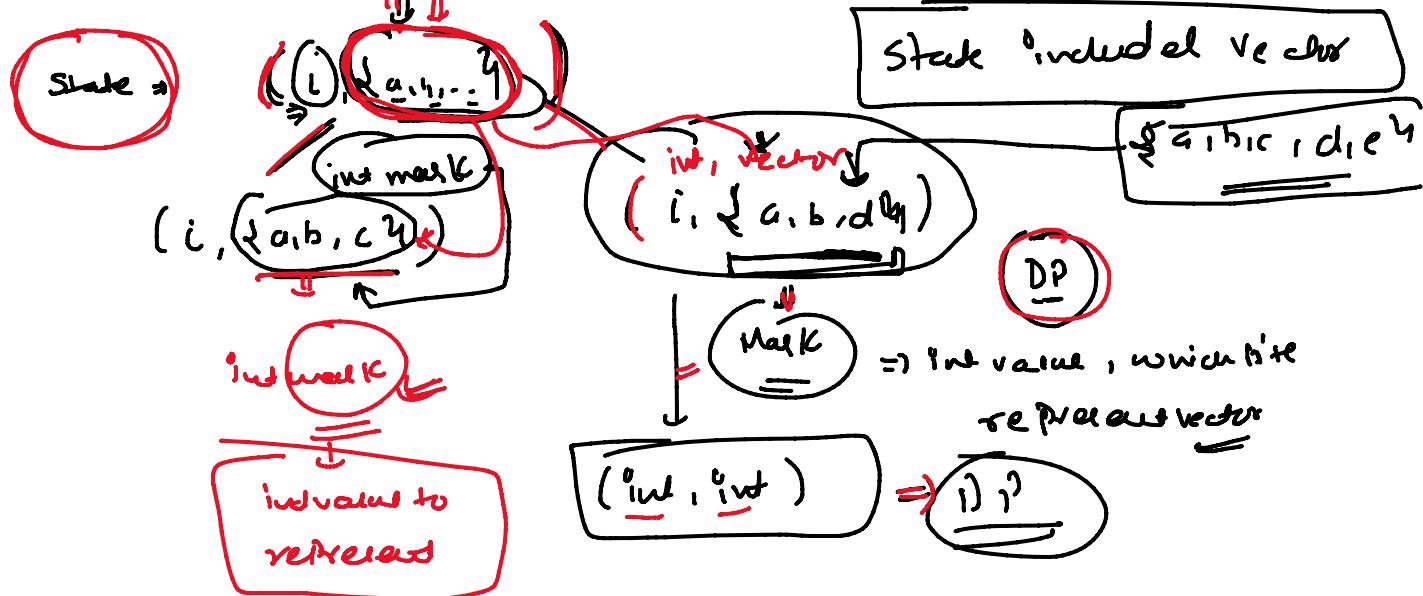
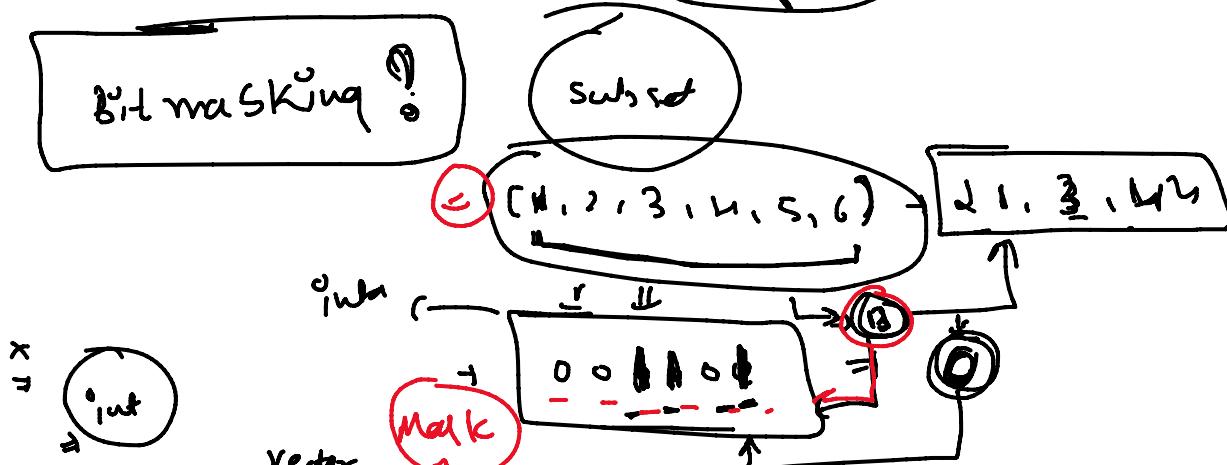


