## 1. Regression discontinuity: banking recovery

After a debt has been legally declared "uncollectable" by a bank, the account is considered "charged-off." But that doesn't mean the bank *walks away* from the debt. They still want to collect some of the money they are owed. The bank will score the account to assess the expected recovery amount, that is, the expected amount that the bank may be able to receive from the customer in the future. This amount is a function of the probability of the customer paying, the total debt, and other factors that impact the ability and willingness to pay.

The bank has implemented different recovery strategies at different thresholds (\$1000, \$2000, etc.) where the greater the expected recovery amount, the more effort the bank puts into contacting the customer. For low recovery amounts (Level 0), the bank just adds the customer's contact information to their automatic dialer and emailing system. For higher recovery strategies, the bank incurs more costs as they leverage human resources in more efforts to obtain payments. Each additional level of recovery strategy requires an additional \$50 per customer so that customers in the Recovery Strategy Level 1 cost the company \$50 more than those in Level 0. Customers in Level 2 cost \$50 more than those in Level 1, etc.

**The big question**: does the extra amount that is recovered at the higher strategy level exceed the extra \$50 in costs? In other words, was there a jump (also called a "discontinuity") of more than \$50 in the amount recovered at the higher strategy level? We'll find out in this notebook.

![Regression discontinuity graph](https://assets.datacamp.com/production/project\_504/img/Regression Discontinuity graph.png)

First, we'll load the banking dataset and look at the first few rows of data. This lets us understand the dataset itself and begin thinking about how to analyze the data.

```
In [115]: # Import modules
    import pandas as pd
    import numpy as np
    # Read in dataset
    df = pd.read_csv("datasets/bank_data.csv")

# Print the first few rows of the DataFrame
    df.head()
```

### Out[115]:

	id	expected_recovery_amount	actual_recovery_amount	recovery_strategy	age	sex
0	2030	194	263.540	Level 0 Recovery	19	Male
1	1150	486	416.090	Level 0 Recovery	25	Female
2	380	527	429.350	Level 0 Recovery	27	Male
3	1838	536	296.990	Level 0 Recovery	25	Male
4	1995	541	346.385	Level 0 Recovery	34	Male

```
In [116]: %%nose
          first_value = _
          def test pandas loaded():
              assert pd. name == 'pandas', \
                   "pandas should be imported as pd."
          def test numpy loaded():
              assert np. name == 'numpy', \
                  "numpy should be imported as np."
          import pandas as pd
          def test df correctly loaded():
              correct df = pd.read csv('datasets/bank data.csv')
              assert correct df.equals(df), \
                  "The variable df should contain the data in 'datasets/bank data.csv'."
          # def test head output():
                try:
                    assert "2030" in first_value.to_string()
                except AttributeError:
                    assert False, \
                        "Please use df.head() as the last line of code in the cell to inspect the data, not the display
          () or print() functions."
                except AssertionError:
                    assert False, \
                        "Hmm, the output of the cell is not what we expected. You should see 2030 in the first five row
          s of the df DataFrame."
```

Out[116]: 3/3 tests passed

## 2. Graphical exploratory data analysis

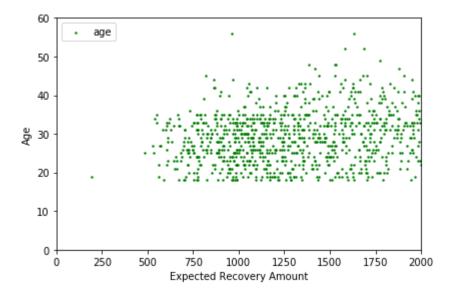
The bank has implemented different recovery strategies at different thresholds (\$1000, \$2000, \$3000 and \$5000) where the greater the Expected Recovery Amount, the more effort the bank puts into contacting the customer. Zeroing in on the first transition (between Level 0 and Level 1) means we are focused on the population with Expected Recovery Amounts between \$0 and \$2000 where the transition between Levels occurred at \$1000. We know that the customers in Level 1 (expected recovery amounts between \$1001 and \$2000) received more attention from the bank and, by definition, they had higher Expected Recovery Amounts than the customers in Level 0 (between \$1 and \$1000).

