

Assignment 3

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The Weigelt Corporation has three branch plants with excess production capacity. Fortunately, the corporation has a new product ready to begin production, and all three plants have this capability, so some of the excess capacity can be used in this way. This product can be made in three sizes—large, medium, and small—that yield a net unit profit of \$420, \$360, and \$300, respectively. Plants 1, 2, and 3 have the excess capacity to produce 750, 900, and 450 units per day of this product, respectively, regardless of the size or combination of sizes involved. The amount of available in-process storage space also imposes a limitation on the production rates of the new product. Plants 1, 2, and 3 have 13,000, 12,000, and 5,000 square feet, respectively, of in-process storage space available for a day's production of this product. Each unit of the large, medium, and small sizes produced per day requires 20, 15, and 12 square feet, respectively. Sales forecasts indicate that if available, 900, 1,200, and 750 units of the large, medium, and small sizes, respectively, would be sold per day. At each plant, some employees will need to be laid off unless most of the plant's excess production capacity can be used to produce the new product. To avoid layoffs if possible, management has decided that the plants should use the same percentage of their excess capacity to produce the new product. Management wishes to know how much of each of the sizes should be produced by each of the plants to maximize profit.

```
### Adding package  
library(lpSolveAPI)
```

```
### creating lp with 0 constraints and 9 decision variables  
lprec <-make.lp(0,9)  
lprec
```

```
## Model name:  
## a linear program with 9 decision variables and 0 constraints
```

```
### Using Max function to maximize the profit  
set.objfn(lprec, c(420,360,300,420,360,300,420,360,300))  
lp.control(lprec,sense="max")
```

```
## $anti.degen  
## [1] "none"  
##  
## $basis.crash  
## [1] "none"  
##  
## $bb.depthlimit  
## [1] -50  
##  
## $bb.floorfirst
```

```

## [1] "automatic"
##
## $bb.rule
## [1] "pseudononint" "greedy"          "dynamic"          "rcostfixing"
##
## $break.at.first
## [1] FALSE
##
## $break.at.value
## [1] 1e+30
##
## $epsilon
##      epsb      epsd      epsel      epsint  epsperturb  epspivot
##      1e-10      1e-09      1e-12      1e-07      1e-05      2e-07
##
## $improve
## [1] "dualfeas" "thetagap"
##
## $infinite
## [1] 1e+30
##
## $maxpivot
## [1] 250
##
## $mip.gap
## absolute relative
##      1e-11      1e-11
##
## $negrange
## [1] -1e+06
##
## $obj.in.basis
## [1] TRUE
##
## $pivoting
## [1] "devex"      "adaptive"
##
## $presolve
## [1] "none"
##
## $scalelimit
## [1] 5
##
## $scaling
## [1] "geometric"  "equilibrate" "integers"
##
## $sense
## [1] "maximize"
##
## $simplextype

```

```
## [1] "dual"    "primal"
##
## $timeout
## [1] 0
##
## $verbose
## [1] "neutral"
```

```
###Plant products production by day
```

```
add.constraint(lprec,c(1, 1, 1, 0, 0, 0, 0, 0, 0), "<=",750)
add.constraint(lprec,c(0, 0, 0, 1, 1, 1, 0, 0, 0), "<=",900)
add.constraint(lprec,c(0, 0, 0, 0, 0, 0, 1, 1, 1), "<=",450)
```

```
###Plant storage for products by day
```

```
add.constraint(lprec,c(20, 15, 12, 0, 0, 0, 0, 0, 0), "<=",13000)
add.constraint(lprec,c(0, 0, 0, 20, 15, 12, 0, 0, 0), "<=",12000)
add.constraint(lprec,c(0, 0, 0, 0, 0, 0, 20, 15, 12), "<=",5000)
```

```
###Sales for products by day:
```

```
add.constraint(lprec,c(1, 1, 1, 0, 0, 0, 0, 0, 0), "<=",900)
add.constraint(lprec,c(0, 0, 0, 1, 1, 1, 0, 0, 0), "<=",1200)
add.constraint(lprec,c(0, 0, 0, 0, 0, 0, 1, 1, 1), "<=",750)
```

```
###All plants should have the same percentage capacity to produce new products
```

```
add.constraint(lprec, c(6, 6, 6, -5, -5, -5, 0, 0, 0), "=",0)
add.constraint(lprec, c(3, 3, 3, 0, 0, 0, -5, -5, -5), "=",0)
```

```
RN <- c("CCon1", "CCon2", "CCon3", "SCon1", "SCon2", "SCon3", "SaCon1", "SaCon2", "Sa
Con3", "%C1", "%C2")
```

```
CN <- c("P1L", "P1M", "P1S", "P2L", "P2M", "P2S", "P3L", "P3M", "P3S")
```

```
dimnames(lprec) <- list(RN, CN)
```

```
lprec
```

```
## Model name:
```

```
## a linear program with 9 decision variables and 11 constraints
```

```
write.lp(lprec, filename = "Assign2Q3", type = "lp")
```

```
### 1.Solve the problem using lp_solve, or any other equivalent library in R.
```

```
solve(lprec)
```

```
## [1] 0
```

```
get.objective(lprec)
```

```
## [1] 696000
```

```
get.variables(lprec)
```

```
## [1] 516.6667 177.7778 0.0000 0.0000 666.6667 166.6667 0.0000 0.0000
## [9] 416.6667
```