Class 91Dynamic Programming

DP with Bitmasking (Adv)



→ **N jobs**, **M workers**

every worker will do single job

$w_1 \rightarrow \underline{9 \ 2 \ 7 \ 8}$
 $w_2 \rightarrow 6 \ 1 \ 3 \ 7$
 $w_3 \rightarrow 5 \ 8 \ 1 \ 8$

incost

$0 \rightarrow i \rightarrow i^*$

i = n

$\{w_1, w_2, w_3, \dots, w_m\}$

unbounded knapsack

$w_1 = 5 \quad 8 \quad 1 \quad 8$
 $w_2 = 2 \quad 6 \quad 9 \quad 7$



No of workers ==
 No of jobs

(i^{th} , $\{w_1, w_2, \dots, w_n\}$)
 $i=n$

$\{w_1, w_2, w_3, w_4\}$

$\{2, 2, w_2, w_3, w_4\}$

$\{3, \{w_3, w_4\}\}$

$\{4, \{w_3, w_4\}\}$

Bitmasking

Solve (O , mask, workers)

mask = $O \rightarrow$

int solve (int i, int mask, vector<vector<int>> workers)

{ int n = workers.size(); if (i == n) return 0; if (dp[i][mask] != -1) return dp[i][mask];

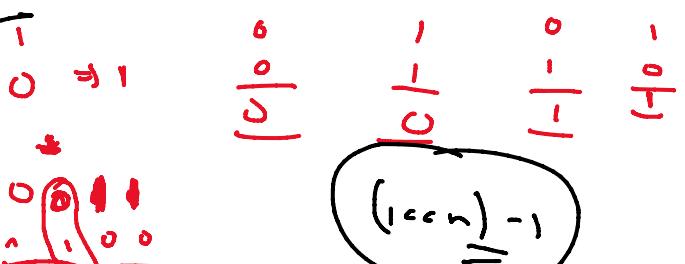
nWorkers

if (i < n)

return 0;

visited

int ans = INT_MAX;
 For (int j = 0; j < n; j++)



visitors

```

For(ind j = 0; j < n; j++)
    if (!mask & (icon[j]))

```



$(icon)_j$

{ int cost = workers[j][i] + solve(i+1, mask & (icon[i]), workers);

ans = min(ans, cost);

n dp[i][mask] =
return ans;

Backtracking / Recursion

1

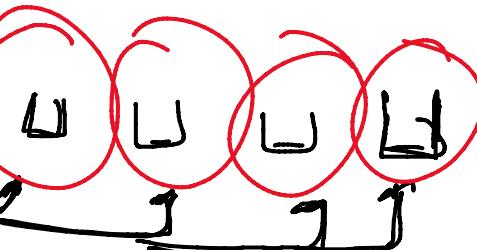
k Equal sum subset

mask

[4, 3, 2, 3, 5, 2, 1]

$$\frac{20}{4} = 5$$

k = 4



total sum of all = 0

$$\frac{20}{4} = 5$$

target(k) = total sum

$$t = \frac{\text{total sum}}{\text{target}}$$

total sum = target

Sum required in each Bucket!

$$\text{int target} = \frac{\text{total sum}}{k};$$

int n = nums.size();

int sum = 0;

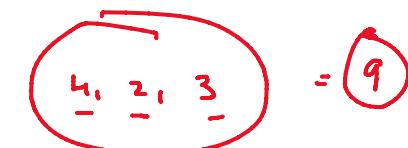
vector<int> dp(1 < n, -1);

dp[0] = 0; int cur = 0;

for (i=0; i<n; i++)
 cur += num[i];

if (cur % k) reduce target;

int tar = cur / k;



for (int mask = 0; mask < (1 < n); mask++)

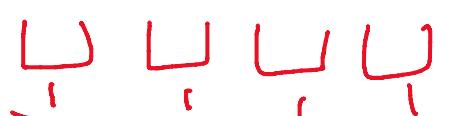
for (i=0; i<n; i++)

dp[target] = 0
 5-1 = 4

$$dp[mask + (1 \ll i)] = (dp[mask] + num[i]) \% tar$$

⑧ dp[mask] = ?

