

CLASS 79Dynamic Programming (DP)

Recursion, Backtracking, Tree

DP = Recursion + Optimization
2-3

Recursion → Explore all possible ways

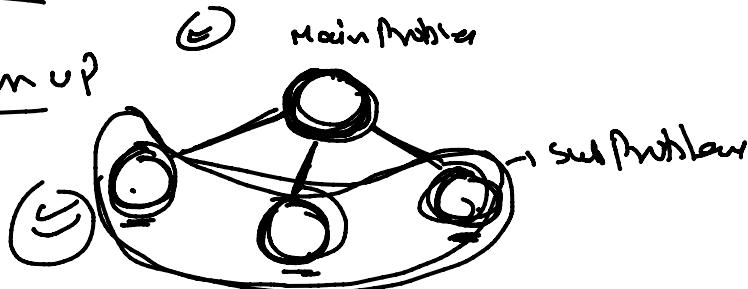
To C ~ Exponential



DP

→ Memoization → Top down

→ Tabulation → Bottom up



Problems!

Recursion

Dynamic Programming

→ optimal subproblems

→ overlapping subproblems

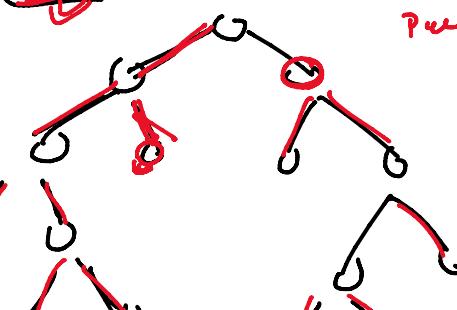
Recursion

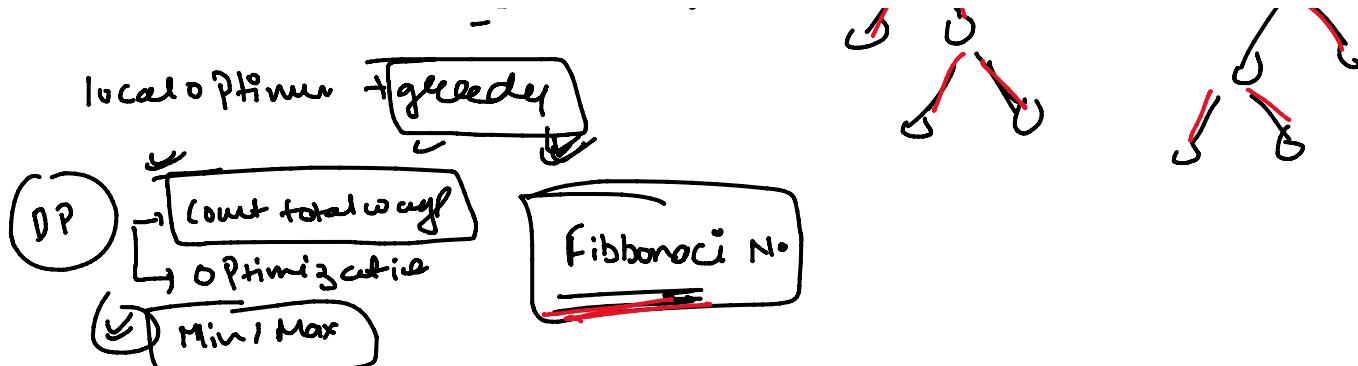
Backtracking

one.
(DP)
previous
No of Pow.