Here's a quick summary of the Levels and thresholds again:

- Level 0: Expected recovery amounts >\$0 and <=\$1000
- Level 1: Expected recovery amounts >\$1000 and <=\$2000</li>
- The threshold of \$1000 separates Level 0 from Level 1

A key question is whether there are other factors besides Expected Recovery Amount that also varied systematically across the \$1000 threshold. For example, does the customer age show a jump (discontinuity) at the \$1000 threshold or does that age vary smoothly? We can examine this by first making a scatter plot of the age as a function of Expected Recovery Amount for a small window of Expected Recovery Amount, \$0 to \$2000. This range covers Levels 0 and 1.

/usr/local/lib/python3.6/dist-packages/matplotlib/figure.py:2267: UserWarning: This figure includes Axes that are not compatible with tight\_layout, so results might be incorrect.
warnings.warn("This figure includes Axes that are not compatible "



Out[118]: 1/1 tests passed

## 3. Statistical test: age vs. expected recovery amount

We want to convince ourselves that variables such as age and sex are similar above and below the \$1000 Expected Recovery Amount threshold. This is important because we want to be able to conclude that differences in the actual recovery amount are due to the higher Recovery Strategy and not due to some other difference like age or sex.

The scatter plot of age versus Expected Recovery Amount did not show an obvious jump around \$1000. We will now do statistical analysis examining the average age of the customers just above and just below the threshold. We can start by exploring the range from \$900 to \$1100.

For determining if there is a difference in the ages just above and just below the threshold, we will use the Kruskal-Wallis test, a statistical test that makes no distributional assumptions.

```
In [119]: # Import stats module
          from scipy import stats
          # Compute average age just below and above the threshold
          era 900 1100 = df.loc[(df['expected recovery amount']<1100) &
                                 (df['expected recovery amount']>=900)]
          by recovery strategy = era 900 1100.groupby(['recovery strategy'])
          by_recovery_strategy['age'].describe().unstack()
          # Perform Kruskal-Wallis test
          Level 0 age = era 900 1100.loc[df['recovery strategy']=="Level 0 Recovery"]['age']
          Level 1 age = era 900 1100.loc[df['recovery strategy']=="Level 1 Recovery"]['age']
          stats.kruskal(Level 0 age, Level 1 age)
Out[119]: KruskalResult(statistic=3.4572342749517513, pvalue=0.06297556896097407)
In [120]: | %%nose
          def test stats loaded():
              assert 'stats' in globals(), \
               'Did you import the stats module from scipy?'
          def test level 0():
              correct Level 0 age mean= df.loc[(df['expected recovery amount']<1100) & (df['expected recovery amount']>
          =900) &
                               (df['recovery strategy']=="Level 0 Recovery")]['age'].mean()
              Level 0 age mean= Level 0 age.mean()
              assert correct Level 0 age mean == Level 0 age mean, \
                   "The mean age for Level 0 age appears to be incorrect. Did you correctly assign Level 0 age?"
          def test level 1():
              correct Level 1 age mean= df.loc[(df['expected recovery amount']<1100) & (df['expected recovery amount']>
          =900) &
                                (df['recovery strategy']=="Level 1 Recovery")]['age'].mean()
              Level 1 age mean= Level 1 age.mean()
              assert correct Level 1 age mean == Level 1 age mean, \
                  "The mean age for Level 1 age appears to be incorrect. Did you correctly assign Level 1 age?"
```

Out[120]: 3/3 tests passed

## 4. Statistical test: sex vs. expected recovery amount

We have seen that there is no major jump in the average customer age just above and just below the \$1000 threshold by doing a statistical test as well as exploring it graphically with a scatter plot.

We want to also test that the percentage of customers that are male does not jump across the \$1000 threshold. We can start by exploring the range of \$900 to \$1100 and later adjust this range.

We can examine this question statistically by developing cross-tabs as well as doing chi-square tests of the percentage of customers that are male vs. female.

```
# Number of customers in each category
In [121]:
          crosstab = pd.crosstab(df.loc[(df['expected recovery amount']<1100) &</pre>
                                         (df['expected recovery_amount']>=900)]['recovery_strategy'],
                                  df['sex'])
          print(crosstab)
          # Chi-square test
          chi2_stat, p_val, dof, ex = stats.chi2_contingency(crosstab)
          p_val
                              Female Male
          sex
          recovery strategy
          Level 0 Recovery
                                  32
                                        57
          Level 1 Recovery
                                  39
                                        55
Out[121]: 0.5377947810444592
```