given dp[1 < n] = 5



sure element

bucket

dp[target] = 0

dp[mask] = 0

dp[target] = 1

target = -

dp[num[i]] = 0

2, 3, 5

dp[target] = 0

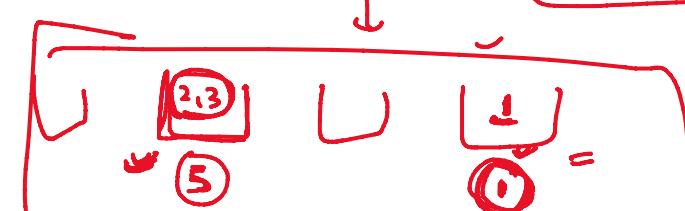
dp[target] = 5

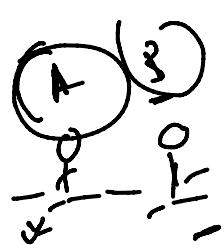
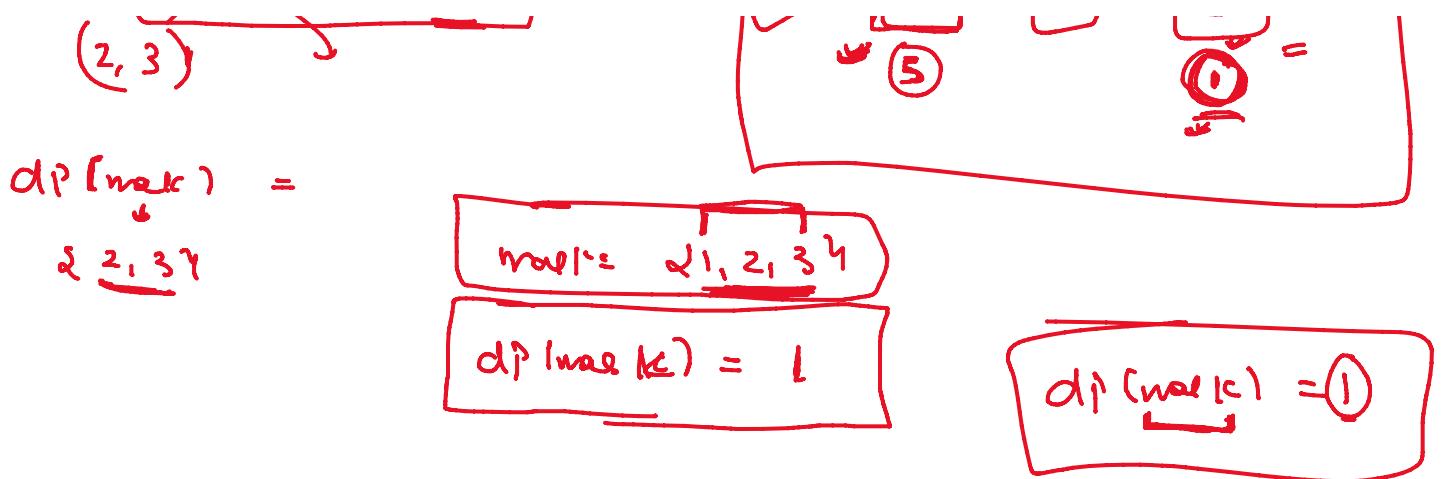
(2, 3)

5

1

0





~~Can I win~~
~~delTotal = 11~~
~~manNo = 10~~

~~52 - 10 = 42~~
~~51, 10~~

~~1 - 10~~
~~11 + 10 = 21~~
~~2 - 10~~

~~11~~
~~A~~
~~C~~

```

bool win (int manNo)
{
    if (delTotal <= 0)
        return 0;
}
    
```

~~int cur~~
~~for (i = 1; i < manNo; i++)~~
~~if ((i < c[i]) & visited == 0)~~
~~cur = win (manNo, delTotal - i, visited~~

~~(i < c[i]))~~

~~1st player~~
~~2nd player~~

$cwe = \text{win}(\text{mouse}, (\text{del total} - i), \text{visited})$
 (click)

if ($cwe == 0$)
 greater

~

~ greater ③;

