

8.4

$$\vec{E} = \text{Re} \left[ \vec{\tilde{E}} e^{-i\omega t + i\vec{k} \cdot \vec{r}} \right] \quad \vec{B} = \text{Re} \left[ \vec{\tilde{B}} e^{-i\omega t + i\vec{k} \cdot \vec{r}} \right]$$

$$\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\left( \frac{\partial E_z}{\partial y} - \frac{\partial E_y}{\partial z} \right) \hat{x} + \left( \frac{\partial E_x}{\partial z} - \frac{\partial E_z}{\partial x} \right) \hat{y} + \left( \frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \hat{z} = -\frac{\partial \vec{B}}{\partial t}$$

$$\text{Re} \left[ \left[ (i k_y \tilde{E}_z - i k_z \tilde{E}_y) \hat{x} + (i k_z \tilde{E}_x - i k_x \tilde{E}_z) \hat{y} + (i k_x \tilde{E}_y - i k_y \tilde{E}_x) \hat{z} \right] e^{-i\omega t + i\vec{k} \cdot \vec{r}} \right] = -(-i\omega) \vec{\tilde{B}} e^{-i\omega t + i\vec{k} \cdot \vec{r}}$$

assume  $\vec{\tilde{E}}$   
+  $\vec{\tilde{B}}$  are  
complex

$$i(\vec{k} \times \vec{\tilde{E}}) = i\omega \vec{\tilde{B}} \quad \leftarrow \omega = ck$$

$$\vec{\tilde{B}} = \frac{1}{c} \frac{\vec{k}}{k} \times \vec{\tilde{E}} \quad \rightarrow \quad \boxed{\vec{\tilde{B}} = \frac{1}{c} \hat{k} \times \vec{\tilde{E}}}$$

The real and complex equations are simply related by taking the real component of the complex equation

$$\boxed{\text{Re} \left[ \vec{\tilde{B}} = \frac{1}{c} \hat{k} \times \vec{\tilde{E}} \right] \Rightarrow \vec{B} = \frac{1}{c} \hat{k} \times \vec{E}}$$