Out[122]: 2/2 tests passed

## 5. Exploratory graphical analysis: recovery amount

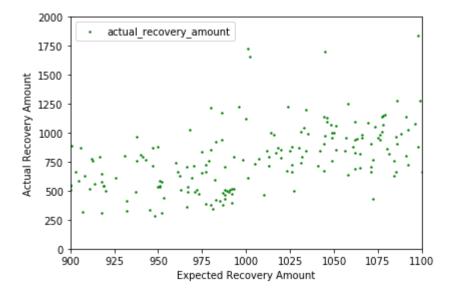
We are now reasonably confident that customers just above and just below the \$1000 threshold are, on average, similar in their average age and the percentage that are male.

It is now time to focus on the key outcome of interest, the actual recovery amount.

A first step in examining the relationship between the actual recovery amount and the expected recovery amount is to develop a scatter plot where we want to focus our attention at the range just below and just above the threshold. Specifically, we will develop a scatter plot of Expected Recovery Amount (X) versus Actual Recovery Amount (Y) for Expected Recovery Amounts between \$900 to \$1100. This range covers Levels 0 and 1. A key question is whether or not we see a discontinuity (jump) around the \$1000 threshold.

```
In [123]: # Scatter plot of Actual Recovery Amount vs. Expected Recovery Amount
    plt.scatter(x=df['expected_recovery_amount'], y=df['actual_recovery_amount'], c="g", s=2)
    plt.xlim(900, 1100)
    plt.ylim(0, 2000)
    plt.xlabel("Expected Recovery Amount")
    plt.ylabel("Actual Recovery Amount")
    plt.legend(loc=2)
    plt.show()
```

/usr/local/lib/python3.6/dist-packages/matplotlib/figure.py:2267: UserWarning: This figure includes Axes that are not compatible with tight\_layout, so results might be incorrect.
warnings.warn("This figure includes Axes that are not compatible "



Out[124]: 1/1 tests passed

# 6. Statistical analysis: recovery amount

As we did with age, we can perform statistical tests to see if the actual recovery amount has a discontinuity above the \$1000 threshold. We are going to do this for two different windows of the expected recovery amount \$900 to \$1100 and for a narrow range of \$950 to \$1050 to see if our results are consistent.

Again, we will use the Kruskal-Wallis test.

We will first compute the average actual recovery amount for those customers just below and just above the threshold using a range from \$900 to \$1100. Then we will perform a Kruskal-Wallis test to see if the actual recovery amounts are different just above and just below the threshold. Once we do that, we will repeat these steps for a smaller window of \$950 to \$1050.

#### Out[125]: KruskalResult(statistic=30.24600000000038, pvalue=3.80575314300276e-08)

```
In [126]: | %%nose
          def test level 0():
              correct Level 0 actual mean= df.loc[(df['expected recovery amount']<1050) & (df['expected recovery amoun
          t'l>=950) &
                                (df['recovery_strategy']=="Level 0 Recovery")]['actual_recovery_amount'].mean()
              Level_0_actual_mean= Level_0_actual.mean()
              assert correct Level 0 actual mean == Level 0 actual mean, \
                   "The mean actual recovery amount for Level 0 actual appears to be incorrect. Did you correctly assign
          Level 0 actual?"
          def test level 1():
              correct Level 1 actual mean= df.loc[(df['expected recovery amount']<1050) & (df['expected recovery amoun
          t']>=950) &
                                (df['recovery strategy']=="Level 1 Recovery")]['actual recovery amount'].mean()
              Level 1 actual mean= Level 1 actual.mean()
              assert correct Level 1 actual mean == Level 1 actual mean, \
                   "The mean actual recovery amount for Level 1 actual appears to be incorrect. Did you correctly assign
          Level 1 actual?"
```

Out[126]: 2/2 tests passed

# 7. Regression modeling: no threshold

We now want to take a regression-based approach to estimate the program impact at the \$1000 threshold using data that is just above and below the threshold.

We will build two models. The first model does not have a threshold while the second will include a threshold.

The first model predicts the actual recovery amount (dependent variable) as a function of the expected recovery amount (independent variable). We expect that there will be a strong positive relationship between these two variables.