The profit is = \$696000

```
### 2. Identify the shadow prices, dual solution, and reduced costs
```

```
#Shadow prices
```

```
get.sensitivity.rhs(lprec)
```

```
## $duals
```

```
## [1] 0 0 0 12 20 60 0 0 0 -12 84 0 0 -24 -40
## [16] 0 0 -360 -120 0
```

```
##
```

```
## $dualsfrom
```

```
## [1] -1.000000e+30 -1.000000e+30 -1.000000e+30 1.041667e+04 1.000000e+04
## [6] 4.800000e+03 -1.000000e+30 -1.000000e+30 -1.000000e+30 -3.333333e+02
## [11] -8.333333e+01 -1.000000e+30 -1.000000e+30 -8.611111e+02 -1.000000e+02
## [16] -1.000000e+30 -1.000000e+30 -5.000000e+01 -1.333333e+02 -1.000000e+30
```

```
##
```

```
## $dualstill
```

```
## [1] 1.000000e+30 1.000000e+30 1.000000e+30 1.388889e+04 1.250000e+04
## [6] 5.400000e+03 1.000000e+30 1.000000e+30 1.000000e+30 1.666667e+02
## [11] 1.666667e+02 1.000000e+30 1.000000e+30 1.111111e+02 2.500000e+02
## [16] 1.000000e+30 1.000000e+30 2.500000e+01 6.666667e+01 1.000000e+30
```

We can find Shadow prices under \$dual and also calculations of shadow prices \$dualsfrom and \$dualstill

```
#Dual solution
```

```
get.dual.solution(lprec)
```

```
## [1] 1 0 0 0 12 20 60 0 0 0 -12 84 0 0 -24
## [16] -40 0 0 -360 -120 0
```

```
#Reduced costs
```

```
get.sensitivity.obj(lprec)
```

```
## $objfrom
## [1] 3.60e+02 3.45e+02 -1.00e+30 -1.00e+30 3.45e+02 2.52e+02 -1.00e+30
## [8] -1.00e+30 2.04e+02
##
## $objtill
## [1] 4.60e+02 4.20e+02 3.24e+02 4.60e+02 4.20e+02 3.24e+02 7.80e+02 4.80e+02
## [9] 1.00e+30
```

3. Identify the sensitivity of the above prices and costs. That is, specify the range of shadow prices and reduced cost within which the optimal solution will not change.

Shadow prices optimal solution will not change

```
cbind( get.sensitivity.rhs(lprec)$duals[1:21], lowerRange=get.sensitivity.rhs(lprec)$dualsfrom[1:21], upperRange=get.sensitivity.rhs(lprec)$dualstill[1:21])
```

```
##          lowerRange  upperRange
## [1,]      0 -1.000000e+30 1.000000e+30
## [2,]      0 -1.000000e+30 1.000000e+30
## [3,]      0 -1.000000e+30 1.000000e+30
## [4,]     12  1.041667e+04 1.388889e+04
## [5,]     20  1.000000e+04 1.250000e+04
## [6,]     60  4.800000e+03 5.400000e+03
## [7,]      0 -1.000000e+30 1.000000e+30
## [8,]      0 -1.000000e+30 1.000000e+30
## [9,]      0 -1.000000e+30 1.000000e+30
## [10,]    -12 -3.333333e+02 1.666667e+02
## [11,]     84 -8.333333e+01 1.666667e+02
## [12,]      0 -1.000000e+30 1.000000e+30
## [13,]      0 -1.000000e+30 1.000000e+30
## [14,]    -24 -8.611111e+02 1.111111e+02
## [15,]    -40 -1.000000e+02 2.500000e+02
## [16,]      0 -1.000000e+30 1.000000e+30
## [17,]      0 -1.000000e+30 1.000000e+30
## [18,]   -360 -5.000000e+01 2.500000e+01
## [19,]   -120 -1.333333e+02 6.666667e+01
## [20,]      0 -1.000000e+30 1.000000e+30
## [21,]     NA          NA          NA
```

