Complex PyTorch for Music Genre Classification

```
In [28]: # Complex pytorch
         import torch
         import torch.nn as nn
         import torch.nn.functional as F
         from torch.utils.data import DataLoader
         from torchvision import datasets, transforms
         from complexPyTorch.complexLayers import *
         from complexPyTorch.complexFunctions import *
         from torch_geometric.nn import GCNConv
         from torch_geometric.data import Data
         # Plot
         import matplotlib.pyplot as plt
         import seaborn as sns
         import time
         # Load Data
         import numpy as np
         import json
         import os
         import math
         import librosa
         import pathlib
         from scipy.spatial.distance import cdist
         from torch.utils.data import Dataset
         from sklearn.model_selection import train_test_split
         import random
         # MFCCS
         from scipy.io import wavfile
         import scipy.fftpack as fft
         from scipy.signal import get_window
```

Data Preparation

MFCCS

```
In [31]: class MusicFeatureExtractorComplex2:
             def __init__(self, FFT_size=2048, HOP_SIZE=512, mel_filter_num=13, dc
                 self.FFT size = FFT size
                 self.HOP_SIZE = HOP_SIZE
                 self.mel_filter_num = mel_filter_num
                 self.dct_filter_num = dct_filter_num
                 self.epsilon = 1e-10 # Added to log to avoid log10(0)
             def normalize_audio(self, audio):
                 audio = audio / np.max(np.abs(audio))
                 return audio
             def frame_audio(self, audio):
                 frame_num = int((len(audio) - self.FFT_size) / self.HOP_SIZE) + 1
                 frames = np.zeros((frame_num, self.FFT_size))
                 for n in range(frame_num):
                     frames[n] = audio[n * self.HOP_SIZE: n * self.HOP_SIZE + self
                 return frames
             def freq_to_mel(self, freq):
                 return 2595.0 * np.log10(1.0 + freq / 700.0)
             def met_to_freq(self, mels):
                 return 700.0 * (10.0 ** (mels / 2595.0) - 1.0)
             def get_filter_points(self, fmin, fmax, sample_rate):
                 fmin_mel = self.freq_to_mel(fmin)
                 fmax_mel = self.freq_to_mel(fmax)
                 mels = np.linspace(fmin_mel, fmax_mel, num=self.mel_filter_num +
                 freqs = self.met_to_freq(mels)
                 return np.floor((self.FFT_size + 1) / sample_rate * freqs).astype
             def get_filters(self, filter_points):
                 filters = np.zeros((len(filter_points) - 2, int(self.FFT_size / 2
                 for n in range(len(filter_points) - 2):
                     filters[n, filter_points[n]: filter_points[n + 1]] = np.linsp
                     filters[n, filter_points[n + 1]: filter_points[n + 2]] = np.l
                 return filters
             def dct(self):
                 basis = np.empty((self.dct_filter_num, self.mel_filter_num))
                 basis[0, :] = 1.0 / np.sqrt(self.mel_filter_num)
                 samples = np.arange(1, 2 * self.mel_filter_num, 2) * np.pi / (2.0)
                 for i in range(1, self.dct_filter_num):
                     basis[i, :] = np.cos(i * samples) * np.sqrt(2.0 / self.mel_fi
                 return basis
             def get_mfcc_features(self, audio, sample_rate):
                 audio = self.normalize_audio(audio)
                 audio framed = self.frame audio(audio)
                 window = get_window("hann", self.FFT_size, fftbins=True)