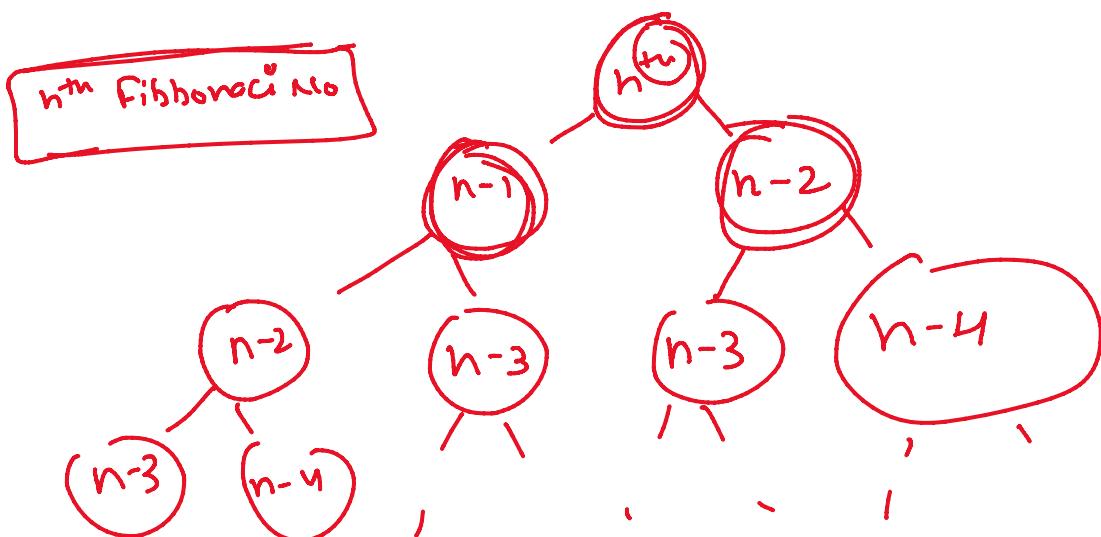
Main Problem

local optima & cycles





0 1 1 2 3 5 8 13 21 34 - - -

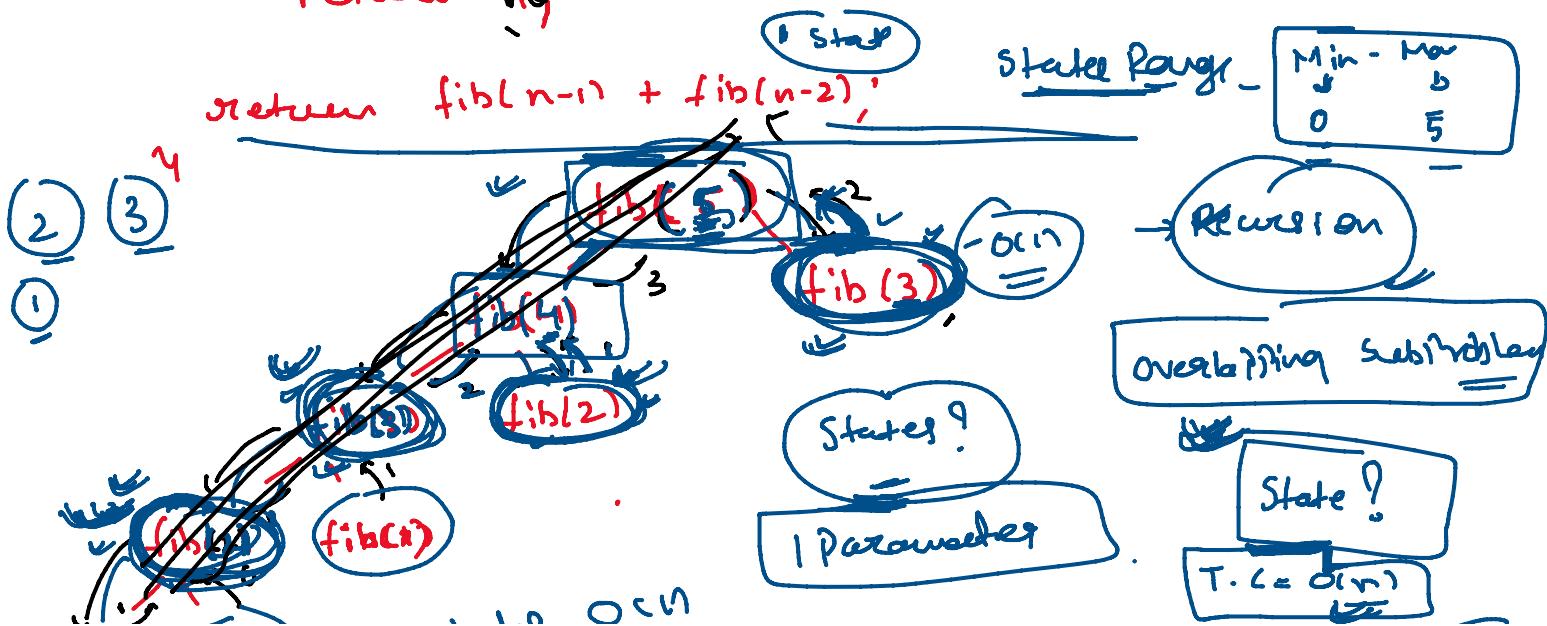


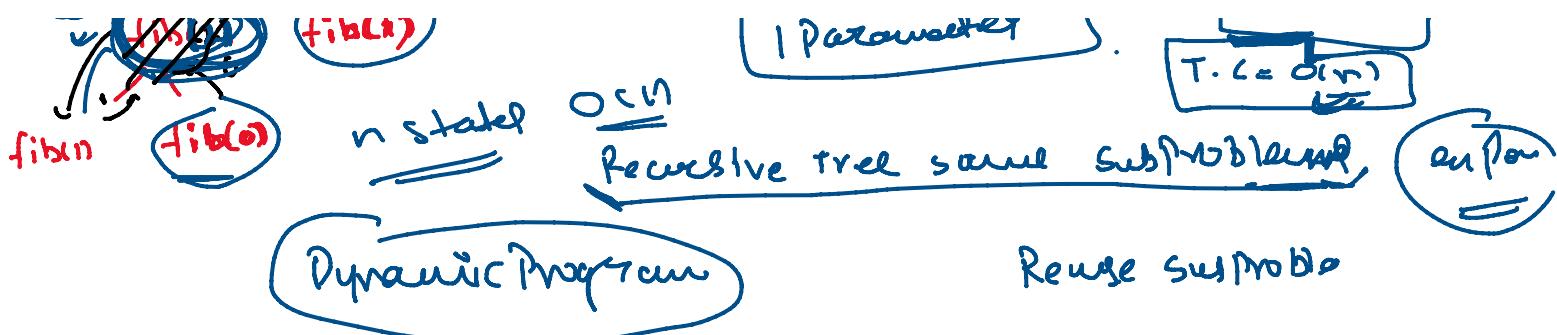
int fib(int n)

2 if (n==0 or n==1)

Vetuur

return fib(n-1) + fib(n-2);





Every Recursion call has their start

$$S.C = O(n) + O(n)$$

Stacks Para DPs Para

Two Recursion calls with same state are seen

State 0 - 5

Array/Vector of size 6

vector<int> dp(6, -1);

-1	-1	-1	-1	-1	-1
0	1	2	3	4	5

dp[0] = dp[1] dp[2]

dp[3] = dp[4] dp[5]

0 - n - 1

int fib (int n, vector<int> &dp)

if (n==0 or n==1)
return n

if (dp[n] != -1) return dp[n];

dp[n] = fib(n-1 + fib(n-2));

return dp[n];