Reduced costs optimal solution will not change

```
cbind(get.sensitivity.obj(lprec)$duals[1:9], lowerRange=get.sensitivity.obj(lprec)$objfrom[1:9], upperRange=get.sensitivity.obj(lprec)$objtill[1:9])
```

```
##          lowerRange upperRange
## [1,]      3.60e+02   4.60e+02
## [2,]      3.45e+02   4.20e+02
## [3,]     -1.00e+30   3.24e+02
## [4,]     -1.00e+30   4.60e+02
## [5,]      3.45e+02   4.20e+02
## [6,]      2.52e+02   3.24e+02
## [7,]     -1.00e+30   7.80e+02
## [8,]     -1.00e+30   4.80e+02
## [9,]      2.04e+02   1.00e+30
```

```
get.sensitivity.rhs(lprec)$duals
```

```
## [1]      0      0      0     12     20     60      0      0      0    -12     84      0      0    -24    -40
## [16]      0      0   -360   -120      0
```

4. Formulate the dual of the above problem and solve it. Does the solution agree with what you observed for the primal problem?

min $Z = 750 y_1 + 900 y_2 + 450 y_3 + 13000 y_4 + 12000 y_5 + 5000 y_6 + 900 y_7 + 1200 y_8 + 750 y_9 + 0 y_{11} + 0 y_{12}$
 subject to $y_1 + 20y_4 + y_7 + 6 y_{10} + 3y_{11} + 450y_{12} \geq 420$ $y_1 + 15y_4 + y_7 + 6y_{10} + 3y_{11} \geq 360$ $y_1 + 12y_4 + y_7 + 6y_{10} + 3y_{11} \geq 300$ $y_2 + 20y_5 + y_8 - 5y_{10} \geq 420$ $y_2 + 15y_5 + y_8 - 5y_{10} \geq 360$ $y_2 + 12y_5 + y_8 - 5y_{10} \geq 300$ $y_3 + 20y_6 + y_9 - 5y_{11} \geq 420$ $y_3 + 15y_6 + y_9 - 5y_{11} \geq 360$ $y_3 + 12y_6 + y_9 - 5y_{11} \geq 300$
 $y_1, y_2, y_3, y_4, y_5, y_6, y_7, y_8, y_9 \geq 0$ and y_{10}, y_{11}, y_{12} unrestricted in sign

```
Dual <- make.lp(0,12)

set.objfn(Dual, c(750,900,450,
                  13000,12000,5000,
                  900,1200,750,
                  0,0,0))
lp.control(Dual, sense='min')
```

```
## $anti.degen
## [1] "fixedvars" "stalling"
##
## $basis.crash
## [1] "none"
##
## $bb.depthlimit
## [1] -50
##
## $bb.floorfirst
## [1] "automatic"
```

```

##
## $bb.rule
## [1] "pseudononint" "greedy"          "dynamic"          "rcostfixing"
##
## $break.at.first
## [1] FALSE
##
## $break.at.value
## [1] -1e+30
##
## $epsilon
##      epsb      epsd      epsel      epsint epsperturb      epspivot
##      1e-10      1e-09      1e-12      1e-07      1e-05      2e-07
##
## $improve
## [1] "dualfeas" "thetagap"
##
## $infinite
## [1] 1e+30
##
## $maxpivot
## [1] 250
##
## $mip.gap
## absolute relative
##      1e-11      1e-11
##
## $negrange
## [1] -1e+06
##
## $obj.in.basis
## [1] TRUE
##
## $pivoting
## [1] "devex"      "adaptive"
##
## $presolve
## [1] "none"
##
## $scalelimit
## [1] 5
##
## $scaling
## [1] "geometric"      "equilibrate" "integers"
##
## $sense
## [1] "minimize"
##
## $simplextype
## [1] "dual"      "primal"

