blacksquare *X* is predictor, feature; *Y* is class label, response.
- (X,Y) have joint probability distribution \mathcal{D} .
- Goal: Based on *N* training pairs (X_i, Y_i) drawn.
- from \mathcal{D} produce a classifier $\hat{C}(X) \in \{0,1\}$.
- Goal: choose \hat{C} to have low generalization error.

Generative Methods

$$\underbrace{\mathbb{E}_{D}[(h(x|D) - y)^{2}]}_{ExpectedError} = \underbrace{\mathbb{E}_{D}[(\theta - \hat{\theta})^{2}]}_{Variance} + \underbrace{\hat{\theta}^{2}}_{Bias}$$

- Boosting converts weak learners to strong learners. Intuitively, a weak learner is just slightly better than a random guess, while a strong learner is very close to perfect performance.
- Goal: Reduce Bias.
- Bagging or bootstrap aggregation averages a given procedure over many samples to reduce its variance — a poor man's Bayes.
- Goal: Reduce Variance.

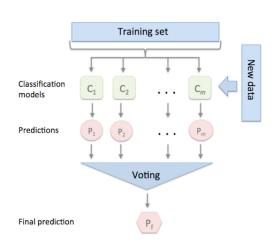
Weak and Strong Learners

Learners

- A weak learner produces a classifier that is only slightly more accurate than random classification.
- A class of concepts is learnable (or strongly learnable) if a polynomial-time algorithm achieves low error with high confidence for all concepts in the class.

Principle of Averaging

Voting Classifier: Average the predictions of a collection of classifiers.



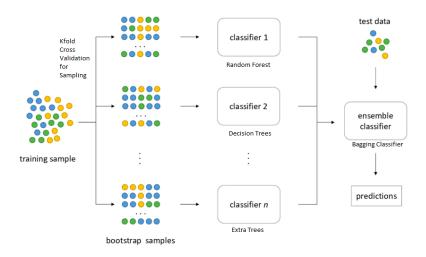
Principle of Averaging

- Instead of training different models on the same data, train the same model multiple times on different data sets and "combine" these "different" models
- We can use some simple/weak models as the base model
- How do we get multiple training data sets? (in practice, we only have one data set at training time)

Bootstrap Aggregating

- Bagging or bootstrap aggregation averages a given procedure over many samples, to reduce its variance — a poor man's Bayes.
- Bagging classifier helps in reducing the variance of individual estimators by introducing randomization into the training stage of each of the estimators and making an ensemble out of all the estimators. Note that the high variance means that changing the training data set results in the constructed or trained estimator by a great deal.

Bagging Sequence



Bagging Algorithm

```
Algorithm 1: Bagged Averaging
Input: Original dataset \mathcal{D}, Number of classifiers T
Output: Aggregated prediction
Initialize empty set of classifiers C;
Initialize empty set of predictions \mathcal{P};
for t = 1 to T do
     Sample a bootstrap dataset \mathcal{D}_t from the original dataset \mathcal{D};
     Train a classifier C_t using \mathcal{D}_t;
     Make predictions \mathcal{P}_t using classifier C_t;
     \mathcal{C} \leftarrow \mathcal{C} \cup \mathcal{C}_t:
     \mathcal{P} \leftarrow \mathcal{P} \cup \mathcal{P}_t:
end
```

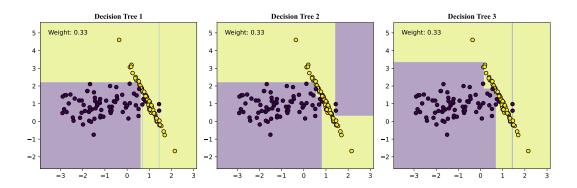
Aggregate predictions in \mathcal{P} using averaging or voting; **return** Aggregated prediction;

Bagged Classifier Trees

Bagged Classifier Trees

Bagged Classifier Trees

Average Bagged Classifier



Classifier Aggregation

- The bagged classifier is an ensemble learning method that combines multiple individual classifiers, known as decision trees, to make predictions.
- Each decision tree in the ensemble is trained on a different subset of the original training dataset, created through bootstrap sampling (sampling with replacement).
- During the training process, the bagged classifier fits each decision tree to a random subset of the training data, allowing each tree to learn different patterns and reduce overfitting.
- When making predictions, the bagged classifier combines the predictions from all decision trees by averaging the predicted probabilities (for classification problems) or taking the majority vote (for binary classification).
- The weights of the individual decision trees in the bagged classifier are calculated as 1/N, where N is the ensemble's total number of decision trees. This ensures that each decision tree contributes equally to the final prediction.
- By aggregating the predictions of multiple decision trees, the bagged classifier aims to improve the overall accuracy, robustness, and generalization ability compared to using a single decision tree.