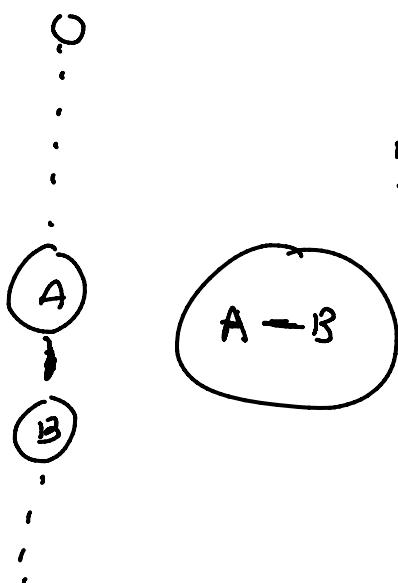


Class 100



$$100 \times 2 = 200 \text{ hrs}$$

## Graphs



### Articulation Point, Bridges

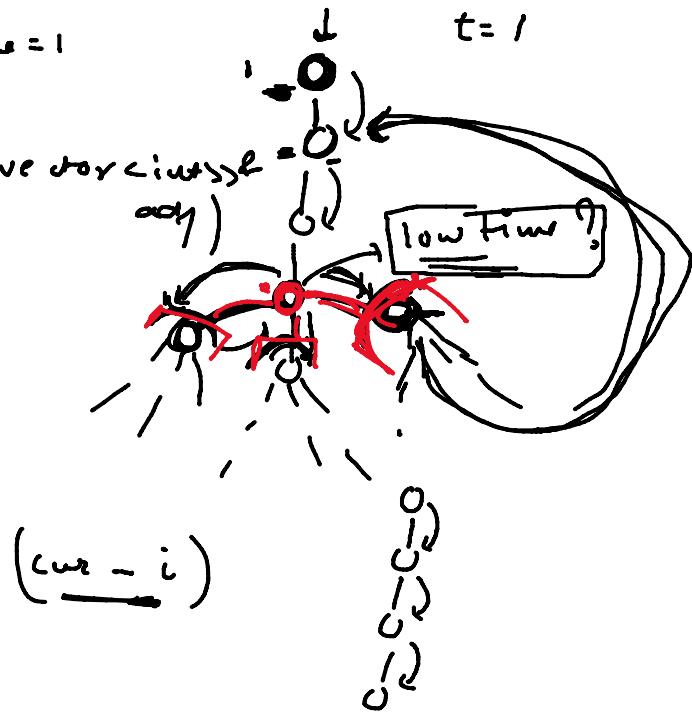
$$\text{low}[B] > \text{dis}[A]$$

$$\text{low}[B] \geq \text{dis}[A]$$

not Ndp

```
int vis[N], dis[N], low[N], time=1
```

```
void dfs ( int cur, int Par, vector<vector<int>> adj )
{
    vis[cur] = 1;
    dis[cur] = time;
    low[cur] = time;
    time++;
    int child = 0;
    for (auto i : adj[cur])
        if (!vis[i])
            dfs(i, cur, adj);
            child++;
}
```



```

    if (!vis[i])
        dfs(i, cur, adj);
        child++;
    low[cur] = min ( low[cur], low[i] );
}

```

```
else if (i != Par)
```

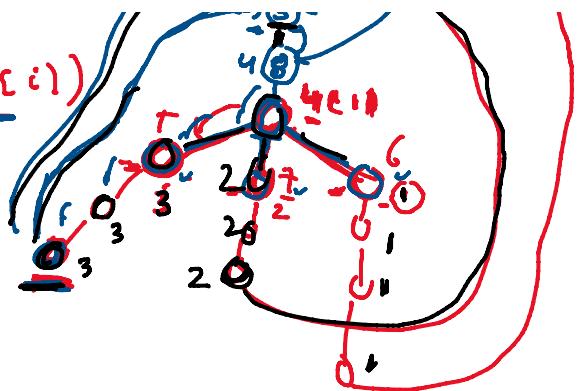
```
    low[cur] = min ( low[cur], dis[i] )
```



$\leftarrow \text{low}[cur] = \min \{\text{low}[w], \text{dis}[i]\}$

4

ii Bridge and articulation point



if ( $\text{low}[i] > \text{dis}[w]$ )

$\leftarrow$  bridge .  $\text{pb}(\text{cur}, i)$ ;

4

if ( $\text{low}[i] \geq \text{dis}[w]$  and  $w \neq \text{root}$ )

$\leftarrow$  Articulation Point .  $\text{pb}(w)$ ;

4

if ( $w = \text{root}$  and  $\text{child} \geq 1$ )

$\leftarrow$  arti-point .  $\text{pb}(w)$ ;

