A7-Regresión logística

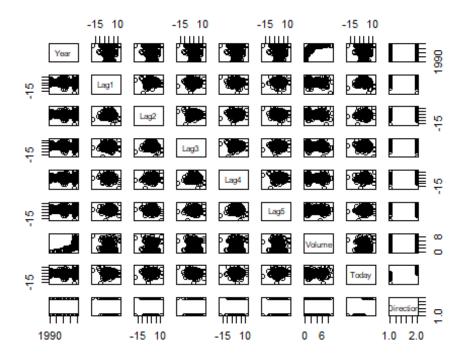
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1. Análisis de datos:

```
# Cargar el set de datos Weekly
data("Weekly")
# Revisando Los datos
head(Weekly)
     Year
            Lag1
                   Lag2
                          Lag3
                                Lag4
                                        Lag5
                                               Volume Today Direction
## 1 1990 0.816 1.572 -3.936 -0.229 -3.484 0.1549760 -0.270
                                                                   Down
## 2 1990 -0.270 0.816 1.572 -3.936 -0.229 0.1485740 -2.576
                                                                   Down
## 3 1990 -2.576 -0.270 0.816 1.572 -3.936 0.1598375
                                                       3.514
                                                                     Up
## 4 1990 3.514 -2.576 -0.270 0.816 1.572 0.1616300
                                                       0.712
                                                                     Up
## 5 1990 0.712 3.514 -2.576 -0.270 0.816 0.1537280
                                                       1.178
                                                                     Up
## 6 1990 1.178 0.712 3.514 -2.576 -0.270 0.1544440 -1.372
                                                                   Down
glimpse(Weekly)
## Rows: 1,089
## Columns: 9
               <dbl> 1990, 1990, 1990, 1990, 1990, 1990, 1990, 1990,
## $ Year
1990, 1990, ~
               <dbl> 0.816, -0.270, -2.576, 3.514, 0.712, 1.178, -1.372,
## $ Lag1
0.807, 0~
               <dbl> 1.572, 0.816, -0.270, -2.576, 3.514, 0.712, 1.178, -
## $ Lag2
1.372, 0~
## $ Lag3
               <dbl> -3.936, 1.572, 0.816, -0.270, -2.576, 3.514, 0.712,
1.178, -~
               <dbl> -0.229, -3.936, 1.572, 0.816, -0.270, -2.576, 3.514,
## $ Lag4
0.712, \sim
## $ Lag5
               <dbl> -3.484, -0.229, -3.936, 1.572, 0.816, -0.270, -
2.576, 3.514,~
               <dbl> 0.1549760, 0.1485740, 0.1598375, 0.1616300,
## $ Volume
0.1537280, 0.154~
               <dbl> -0.270, -2.576, 3.514, 0.712, 1.178, -1.372, 0.807,
## $ Today
0.041, 1~
## $ Direction <fct> Down, Down, Up, Up, Down, Up, Up, Up, Down,
Down, Up, Up~
summary(Weekly)
##
                        Lag1
                                           Lag2
                                                              Lag3
## Min. :1990
                  Min. :-18.1950 Min. :-18.1950
                                                        Min. :-18.1950
```

```
1st Qu.:1995 1st Qu.: -1.1540
                                    1st Qu.: -1.1540
##
                                                       1st Qu.: -1.1580
##
   Median :2000
                  Median :
                            0.2410
                                     Median :
                                             0.2410
                                                       Median : 0.2410
   Mean
          :2000
                  Mean
                            0.1506
                                     Mean
                                          :
                                              0.1511
                                                       Mean
                                                            : 0.1472
##
   3rd Qu.:2005
                  3rd Qu.: 1.4050
                                     3rd Qu.: 1.4090
                                                       3rd Qu.: 1.4090
##
                                                             : 12.0260
   Max.
          :2010
                  Max.
                         : 12.0260
                                     Max.
                                            : 12.0260
                                                       Max.
##
        Lag4
                           Lag5
                                             Volume
                                                              Today
                                                :0.08747
##
          :-18.1950
                      Min.
                             :-18.1950
                                         Min.
                                                          Min.
   Min.
                                                                 : -
18.1950
   1st Qu.: -1.1580
                      1st Qu.: -1.1660
                                         1st Qu.:0.33202
                                                          1st Qu.: -
1.1540
                      Median : 0.2340
                                         Median :1.00268
##
   Median : 0.2380
                                                          Median :
0.2410
## Mean :
             0.1458
                      Mean :
                                0.1399
                                         Mean
                                               :1.57462
                                                          Mean
0.1499
                                         3rd Qu.:2.05373
##
   3rd Qu.:
             1.4090
                      3rd Qu.:
                                1.4050
                                                          3rd Qu.:
1.4050
   Max. : 12.0260
                      Max. : 12.0260
                                               :9.32821
##
                                        Max.
                                                          Max.
                                                               :
12.0260
##
   Direction
##
   Down:484
##
   Up :605
##
##
##
##
pairs(Weekly)
```



```
cor(Weekly[, -9]) # Excluye 'Direction' ya que es categórica
##
               Year
                           Lag1
                                      Lag2
                                                 Lag3
                                                            Lag4
## Year
         1.00000000 -0.032289274 -0.03339001 -0.03000649 -0.031127923
## Lag1
         -0.03228927
                    1.000000000 -0.07485305 0.05863568 -0.071273876
## Lag2
         -0.03339001 -0.074853051 1.00000000 -0.07572091
                                                      0.058381535
## Lag3
         ## Lag4
         -0.03112792 -0.071273876 0.05838153 -0.07539587
                                                      1.000000000
## Lag5
         -0.03051910 -0.008183096 -0.07249948 0.06065717 -0.075675027
## Volume 0.84194162 -0.064951313 -0.08551314 -0.06928771 -0.061074617
         -0.03245989 -0.075031842 0.05916672 -0.07124364 -0.007825873
## Today
##
                Lag5
                         Volume
                                      Today
## Year
         -0.008183096 -0.06495131 -0.075031842
## Lag1
## Lag2
        -0.072499482 -0.08551314 0.059166717
## Lag3
         0.060657175 -0.06928771 -0.071243639
## Lag4
         -0.075675027 -0.06107462 -0.007825873
## Lag5
         1.000000000 -0.05851741 0.011012698
## Volume -0.058517414 1.00000000 -0.033077783
## Today 0.011012698 -0.03307778 1.000000000
```