                 audio_win = audio_framed * window
                 audio_winT = np.transpose(audio_win)
                 audio_fft = np.empty((int(1 + self.FFT_size // 2), audio_winT.sha
                 for n in range(audio_fft.shape[1]):
                     audio_fft[:, n] = fft.fft(audio_winT[:, n], axis=0)[:audio_ff
                 audio_fft = np.transpose(audio_fft)
                 mag_fft = np.square(np.abs(audio_fft))
                 phase_fft = np.angle(audio_fft)
```

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freq_min = 0
freq_high = sample_rate / 2
filter_points, mel_freqs = self.get_filter_points(freq_min, freq_
filters = self.get_filters(filter_points)
audio_filtered = np.dot(filters, np.transpose(mag_fft))
phase_filtered = np.dot(filters, np.transpose(phase_fft))
audio_filtered = np.maximum(audio_filtered, self.epsilon) # Repl
audio_log = 10.0 * np.log10(audio_filtered)
dct_filters = self.dct()
cepstral_coefficents = np.dot(dct_filters, audio_log)
phase_coefficents = np.dot(dct_filters, phase_filtered)
return np.array([cepstral_coefficents]), np.array([phase_coeffice
```

```
In [32]: class GenreDatasetMFCC(Dataset):
             def __init__(self, train_path, n_fft=2048, hop_length=512, num_segmen
                 cur_path = pathlib.Path(train_path)
                 self.files = []
                 for i in list(cur_path.rglob("*.wav")):
                      for j in range(num_segments):
                          self.files.append([j, i])
                 self.samples_per_segment = int(SAMPLES_PER_TRACK / num_segments)
                 self.n_fft = n_fft
                 self.hop_length = hop_length
                 self.num_segments = num_segments
                 self.dct_filter_num = dct_filter_num
                 self.training = training
             def apply_augmentations(self, signal):
                 # Apply augmentations to the audio signal
                 if random.random() < 0.5:</pre>
                      signal = librosa.effects.pitch_shift(signal, sr=SAMPLE_RATE,
                 if random.random() < 0.5:</pre>
                      signal = librosa.effects.time_stretch(signal, rate=random.uni
                  return signal
             def adjust_shape(self, sequence, max_sequence_length = 126):
                 current_length = sequence.shape[2]
                 if current_length < max_sequence_length:</pre>
                      padding = np.zeros((1, 13, max_sequence_length - current_leng
                      padded_sequence = np.concatenate((sequence, padding), axis=2)
                 else:
                      padded_sequence = sequence[:, :, :max_sequence_length]
                  return padded_sequence
             def len (self):
                 return len(self.files)
             def __getitem__(self, idx):
                 cur_file = self.files[idx]
                 d = cur file[0]
                 file_path = cur_file[1]
                 target = genre mappings[str(file path).split("/")[2]]
                 signal, sample_rate = librosa.load(file_path, sr=SAMPLE_RATE)
                 start = self.samples_per_segment * d
                 finish = start + self.samples_per_segment
                 cur signal = signal[start:finish]
                 if self training: cur_signal = self.apply_augmentations(cur_signal
                 cur_mfcc = self.mfcc_extractor.get_mfcc_features(cur_signal, samp
                 cur_mfcc = self.adjust_shape(cur_mfcc)
```

```
return torch.tensor(cur_mfcc, dtype=torch.float32), target