Memoization

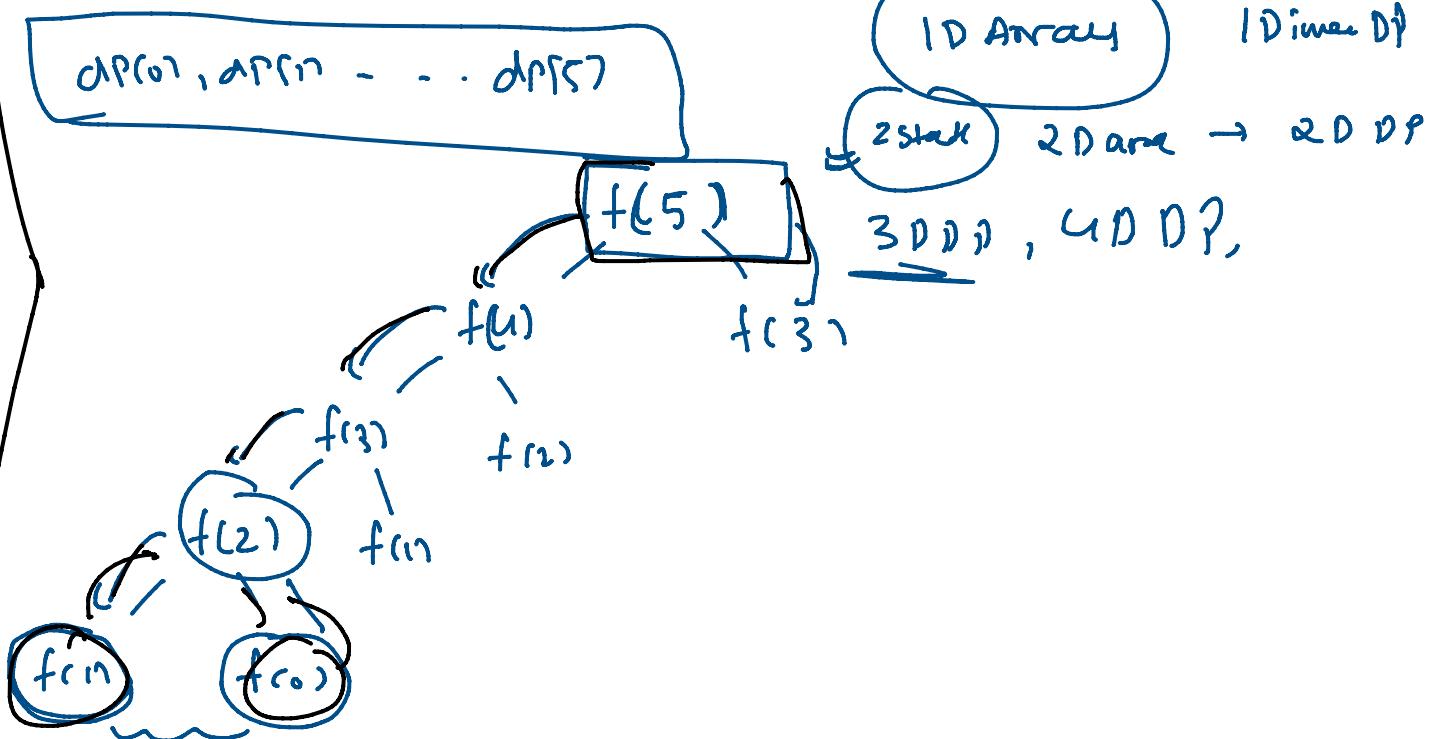
Recursion

Top-down

1D Array

1D Inner DP

dp[0], dp[1] ... dp[5]



Tabulation Approach (Bottom Up DP)

We directly start from Bottom:

vector<int> dp(n, -1);

$$\begin{cases} \text{dp}[0] = 0; \\ \text{dp}[1] = 1; \end{cases}$$

for (i=2; i<n; i++)

$$\text{dp}[i] = \text{dp}[i-1] + \text{dp}[i-2];$$

T.C = O(n)

S.C = O(n)

Optimization

n = 6

$$\text{Prev1} = 1, \quad \text{Prev2} = 0$$

```
int Prev2 = 0;
int Prev1 = 1;
```

$$i=2 \quad \text{cur} = 1, \quad \text{Prev2} = 1$$

1D Array
2 Stack
2D arr → 2D DP
3DDP, 4DDP,
1Dimer DP

$$i=2 \quad \text{cur} = 1, \quad \text{Prev2} = 1$$

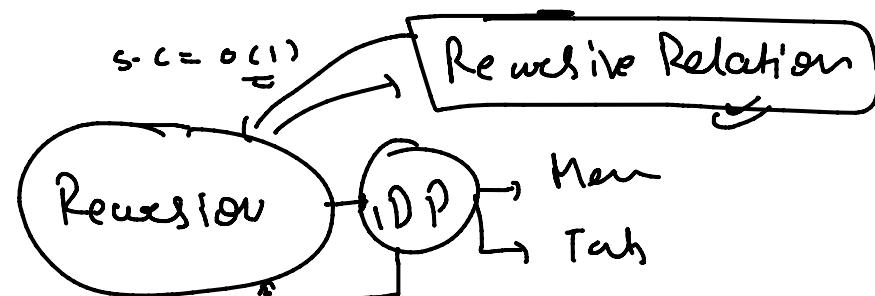
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int Prev2=0;
int Prev=1;