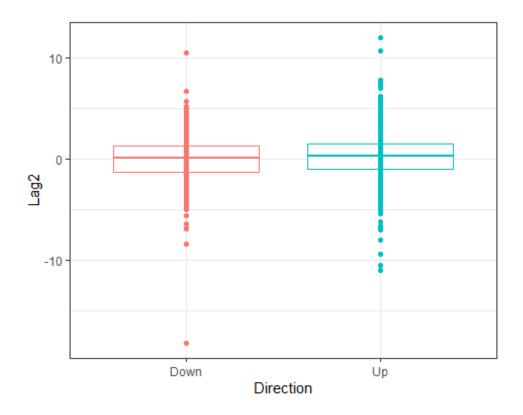
2. Modelo logístico con todas las variables menos "Today":

```
# Modelo logístico excluyendo 'Today'
modelo.log.m <- glm(Direction ~ . -Today, data = Weekly, family =
binomial)
summary(modelo.log.m)
##
## Call:
## glm(formula = Direction ~ . - Today, family = binomial, data = Weekly)
##
## Deviance Residuals:
                     Median
                                  3Q
      Min
                10
                                          Max
                     0.9941
## -1.7071 -1.2578
                              1.0873
                                       1.4665
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 17.225822 37.890522 0.455
                                            0.6494
## Year
              -0.008500 0.018991 -0.448
                                            0.6545
              -0.040688 0.026447 -1.538
                                            0.1239
## Lag1
                                   2.204
                                            0.0275 *
               0.059449 0.026970
## Lag2
              -0.015478   0.026703   -0.580
                                            0.5622
## Lag3
## Lag4
              -0.027316
                          0.026485 -1.031
                                            0.3024
## Lag5
              -0.014022
                          0.026409 -0.531
                                            0.5955
## Volume
               0.003256 0.068836 0.047
                                            0.9623
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 1496.2 on 1088 degrees of freedom
## Residual deviance: 1486.2 on 1081 degrees of freedom
## AIC: 1502.2
##
## Number of Fisher Scoring iterations: 4
confint(modelo.log.m, level = 0.95) # Intervalos de confianza
## Waiting for profiling to be done...
##
                       2.5 %
                                  97.5 %
## (Intercept) -56.985558236 91.66680901
## Year
               -0.045809580 0.02869546
## Lag1
               -0.092972584 0.01093101
## Lag2
                0.007001418 0.11291264
                -0.068140141 0.03671410
## Lag3
                -0.079519582 0.02453326
## Lag4
                -0.066090145 0.03762099
## Lag5
                -0.131576309 0.13884038
## Volume
```