class GenreDatasetPhaseMFCC2(GenreDatasetMFCC);
   def __init__(self, train_path, n_fft=2048, hop_length=512, num_segmen
        super().__init__(train_path, n_fft, hop_length, num_segments, mel
        self.mfcc_extractor = MusicFeatureExtractorComplex2(
            FFT size=n fft, HOP SIZE=hop length, mel filter num = mel fil
   def __getitem__(self, idx):
        cur_file = self.files[idx]
        d = cur file[0]
        file path = cur file[1]
        target = genre_mappings[str(file_path).split("/")[2]]
        signal, sample_rate = librosa.load(file_path, sr=SAMPLE_RATE)
        start = self.samples_per_segment * d
        finish = start + self.samples_per_segment
        cur_signal = signal[start:finish]
        if self training: cur_signal = self apply_augmentations(cur_signal)
        cur_mfcc, cur_phase = self.mfcc_extractor.get_mfcc_features(cur_s
        cur_mfcc, cur_phase = self.adjust_shape(cur_mfcc), self.adjust_sh
        return torch.tensor(cur_mfcc, dtype=torch.float32), torch.tensor(
```

In [33]: train_dataset = GenreDatasetPhaseMFCC2("Data/train/", n_fft=2048, hop_len
 test_dataset = GenreDatasetPhaseMFCC2("Data/test/", n_fft=2048, hop_lengt
 train_loader = torch.utils.data.DataLoader(dataset=train_dataset, shuffle
 test_loader = torch.utils.data.DataLoader(dataset=test_dataset, shuffle=F

1. Simple Graph Net (Only magnitude)

```
In [34]: def train(model, device, train_loader, test_loader, optimizer, epoch, met
             model.train()
             total_loss = 0
             correct = 0
             total_samples = len(train_loader.dataset)
             start_time = time.time()
             for batch_idx, (data, data2, target) in enumerate(train_loader):
                 data, data2, target = data.to(device), data2.to(device), target.t
                 optimizer.zero_grad()
                 output = model(data)
                 loss = F.nll_loss(output, target)
                 loss.backward()
                 optimizer.step()
                 total_loss += loss.item()
                 pred = output.argmax(dim=1, keepdim=True)
                 correct += pred.eq(target.view_as(pred)).sum().item()
                 if batch_idx % 100 == 0:
                      batch_accuracy = 100. * correct / ((batch_idx + 1) * len(data
                      print('Train Epoch: {:3} [{:6}/{:6} ({:3.0f}%)]\tLoss: {:.6f}
                          epoch,
                          batch_idx * len(data),
                          total_samples,
                          100. * batch_idx / len(train_loader),
                         loss.item(),
                         batch_accuracy)
```

```
end time = time.time()
epoch_times = metrics_dict['epoch_times']
epoch_times.append(end_time - start_time)
epoch_loss = total_loss / len(train_loader)
epoch accuracy = 100. * correct / total samples
train_losses = metrics_dict['train_losses']
train accuracies = metrics dict['train accuracies']
train_losses.append(epoch_loss)
train_accuracies.append(epoch_accuracy)
print('Epoch {} - Time: {:.2f}s - Train Loss: {:.6f} - Train Accuracy
# Evaluate on test data
model.eval()
test_loss = 0
correct = 0
with torch.no_grad():
    for data, data2, target in test_loader:
        data, data2, target = data.to(device), data2.to(device), targ
        output = model(data)
        test_loss += F.nll_loss(output, target, reduction='sum').item
        pred = output.argmax(dim=1, keepdim=True)
        correct += pred.eq(target.view_as(pred)).sum().item()
test_loss /= len(test_loader.dataset)
test_accuracy = 100. * correct / len(test_loader.dataset)