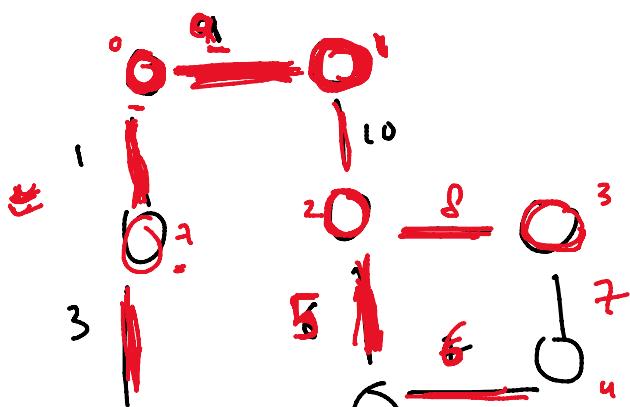
4



MST

Kruskal's alg using DSU

Prims Algorithm



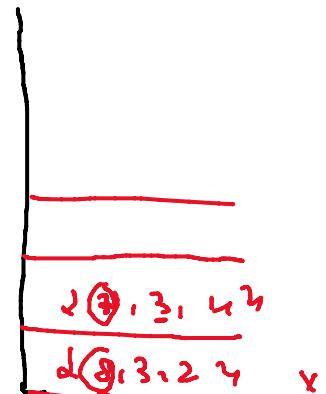
$\downarrow [5, 3, 2] Y$

$\downarrow [6, 5, 2] Y$

$\downarrow [7, 4, 5] Y$

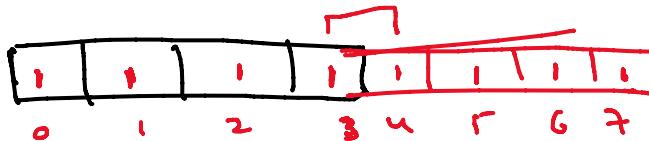
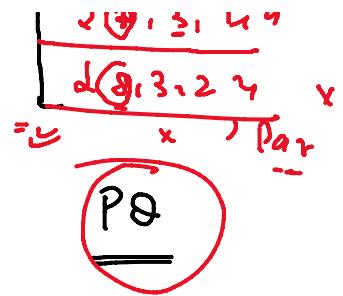
$\downarrow [8, 4, 3] X$

$\downarrow [9, 3, 2] Y$





$(\underline{u}, \underline{v}) \in E$



$\rightarrow O(\log v) \text{ or } O(n)$

```
int Parent[N];
```

```
int Key[N]; // Store distance of Node
```

```
bool mstSet[N];
```

```
For (i=0; i<n; i++)
```

```
    Key[i] = INT-MAX;
```

```
mstSet[i] = 0;
```

```
    wt[node]
```

```
Priority-queue < Pair<int, int>, vector<Pair<int, int>> &  
greater < Pair<int, int>> pq;
```

```
Key[0] = 0;
```

```
pq.push( {0, 0} );
```

```
Parent[0] = -1;
```

```
while ( !pq.empty() )
```

```
& int u = pq.top().second;
```

```
    pq.pop();  $\xrightarrow{\text{Key}(u)} = \underline{\text{pq.top().first}}$ 
```

```
mstSet[u] = true;
```

for (auto it: adj(v))

{ int v = it.first;

int wt = it.second;

$w < key(v)$

if (mstSet(v) == false && wt < key(v))

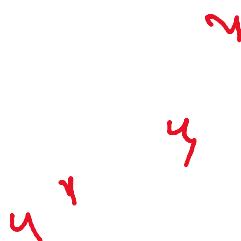
{ Parent(v) = u.

key(v) = wt;

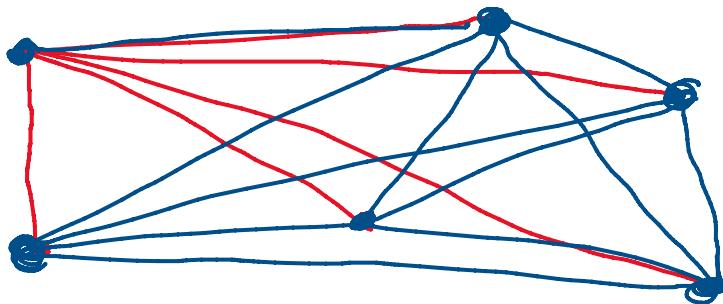
ParPush( &key(v), v, u );

key(v) = infinity

=



Graph



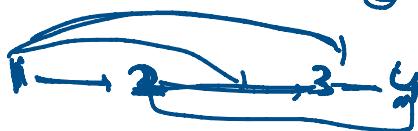
Tree

Min

Min Spanning Tree

Kruskal's Prime

(MST)



vector<vector<int>> edgeList;

For (i=0; i < Points.size(); i++)

{ int u = Point(i).id;

int y = Point(i).id;

```

For (j = i+1; j < points.size(); j++) {
    edgeList.push_back({abs(points[r][0] - u) +
        abs(points[r][1] - v), {i, j}});
}

sort(edgeList.begin(), edgeList.end());

DSU d(points.size());
int ans = 0;

for (i = 0; i < edgeList.size(); i++) {
    if (d.areSame(edgeList[i][1], edgeList[i][2])) {
        continue;
    } else {
        d.union(edgeList[i][1], edgeList[i][2]);
        ans += edgeList[i][0];
    }
}

return ans;

```