3. Variables significativas:

```
# Gráfico de boxplot para una variable significativa (Lag2)
ggplot(Weekly, aes(x = Direction, y = Lag2)) +
  geom_boxplot(aes(color = Direction)) +
  geom_point(aes(color = Direction)) +
  theme_bw() +
  theme(legend.position = "null")
```



4. División de los datos en entrenamiento y prueba:

```
# División en datos de entrenamiento y prueba
datos.entrenamiento <- Weekly$Year < 2009
datos.test <- Weekly[!datos.entrenamiento, ]

# Verifica La división (contando filas)
sum(datos.entrenamiento) + nrow(datos.test)

## [1] 1089</pre>
```

5. Modelo con las variables significativas:

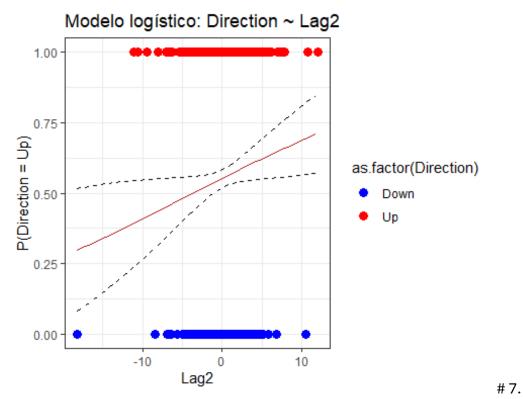
```
# Ajuste del modelo logístico con variables significativas
modelo.log.s <- glm(Direction ~ Lag2, data = Weekly, family = binomial,
subset = datos.entrenamiento)
summary(modelo.log.s)

##
## Call:
## glm(formula = Direction ~ Lag2, family = binomial, data = Weekly,
## subset = datos.entrenamiento)
##
## Deviance Residuals:
## Min 1Q Median 3Q Max</pre>
```

```
## -1.536 -1.264 1.021 1.091
                                   1.368
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
                                    3.162 0.00157 **
## (Intercept) 0.20326 0.06428
## Lag2
               0.05810
                          0.02870
                                    2.024 0.04298 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 1354.7 on 984 degrees of freedom
## Residual deviance: 1350.5 on 983 degrees of freedom
## AIC: 1354.5
##
## Number of Fisher Scoring iterations: 4
```

6. Representación gráfica del modelo

```
# Nuevos puntos para Lag2
nuevos_puntos <- seq(min(Weekly$Lag2), max(Weekly$Lag2), by = 0.5)</pre>
# Predicción de las probabilidades
predicciones <- predict(modelo.log.s, newdata = data.frame(Lag2 =</pre>
nuevos_puntos), se.fit = TRUE, type = "response")
# Límites del intervalo de confianza
CI_inferior <- predicciones$fit - 1.96 * predicciones$se.fit</pre>
CI_superior <- predicciones$fit + 1.96 * predicciones$se.fit</pre>
# Crear un data frame para graficar
datos curva <- data.frame(Lag2 = nuevos puntos, probabilidad =</pre>
predicciones$fit, CI.inferior = CI_inferior, CI.superior = CI_superior)
# Gráfico del modelo logístico
ggplot(Weekly, aes(x = Lag2, y = as.numeric(Direction == "Up"))) +
  geom_point(aes(color = as.factor(Direction)), size = 3) +
  geom_line(data = datos_curva, aes(y = probabilidad), color =
"firebrick") +
  geom line(data = datos curva, aes(y = CI.superior), linetype =
"dashed") +
  geom_line(data = datos_curva, aes(y = CI.inferior), linetype =
"dashed") +
  labs(title = "Modelo logístico: Direction ~ Lag2", x = "Lag2", y =
"P(Direction = Up)") +
  scale color manual(values = c("blue", "red")) +
 theme bw()
```



Evaluación del modelo:

```
# Prueba de chi cuadrada
anova(modelo.log.s, test = "Chisq")
## Analysis of Deviance Table
##
## Model: binomial, link: logit
##
## Response: Direction
##
## Terms added sequentially (first to last)
##
##
##
        Df Deviance Resid. Df Resid. Dev Pr(>Chi)
## NULL
                         984
                                 1354.7
                         983
                                 1350.5 0.04123 *
## Lag2 1
            4.1666
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

8. Matriz de confusión y evaluación del modelo

```
# Predicciones en el conjunto de prueba
predicciones.test <- predict(modelo.log.s, newdata = datos.test, type =
"response")
predicciones.test <- ifelse(predicciones.test > 0.5, "Up", "Down")
```

```
# Matriz de confusión
table(Predicted = predicciones.test, Actual = datos.test$Direction)
## Actual
## Predicted Down Up
## Down 9 5
## Up 34 56
```