test_losses = metrics_dict['test_losses']
test_accuracies = metrics_dict['test_accuracies']
test_losses.append(test_loss)
test_accuracies.append(test_accuracy)
print('Test Loss: {:.6f} - Test Accuracy: {:.2f}%\n'.format(test_loss
def __init__(self):
```

```
In [35]: class ComplexGraphNet(nn.Module):
                 super(ComplexGraphNet, self).__init__()
                 self.gnn_layer = GCNConv(in_channels=126, out_channels=126, node_
                 self.conv1 = ComplexConv2d(1, 10, 2, 1)
                 self.bn = ComplexBatchNorm2d(10)
                 self.conv2 = ComplexConv2d(10, 20, 2, 1)
                 self.fc1 = ComplexLinear(30*2*20, 500)
                 self.fc2 = ComplexLinear(500, 10)
             def forward(self, x): # Pass edge_index for GNN
                 batch_size, _, num_nodes, node_size = x.size()
                 edge_index = torch.tensor([[i, j] for i in range(num_nodes) for j
                 x = x.view(-1, num_nodes, node_size) # Reshape for batch process
                 x = self.gnn_layer(x, edge_index)
                 x = x.unsqueeze(1)
                 x = x.type(torch.complex64)
                 x = self.conv1(x)
                 x = complex_relu(x)
                 x = complex_max_pool2d(x, 2, 2)
                 x = self.bn(x)
                 x = self.conv2(x)
                 x = complex_relu(x)
                 x = complex max pool2d(x, 2, 2)
                 x = x.view(batch_size, -1) # Reshape back to batched form
                 x = self.fc1(x)
                 x = complex_relu(x)
```

```
x = self.fc2(x)
        x = x.abs()
        x = F.\log_softmax(x, dim=1)
        return x
device = torch.device('cuda' if torch.cuda.is_available() else 'cpu')
model = ComplexGraphNet().to(device)
optimizer = torch.optim.SGD(model.parameters(), lr=0.01, momentum=0.9)
metrics_dict_e1 = {
    'epoch_times': [],
    'train_losses': [],
    'train_accuracies': [],
    'test_losses': [],
    'test_accuracies': []
}
for epoch in range(NUM_EPOCHS):
    train(model,
          device,
          train_loader,
          test_loader,
          optimizer,
          epoch,
          metrics_dict_e1)
print("-"*100)
print("-"*100)
print("FINAL RESULTS:")
print("-"*100)
for key, value in metrics_dict_e1.items():
    print(f'{key}: {value}')
```

```
0 [
Train Epoch:
                      0/ 8390 ( 0%)] Loss: 2.283815 Accuracy: 9.38%
              0 [ 3200/ 8390 ( 38%)] Loss: 2.285956 Accuracy: 15.53%
0 [ 6400/ 8390 ( 76%)] Loss: 2.140933 Accuracy: 17.06%
Train Epoch:
Train Epoch:
Epoch 0 - Time: 233.97s - Train Loss: 2.234477 - Train Accuracy: 17.37%
Test Loss: 2.186637 - Test Accuracy: 20.44%
                      0/ 8390 ( 0%)] Loss: 2.173024 Accuracy: 25.00%
Train Epoch:
               1 [
Train Epoch:
              1 [ 3200/ 8390 ( 38%)] Loss: 2.406570 Accuracy: 19.15%
              1 [ 6400/ 8390 ( 76%)] Loss: 2.102077 Accuracy: 19.45%
Train Epoch:
Epoch 1 - Time: 226.15s - Train Loss: 2.182805 - Train Accuracy: 19.19%
Test Loss: 2.154018 - Test Accuracy: 20.75%
Train Epoch:
              2 [
                      0/ 8390 ( 0%)] Loss: 2.015391 Accuracy: 34.38%
              2 [ 3200/ 8390 ( 38%)] Loss: 2.243402 Accuracy: 19.06%
Train Epoch:
Train Epoch:
               2 [ 6400/ 8390 ( 76%)] Loss: 2.275811 Accuracy: 19.56%
Epoch 2 - Time: 236.52s - Train Loss: 2.171332 - Train Accuracy: 19.48%
Test Loss: 2.191294 - Test Accuracy: 17.31%
                      0/ 8390 ( 0%)] Loss: 2.239104 Accuracy: 9.38%
Train Epoch:
              3 [
Train Epoch:
              3 [ 3200/ 8390 ( 38%)] Loss: 2.304262 Accuracy: 20.39%