We will examine the adjusted R-squared to see the percent of variance explained by the model. In this model, we are not representing the threshold but simply seeing how the variable used for assigning the customers (expected recovery amount) relates to the outcome variable (actual recovery amount)

```
In [127]: # Import statsmodels
import statsmodels.api as sm

# Define X and y
X = era_900_1100['expected_recovery_amount']
y = era_900_1100['actual_recovery_amount']
X = sm.add_constant(X)

# Build linear regression model
model = sm.OLS(y, X).fit()
predictions = model.predict(X)

# Print out the model summary statistics
model.summary()
```

### Out[127]:

**OLS Regression Results** 

Dep. Variable:	actual_recovery_amount	R-squared:	0.261
Model:	OLS	Adj. R-squared:	0.256
Method:	Least Squares	F-statistic:	63.78
Date:	Wed, 10 Jun 2020	Prob (F-statistic):	1.56e-13
Time:	03:19:57	Log-Likelihood:	-1278.9
No. Observations:	183	AIC:	2562.
Df Residuals:	181	BIC:	2568.
Df Model:	1		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
const	-1978.7597	347.741	-5.690	0.000	-2664.907	-1292.612
expected_recovery_amount	2.7577	0.345	7.986	0.000	2.076	3.439

 Omnibus:
 64.493
 Durbin-Watson:
 1.777

 Prob(Omnibus):
 0.000
 Jarque-Bera (JB):
 185.818

 Skew:
 1.463
 Prob(JB):
 4.47e-41

 Kurtosis:
 6.977
 Cond. No.
 1.80e+04

#### Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.8e+04. This might indicate that there are strong multicollinearity or other numerical problems.

```
In [128]: | %%nose
          def test x():
              correct x= df.loc[(df['expected recovery amount']<1100) & (df['expected recovery amount']>=900)]['expecte
          d recovery amount'l
              correct x = sm.add constant(correct x)
              assert correct x['expected recovery amount'].mean() == X['expected recovery amount'].mean(), \
                   "The mean expected recovery amount for X appears incorrect. Check your assignment of X. It should in
          clude expected recovery amount and indicator 1000 when the expected recovery amount is <1100 and >=900."
          def test v():
              correct y= df.loc[(df['expected recovery amount']<1100) & (df['expected recovery amount']>=900)]['actual
          recovery amount']
              assert correct y.mean() == y.mean(), \
                  "The mean actual recovery amount for y appears incorrect. Check your assignment of y. It should inclu
          de the actual recovery amount when the expected recovery amount is <1100 and >=900."
          # def test df correctly loaded():
                correct model = sm.OLS(v,x).fit()
                assert correct model.params[1] == model.params[1], \
                     "Check your assignment of model. It should be equal to sm.OLS(v,X).fit()."
```

Out[128]: 2/2 tests passed

## 8. Regression modeling: adding true threshold

From the first model, we see that the expected recovery amount's regression coefficient is statistically significant.

The second model adds an indicator of the true threshold to the model (in this case at \$1000).

We will create an indicator variable (either a 0 or a 1) that represents whether or not the expected recovery amount was greater than \$1000. When we add the true threshold to the model, the regression coefficient for the true threshold represents the additional amount recovered due to the higher recovery strategy. That is to say, the regression coefficient for the true threshold measures the size of the discontinuity for customers just above and just below the threshold.

If the higher recovery strategy helped recovery more money, then the regression coefficient of the true threshold will be greater than zero. If the higher recovery strategy did not help recovery more money, then the regression coefficient will not be statistically significant.

### Out[129]:

**OLS Regression Results** 

Dep. Variable:	actual_recovery_amount	R-squared:	0.261
Model:	OLS	Adj. R-squared:	0.256
Method:	Least Squares	F-statistic:	63.78
Date:	Wed, 10 Jun 2020	Prob (F-statistic):	1.56e-13
Time:	03:19:57	Log-Likelihood:	-1278.9
No. Observations:	183	AIC:	2562.
Df Residuals:	181	BIC:	2568.
Df Model:	1		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
const	-1978.7597	347.741	-5.690	0.000	-2664.907	-1292.612
expected_recovery_amount	2.7577	0.345	7.986	0.000	2.076	3.439

