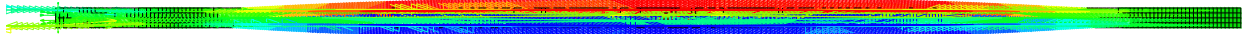


# Assignment 4

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Finite Element Analysis I

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# Abstract

In this assignment we examine the behaviour of a beam after being subjected to an impulse. The goal is to extract the resonance frequency of the beam with the given dimensions and material coefficients.

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# 1 Introduction

The goal of this assignment is to examine contact forces and the behaviour of a certain material under compression. The plate (some kind of metal / aluminium) is being squeezed by a press stamp. Due to the given material characteristics, certain forces are exerted on the surface of the press and the plate. Using this forces, and the respective deformation, we can reverse engineer the

## 2 Methods

### 2.1 Analytical solution

Consider a beam with the following dimensions attached to a wall, in our case, on the lefthand end:

$$L = 150mm, h = 2.5mm, b = 20mm, E = 10GPa, \nu = 0.3, \rho = 7.0E3kg.m^{-3} \quad (1)$$

The resonance frequencies (inducing a bending in the direction of the dimension h) of such a model are given by the formula:

$$\frac{1}{2\pi\sqrt{12}}\alpha_i^2\sqrt{\frac{E}{\rho}\frac{h}{L^2}} \quad (2)$$

Where:

$$\alpha_0 = 1.875, \alpha_1 = 4.695, \alpha_2 = 7.85, \dots, \alpha_i = (2i + 1)\frac{\pi}{2} \text{ for } i > 2$$

$E$  = Young's modulus

$\rho$  = density of the material

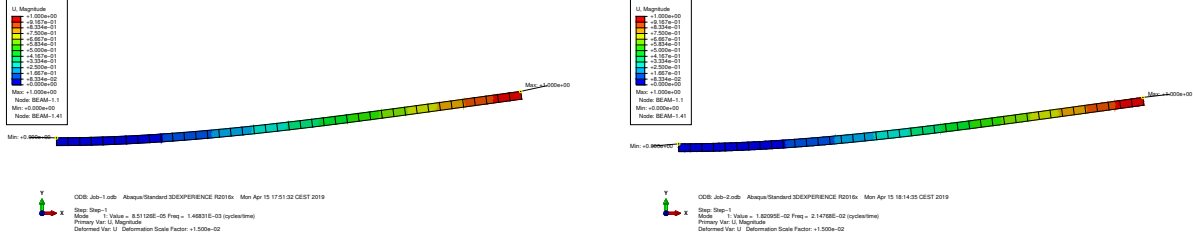
$h$  = height of the cross-section of the beam

$L$  = length of the beam

Using our values for  $\alpha_0$ :

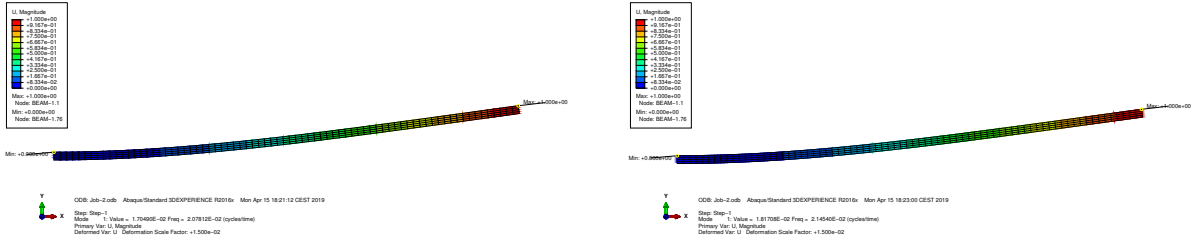
$$f_0 = \frac{1}{2\pi\sqrt{12}}1.875^2\sqrt{\frac{10 \cdot 10^9 Pa}{7 \cdot 10^3 \frac{kg}{m^3}} \frac{2.5 \cdot 10^{-3} m}{(150 \cdot 10^{-3} m)^2}} = 21.451 Hz \quad (3)$$

## 2.2 Frequency mode on Beam



(a) calculated frequency with CPS4R: 14.6 Hz    (b) calculated frequency with CPS8R: 21.4 Hz

Figure 1: Lower mesh count



(a) calculated frequency with CPS4R: 20.7 Hz    (b) calculated frequency with CPS8R: 21.4 Hz

Figure 2: Higher mesh count

Figure 1 shows us the results using a lower mesh density. With (a) using a linear meshing compared to a quadratic one, we immediately see the better results. This comparison was also discussed in assignment 1. With a higher mesh density (Figure 2), the differences between the linear and the quadratic method is less significant.

## 2.3 Generating an impulse

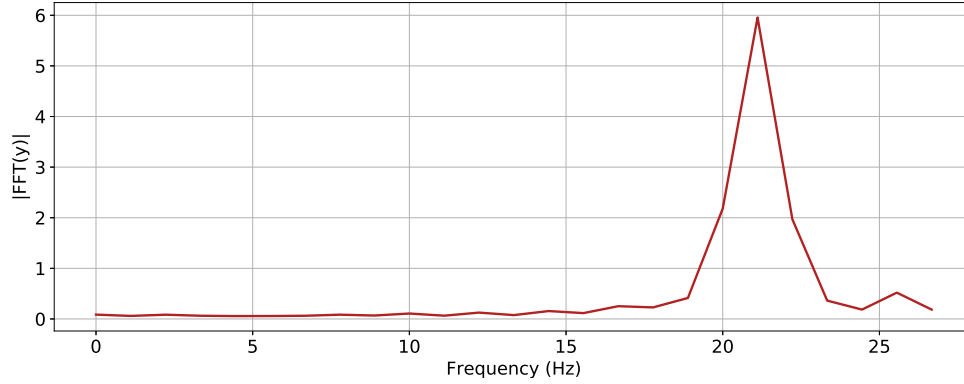


Figure 3: Fourier transformation

The impulse on the beam is generated by applying a concentrated force load on the extremity of the beam (the non-encastered end). This load is being applied for a short time period (1ms). Abaqus gives us the resonance frequency as one single number. We then export the X/Y data (obtained at the node where the force is applied) into Python to perform a forward fourier transform. The main advantage of this procedure is an output that shows not only one number, but the distribution of resonance frequencies. We observe a peak at around 21Hz. This supports our analytical solution from section 2.1.

## 3 Results and Discussion

The fourier transform gives a much better analysis regarding the resonance frequencies, than just a single number output from Abaqus. Possible secondary frequency-peaks can also be identified. The FE simulation in comparison offers only a limited insight. The obtainable and exportable data however depends highly on the elements used and the applied mesh density. Additionally, we observed that the natural frequency of the beam does not change with impulse intensity[1]. However the acquired data shows a more distinguished peak.

## References

- [1] Barry J. Goodno, James McGere *Mechanics of Materials (2018)*. (English)
- [2] Michel Goossens, Frank Mittelbach, and Alexander Samarin. *The L<sup>A</sup>T<sub>E</sub>X Companion*. Addison-Wesley, Reading, Massachusetts, 1993.