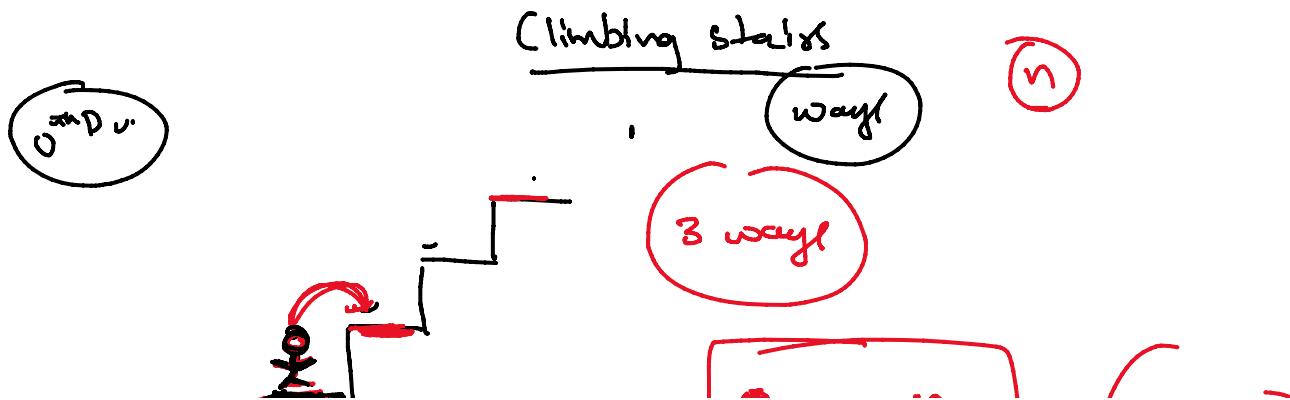
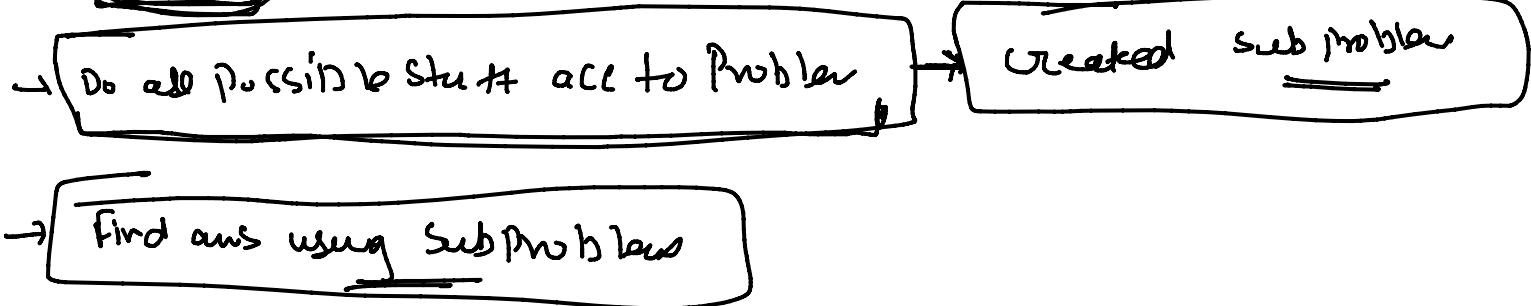
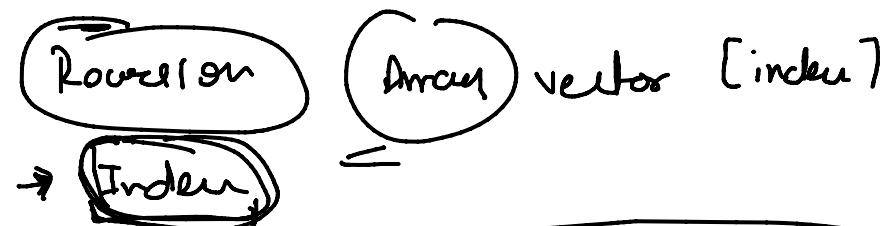
for (i=2; i<=n; i++)
    {
        int cur = Prev + Prev2;
        Prev2 = Prev;
        Prev = cur;
    }
return Prev;