              3 [ 6400/ 8390 ( 76%)] Loss: 2.138627 Accuracy: 20.20%
Train Epoch:
Epoch 3 - Time: 238.93s - Train Loss: 2.166512 - Train Accuracy: 19.83%
Test Loss: 2.181513 - Test Accuracy: 18.69%
Train Epoch:
              4 [
                      0/ 8390 ( 0%)] Loss: 2.182257 Accuracy: 15.62%
              4 [ 3200/ 8390 ( 38%)] Loss: 2.212053 Accuracy: 20.45%
Train Epoch:
              4 [ 6400/ 8390 (76%)] Loss: 2.122830 Accuracy: 21.21%
Train Epoch:
Epoch 4 - Time: 239.38s - Train Loss: 2.143740 - Train Accuracy: 20.86%
Test Loss: 2.133375 - Test Accuracy: 22.38%
              5 [
                      0/ 8390 ( 0%)] Loss: 2.226711 Accuracy: 18.75%
Train Epoch:
                   3200/ 8390 ( 38%)] Loss: 2.121426 Accuracy: 21.10%
               5 [
Train Epoch:
              5 [ 6400/ 8390 ( 76%)] Loss: 1.933081 Accuracy: 21.39%
Train Epoch:
Epoch 5 - Time: 236.68s - Train Loss: 2.138812 - Train Accuracy: 21.49%
Test Loss: 2.176407 - Test Accuracy: 18.31%
              6 [
                      0/ 8390 ( 0%)] Loss: 2.114547 Accuracy: 12.50%
Train Epoch:
              6 [ 3200/ 8390 ( 38%)] Loss: 2.301475 Accuracy: 22.03%
Train Epoch:
              6 [ 6400/ 8390 ( 76%)] Loss: 2.247961 Accuracy: 21.08%
Train Epoch:
Epoch 6 - Time: 237.03s - Train Loss: 2.130672 - Train Accuracy: 21.20%
Test Loss: 2.145782 - Test Accuracy: 21.50%
              7 [
                      0/ 8390 ( 0%)] Loss: 2.018586 Accuracy: 37.50%
Train Epoch:
Train Epoch:
              7 [ 3200/ 8390 ( 38%)] Loss: 2.011729 Accuracy: 21.04%
Train Epoch:
              7 [ 6400/ 8390 ( 76%)] Loss: 2.357390 Accuracy: 22.05%
Epoch 7 - Time: 239.32s - Train Loss: 2.122056 - Train Accuracy: 21.80%
Test Loss: 2.176117 - Test Accuracy: 19.69%
              8 [
                      0/ 8390 ( 0%)] Loss: 2.233269 Accuracy: 18.75%
Train Epoch:
              8 [ 3200/ 8390 ( 38%)] Loss: 2.092553 Accuracy: 20.39%
Train Epoch:
Train Epoch:
              8 [ 6400/ 8390 ( 76%)] Loss: 2.221566 Accuracy: 21.10%
Epoch 8 - Time: 242.28s - Train Loss: 2.119308 - Train Accuracy: 21.44%
Test Loss: 2.113507 - Test Accuracy: 22.31%
Train Epoch:
              9 [
                      0/ 8390 ( 0%)] Loss: 1.932667 Accuracy: 37.50%
Train Epoch:
              9 [ 3200/ 8390 ( 38%)] Loss: 2.014356 Accuracy: 22.71%
              9 [ 6400/ 8390 ( 76%)] Loss: 2.107163 Accuracy: 22.62%
Train Epoch:
Epoch 9 - Time: 240.29s - Train Loss: 2.099407 - Train Accuracy: 22.24%
Test Loss: 2.145893 - Test Accuracy: 19.19%
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Train Epoch: 10 [
                      0/ 8390 ( 0%)] Loss: 2.220515 Accuracy: 15.62%
Train Epoch: 10 [ 3200/ 8390 ( 38%)] Loss: 2.189619 Accuracy: 21.94%
Train Epoch: 10 [ 6400/ 8390 ( 76%)] Loss: 1.973737 Accuracy: 22.68%
Epoch 10 - Time: 241.49s - Train Loss: 2.108154 - Train Accuracy: 22.80%
Test Loss: 2.145267 - Test Accuracy: 22.25%
                      0/ 8390 ( 0%)] Loss: 2.138165 Accuracy: 18.75%
Train Epoch: 11 [
Train Epoch: 11 [ 3200/ 8390 ( 38%)] Loss: 2.291169 Accuracy: 23.05%
Train Epoch: 11 [ 6400/ 8390 ( 76%)] Loss: 2.173194 Accuracy: 22.84%
Epoch 11 - Time: 237.19s - Train Loss: 2.095983 - Train Accuracy: 22.82%
Test Loss: 2.097750 - Test Accuracy: 23.88%
Train Epoch: 12 [
                      0/ 8390 ( 0%)] Loss: 1.984829 Accuracy: 25.00%
Train Epoch: 12 [ 3200/ 8390 ( 38%)] Loss: 1.933785 Accuracy: 23.58%
Train Epoch: 12 [ 6400/ 8390 ( 76%)] Loss: 1.954490 Accuracy: 23.97%
Epoch 12 - Time: 233.34s - Train Loss: 2.078130 - Train Accuracy: 24.18%
Test Loss: 2.239533 - Test Accuracy: 18.81%