Omnibus: 64.493 Durbin-Watson: 1.777

Prob(Omnibus): 0.000 Jarque-Bera (JB): 185.818

**Skew:** 1.463 **Prob(JB):** 4.47e-41

**Kurtosis:** 6.977 **Cond. No.** 1.80e+04

#### Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.8e+04. This might indicate that there are strong multicollinearity or other numerical problems.

```
In [130]: \%\nose
          def test x():
              correct x= df.loc[(df['expected recovery amount']<1100) & (df['expected recovery amount']>=900),
                     ['expected recovery amount', 'indicator 1000']]
              correct x = sm.add constant(correct x)
              assert correct x['expected recovery amount'].mean() == X['expected recovery amount'].mean(), \
                  "The mean expected recovery amount for X appears incorrect. Check your assignment of X. It should in
          clude expected recovery amount and indicator 1000 when the expected recovery amount is <1100 and >=900."
          def test v():
              correct y= df.loc[(df['expected recovery amount']<1100) & (df['expected recovery amount']>=900)]['actual
          recovery amount']
              assert correct y.mean() == y.mean(), \
                  "The mean actual recovery amount for y appears incorrect. Check your assignment of y. It should inclu
          de the actual recovery amount when the expected recovery amount is <1100 and >=900."
          # def test df correctly loaded():
                correct model = sm.OLS(v,X).fit()
                assert correct model.params[1] == model.params[1], \
                    "Check your assignment of model. It should be equal to sm.OLS(v,X).fit()."
```

Out[130]: 2/2 tests passed

# 9. Regression modeling: adjusting the window

The regression coefficient for the true threshold was statistically significant with an estimated impact of around \$278. This is much larger than the \$50 per customer needed to run this higher recovery strategy.

Before showing this to our manager, we want to convince ourselves that this result wasn't due to choosing an expected recovery amount window of \$900 to \$1100. Let's repeat this analysis for the window from \$950 to \$1050 to see if we get similar results.

The answer? Whether we use a wide (\$900 to \$1100) or narrower window (\$950 to \$1050), the incremental recovery amount at the higher recovery strategy is much greater than the \$50 per customer it costs for the higher recovery strategy. So we conclude that the higher recovery strategy is worth the extra cost of \$50 per customer.

### Out[131]:

**OLS Regression Results** 

Dep. Variable:	actual_recovery_amount	R-squared:	0.283
Model:	OLS	Adj. R-squared:	0.269
Method:	Least Squares	F-statistic:	18.99
Date:	Wed, 10 Jun 2020	Prob (F-statistic):	1.12e-07
Time:	03:19:57	Log-Likelihood:	-692.92
No. Observations:	99	AIC:	1392.
Df Residuals:	96	BIC:	1400.
Df Model:	2		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
const	-279.5243	1840.707	-0.152	0.880	-3933.298	3374.250
expected_recovery_amount	0.9189	1.886	0.487	0.627	-2.825	4.663
indicator_1000	286.5337	111.352	2.573	0.012	65.502	507.566

 Omnibus:
 39.302
 Durbin-Watson:
 1.955

 Prob(Omnibus):
 0.000
 Jarque-Bera (JB):
 82.258

 Skew:
 1.564
 Prob(JB):
 1.37e-18

 Kurtosis:
 6.186
 Cond. No.
 6.81e+04

### Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 6.81e+04. This might indicate that there are strong multicollinearity or other numerical problems.

```
In [132]: %%nose
          def test x():
              correct x= df.loc[(df['expected recovery amount']<1050) & (df['expected recovery amount']>=950),['expecte
          d recovery amount', 'indicator 1000']]
              correct x = sm.add constant(correct x)
              assert correct x['expected recovery amount'].mean() == X['expected recovery amount'].mean(), \
                  "The mean expected recovery amount for X appears incorrect. Check your assignment of X. It should in
          clude expected recovery amount and indicator 1000 when the expected recovery amount is <1050 and >=950."
          def test v():
              correct y= df.loc[(df['expected recovery amount']<1050) & (df['expected recovery amount']>=950)]['actual
          recovery amount']
              assert correct y.mean() == y.mean(), \
                   "The mean actual recovery amount for y appears incorrect. Check your assignment of y. It should inclu
          de the actual recovery amount when the expected recovery amount is <1050 and >=950."
          # def test df correctly loaded():
                correct model = sm.OLS(v,X).fit()
                assert correct model.params[1] == model.params[1], \
                    "Check your assignment of model. It should be equal to sm.OLS(v,X).fit()."
```

#### Out[132]: 2/2 tests passed

```
In [ ]:
```