POINT TORSIONAL STABILITY BRACING OF A BEAM.

Beam torsional bracing: Point Bracing Example

#WeLoveSteelConstruction

- ตัวอย่าง จงตรวจสอบระบบค้ำยันทางขวางที่เป็น built-up beam HZ50x100x6x41nsqS5400 ของคานแล้กเชื่อมประกอบ simple beam ยาว 12 เมตร 2 ตัว ขนาด 500x250x12x6 ที่มีการคำยับ ณ ตำแหน่ง 1/3 ของความยาวคาน โดยคานตัวนี้ รับ DL และ LL 400 และ 800 kg/m² ตามลำดับ
- Step 1: คำนวณ required moment
- Step 2: คำนวณ required brace force
- Step 3: คำนวณ required braced stiffness
- Step 4: คำนวณ available brace strength
- Step 5: คำนวณ available brace stiffness
- Step 6: ตรวจสอบ brace strength & stiffness

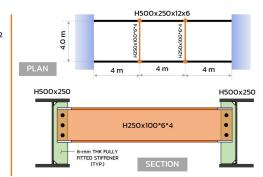


Figure 1: image

Load

Dead Load: $DL = 800 \frac{kg}{m^2}$

 $DL_{line} = 1600 \frac{kg}{m}$

Live Load: $LL = 400 \frac{kg}{m^2}$

 $LL_{line} = 800 \frac{kg}{m}$

 $W_{factor} = 1.2 * (1600) + 1.6 * (800) = 3200 \frac{kg}{m}$

Material Property

Yield Strength: $A_s = 245MPa$

Section Property of H-250x100x6x4

Section Area: $A_s = 21.52cm^2$

Weight: $w = 16.9 \frac{kg}{m}$

Moment of inertia about x: $I_y = 100cm^4$

Moment of inertia about y: $I_x = 2256cm^4$

Section Property of H-500x250x12x6

Section Area: $A_s = 88.56 \frac{kg}{m}$

Weight: $w = 69.52 \frac{kg}{m}$

Moment of inertia about x: $I_x = 41121cm^4$ Moment of inertia about y: $I_y = 3126cm^4$

1. Required Moment.

ASD	LRFD
$M = \frac{W_u * l^2}{8} = \frac{2400 * 12^2}{8}$ $M_r = 43200 kg.m$	$M = \frac{W_u * l^2}{8} = \frac{3200 * 12^2}{8}$ $M_r = 57600 kg.m$

2. Required Brace Force (The required flexural strength for a point torsional brace).

ASD	LRFD
$\overline{M_{br} = 0.02M_a}$	$M_{br} = 0.02M_u$
$M_{br} = 864kg.m$	$M_{br} = 1152kg.m$

3. Required Braced Stiffness.

ASD	LRFD
$\beta_T = \Omega \frac{2.4*L}{nEI_{yeff}} (\frac{M_r}{C_b})^2$ $\beta_T = 3* \frac{2.4*12*10^3}{3*2*10^6*41121*10^4} (\frac{864*10^{-3}*9.81}{1})^2$ $\beta_T = 2.52*10^{-9} \frac{N}{r_{qd}}$	$\beta_T = \frac{1}{\phi} \frac{2.4*L}{nEI_{yeff}} \left(\frac{M_r}{C_b}\right)^2$ $\beta_T = \frac{1}{0.75} *$ $\frac{2.4*12*10^3}{3*2*10^6*41121*10^4} \left(\frac{1152*10^{-3}*9.81}{1}\right)^2$ $\beta_T = 1.99 * 10^{-9} \frac{N}{rad}$

4. Avilable Braced Strength.

From:

$$M_n = M_p = F_y Z \le 1.6 * F_y S_x$$

$$Z = 203.04cm^3$$

$$S_x = 178.87cm^3$$

$$1.6 * F_y S_x = 1.6 * 245 * 178.87 * 10^3 = 70.12 * 10^6$$

$$M_n = F_y Z = 245 * 203.04 * 10^3 = 49.74 * 10^6 \le 70.12 * 10^6$$
 is true;

5. Avilable Braced Stiffness and Design thinkness of stiff-

$$\begin{split} \beta_{Tb} &= \frac{6EI}{L} = \frac{6*2*10^6*2256*10^4}{12*10^3} \frac{N}{rad.} \\ \beta_{Tb} &= 2.26*10^{10} \frac{N}{rad.} \end{split}$$

$$\beta_{Tb} = 2.26 * 10^{10} \frac{N}{rad.}$$

From:

$$\frac{1}{\beta_T} = \frac{1}{\beta_{TB}} + \frac{1}{\beta_{sec}}$$

ASD	LRFD
$\frac{1}{2.52*10^{-9}} = \frac{1}{2.26*10^{10}} + \frac{1}{\beta_{sec}}$ $\beta_{sec} = 2.52*10^{-9} \frac{N}{rad.}$	$\frac{1}{1.99*10^{-9}} = \frac{1}{2.26*10^{10}} + \frac{1}{\beta_{sec}}$ $\beta_{sec} = 1.99*10^{-9} \frac{N}{rad.}$

Determine the required width, bs, of 4 mm.-thick of stiffeners.

$$\beta_{sec} = \frac{3.3*E}{h_o}*[\frac{1.5*h_o*t_w^3}{12} + \frac{t_{st}*b_s^3}{12}]$$

ASD	LRFD
$\begin{array}{l} 2.52*10^{-9} = \\ \frac{3.3*2*10^6}{488}* \left[\frac{1.5*488*6^3}{12} + \frac{4*b_s^3}{12}\right] \\ b_s^3 = -34mm. < 0 \end{array}$	$1.99*10^{-9} = \frac{3.3*E}{488} * \left[\frac{1.5*488*6^3}{12} + \frac{4*b_s^3}{12} \right]$
$\frac{1}{488} * \left[\frac{1}{12} + \frac{1}{12} \right]$ $b_s^3 = -34mm. < 0$	$b_s^3 = -34mm. < 0$

6. Brace Strength & Stiffness Check.

ASD	LRFD
$\frac{M_n}{\Omega} = \frac{49.74 \times 10^6}{3} = 16.58 \times 10^6 kN.m$	$\phi M = 0.75 * 49.74 * 10^6 = 37.31 * 10^6 kN.m$
$16.58*10^6 \text{kN.m} > 8.64 \text{kN.m} \text{ (ok)}$	$37.31*10^6 \text{kN.m} > 11.52 \text{kN.m} \text{ (ok)}$