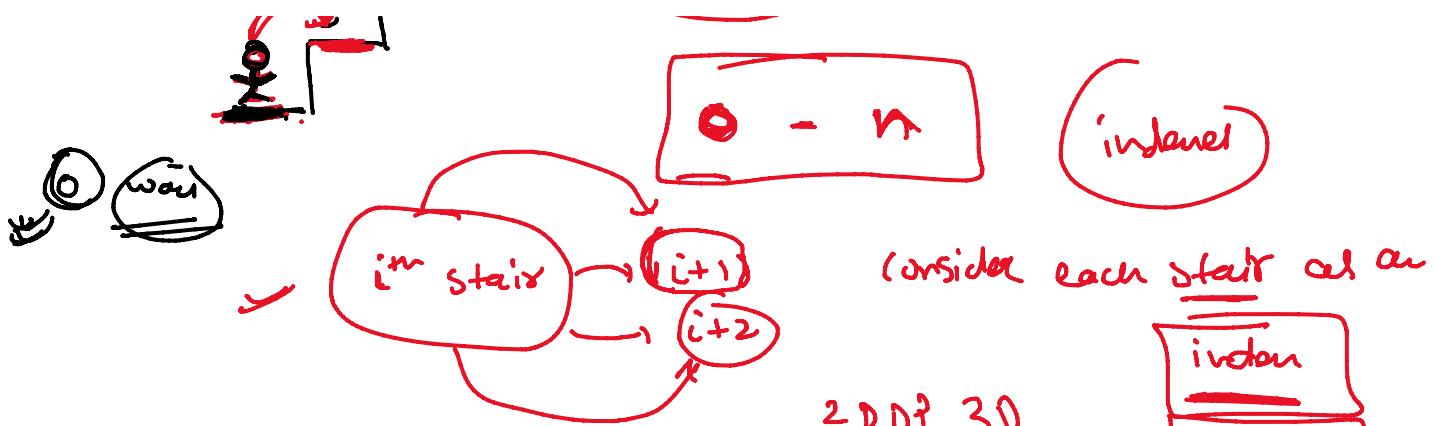
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$i=2 \quad cur = 1, Prev2 = 1$
 $Prev = 1$
 $i=3 \quad cur = 2, Prev2 = 1$
 $Prev = 2$
 $i=4 \quad cur = 3, Prev2 = 2$
 $Prev = 3$



- Count total ways :
- ↓
- Min/Max :
- ↓





int Climbing_Stair (int i) \Rightarrow No of ways to reach ith floor

{ if ($i == 0$)
return 1;

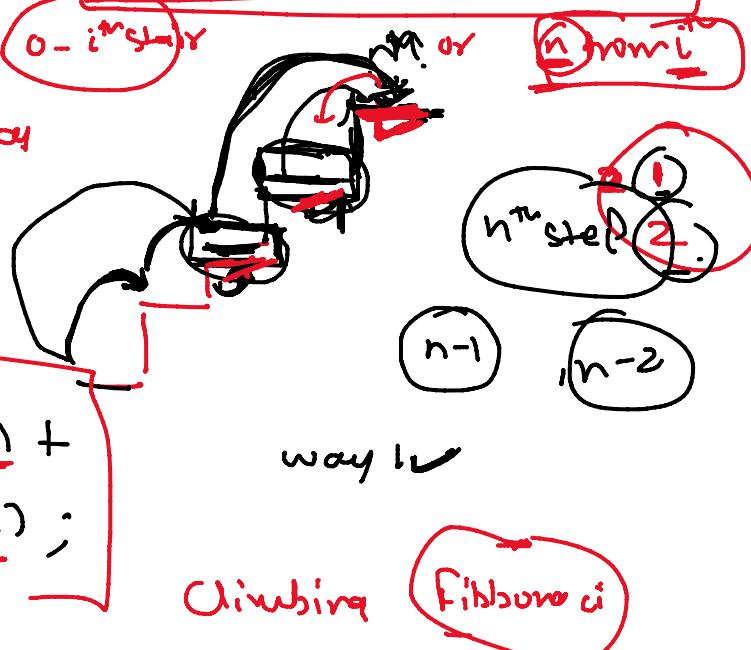
if ($i == 1$)
return 1;

if (dp[i] != -1) return dp[i];

dp[i] = Climbing_Stair (i-1) +
" " i-2;

return dp[i]

Tabulation

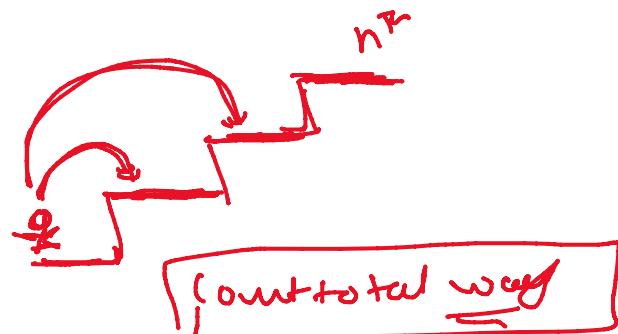


int ClimbingStair (int i) int n)

{ if ($i == n$)
return 1;
if ($i == n-1$)
return 1;

return Climbing (i+1, n) + Climbing (i+2, n);

climbingStair (0, n)



T.C of Memoization = Tabulation