```

```
##  
## $timeout  
## [1] 0  
##  
## $verbose  
## [1] "neutral"
```

```
add.constraint(Dual ,c(1,0,0,20,0,0,1,0,0,900,0,450), ">=", 420)  
add.constraint(Dual ,c(0,1,0,0,20,0,1,0,0,-750,450,0), ">=", 420)  
add.constraint(Dual ,c(0,0,1,0,0,20,1,0,0,0,-900,-750), ">=", 420)  
add.constraint(Dual ,c(1,0,0,15,0,0,0,1,0,900,0,450), ">=", 360)  
add.constraint(Dual ,c(0,1,0,0,15,0,0,1,0,-750,450,0), ">=", 360)  
add.constraint(Dual ,c(0,0,1,0,0,15,0,1,0,0,-900,-750), ">=", 360)  
add.constraint(Dual ,c(1,0,0,12,0,0,0,0,1,900,0,450), ">=", 300)  
add.constraint(Dual ,c(0,1,0,0,12,0,0,0,1,-750,450,0), ">=", 300)  
add.constraint(Dual ,c(0,0,1,0,0,12,0,0,1,0,-900,-750), ">=", 300)  
Dual
```

```
## Model name:  
## a linear program with 12 decision variables and 9 constraints
```

```
options(scipen = 100)
```

```
solve(Dual)
```

```
## [1] 0
```

```
get.objective(Dual)
```

```
## [1] 696000
```

```
get.variables(Dual)
```

```
## [1] 0.0000000 0.0000000 0.0000000 12.0000000 20.0000000 60.0000000  
## [7] 0.0000000 0.0000000 0.0000000 0.2000000 0.4666667 0.0000000
```

```
get.constraints(Dual)
```

```
## [1] 420 460 780 360 360 480 324 300 300
```

```
get.sensitivity.rhs(Dual)
```



```

## $duals
## [1] 516.66667 0.00000 0.00000 177.77778 666.66667 0.00000 0.00000
## [8] 166.66667 416.66667 55.55556 66.66667 33.33333 0.00000 0.00000
## [15] 0.00000 383.33333 355.55556 166.66667 0.00000 0.00000 0.00000
##
## $dualsfrom
## [1] 360 -100000000000000000019884624838656
## [3] -100000000000000000019884624838656 345
## [5] 345 -100000000000000000019884624838656
## [7] -100000000000000000019884624838656 258
## [9] 204 -100000000000000000019884624838656
## [11] -100000000000000000019884624838656 -100000000000000000019884624838656
## [13] -100000000000000000019884624838656 -100000000000000000019884624838656
## [15] -100000000000000000019884624838656 -40
## [17] -60 -24
## [19] -100000000000000000019884624838656 -100000000000000000019884624838656
## [21] -100000000000000000019884624838656
##
## $dualstill
## [1] 460.0 100000000000000000019884624838656.0
## [3] 100000000000000000019884624838656.0 420.0
## [5] 412.5 100000000000000000019884624838656.0
## [7] 100000000000000000019884624838656.0 324.0
## [9] 100000000000000000019884624838656.0 180.0
## [11] 210.0 480.0
## [13] 100000000000000000019884624838656.0 100000000000000000019884624838656.0
## [15] 100000000000000000019884624838656.0 60.0
## [17] 15.0 32.0
## [19] 100000000000000000019884624838656.0 100000000000000000019884624838656.0
## [21] 0.4

```

```
get.sensitivity.obj(Dual)
```

```
## $objfrom
## [1] 694.4444 833.3333
## [3] 416.6667 11222.2222
## [5] 11571.1384 4800.0000
## [7] 516.6667 844.4444
## [9] 583.3333 -40000.0000
## [11] -15000.0000 -100000000000000000019884624838656.0000
##
## $objtill
## [1] 1000000000000000000019884624838656.000000000000000000
## [2] 1000000000000000000019884624838656.000000000000000000
## [3] 1000000000000000000019884624838656.000000000000000000
## [4] 13888.888888888889596274
## [5] 12500.000000000000181899
## [6] 5181.81818181818107405
## [7] 1000000000000000000019884624838656.000000000000000000
## [8] 1000000000000000000019884624838656.000000000000000000
## [9] 1000000000000000000019884624838656.000000000000000000
## [10] 0.00000000007996926
## [11] 0.00000000004798156
## [12] 0.00000000003998463
```

```
get.dual.solution(Dual)
```

##	[1]	1.00000	516.66667	0.00000	0.00000	177.77778	666.66667	0.00000
##	[8]	0.00000	166.66667	416.66667	55.55556	66.66667	33.33333	0.00000
##	[15]	0.00000	0.00000	383.33333	355.55556	166.66667	0.00000	0.00000
##	[22]	0.00000						