                      0/ 8390 ( 0%)] Loss: 2.180044 Accuracy: 15.62%
Train Epoch: 13 [
Train Epoch: 13 [ 3200/ 8390 ( 38%)] Loss: 1.909034 Accuracy: 24.29%
Train Epoch: 13 [ 6400/ 8390 ( 76\%)] Loss: 2.191316 Accuracy: 23.17%
Epoch 13 - Time: 231.77s - Train Loss: 2.090801 - Train Accuracy: 23.71%
Test Loss: 2.107307 - Test Accuracy: 25.00%
Train Epoch: 14 [
                      0/ 8390 ( 0%)] Loss: 2.004154 Accuracy: 21.88%
Train Epoch: 14 [ 3200/ 8390 ( 38%)] Loss: 1.827421 Accuracy: 24.16%
Train Epoch: 14 [ 6400/ 8390 ( 76%)] Loss: 2.039760 Accuracy: 24.61%
Epoch 14 - Time: 228.70s - Train Loss: 2.073023 - Train Accuracy: 24.37%
Test Loss: 2.113122 - Test Accuracy: 21.69%
Train Epoch: 15 [
                      0/ 8390 ( 0%)] Loss: 2.098036 Accuracy: 12.50%
             15 [ 3200/ 8390 ( 38%)] Loss: 1.838435 Accuracy: 23.73%
Train Epoch:
            15 [ 6400/ 8390 ( 76%)] Loss: 2.227892 Accuracy: 24.07%
Train Epoch:
Epoch 15 - Time: 228.27s - Train Loss: 2.051294 - Train Accuracy: 24.35%
Test Loss: 2.088547 - Test Accuracy: 26.12%
                      0/ 8390 ( 0%)] Loss: 2.222553 Accuracy: 18.75%
Train Epoch: 16 [
Train Epoch: 16 [ 3200/ 8390 ( 38%)] Loss: 2.005491 Accuracy: 25.31%
            16 [ 6400/ 8390 ( 76%)] Loss: 2.025543 Accuracy: 25.36%
Train Epoch:
Epoch 16 - Time: 228.22s - Train Loss: 2.059692 - Train Accuracy: 25.40%
Test Loss: 2.077507 - Test Accuracy: 25.62%
Train Epoch: 17 [
                      0/ 8390 ( 0%)] Loss: 2.034314 Accuracy: 18.75%
Train Epoch: 17 [ 3200/ 8390 ( 38%)] Loss: 1.842534 Accuracy: 28.56%
Train Epoch: 17 [ 6400/ 8390 (76%)] Loss: 2.120786 Accuracy: 27.05%
Epoch 17 - Time: 226.93s - Train Loss: 2.034155 - Train Accuracy: 26.52%
Test Loss: 2.073564 - Test Accuracy: 24.38%
                      0/ 8390 ( 0%)] Loss: 2.023822 Accuracy: 25.00%
Train Epoch: 18 [
Train Epoch: 18 [ 3200/ 8390 ( 38%)] Loss: 1.873845 Accuracy: 26.64%
Train Epoch: 18 [ 6400/ 8390 (76%)] Loss: 2.002745 Accuracy: 26.00%
Epoch 18 - Time: 227.17s - Train Loss: 2.036771 - Train Accuracy: 25.69%
Test Loss: 2.069038 - Test Accuracy: 25.81%
Train Epoch: 19 [
                      0/ 8390 ( 0%)] Loss: 2.088804 Accuracy: 21.88%
Train Epoch: 19 [ 3200/ 8390 ( 38%)] Loss: 1.972812 Accuracy: 25.93%
Train Epoch: 19 [ 6400/ 8390 ( 76%)] Loss: 1.902578 Accuracy: 25.47%
Epoch 19 - Time: 228.38s - Train Loss: 2.030699 - Train Accuracy: 26.22%
Test Loss: 2.080796 - Test Accuracy: 24.94%
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Train Epoch: 20 [
                      0/ 8390 ( 0%)] Loss: 1.757594 Accuracy: 31.25%
Train Epoch: 20 [ 3200/ 8390 ( 38%)] Loss: 2.131952 Accuracy: 25.93%
Train Epoch: 20 [ 6400/ 8390 ( 76%)] Loss: 1.976331 Accuracy: 25.65%
Epoch 20 - Time: 234.30s - Train Loss: 2.032363 - Train Accuracy: 25.85%
Test Loss: 2.099731 - Test Accuracy: 25.19%
                      0/ 8390 ( 0%)] Loss: 1.994877 Accuracy: 21.88%
Train Epoch: 21 [
Train Epoch: 21 [ 3200/ 8390 ( 38%)] Loss: 2.212613 Accuracy: 25.96%
Train Epoch: 21 [ 6400/ 8390 ( 76%)] Loss: 1.958855 Accuracy: 25.64%
Epoch 21 - Time: 225.82s - Train Loss: 2.027406 - Train Accuracy: 26.23%
Test Loss: 2.047946 - Test Accuracy: 25.31%
Train Epoch: 22 [
                      0/ 8390 ( 0%)] Loss: 2.057194 Accuracy: 28.12%
Train Epoch: 22 [ 3200/ 8390 ( 38%)] Loss: 1.830850 Accuracy: 27.51%
Train Epoch: 22 [ 6400/ 8390 ( 76%)] Loss: 1.977901 Accuracy: 27.15%
Epoch 22 - Time: 225.02s - Train Loss: 2.001441 - Train Accuracy: 26.96%
Test Loss: 2.053808 - Test Accuracy: 25.69%
                      0/ 8390 ( 0%)] Loss: 2.087957 Accuracy: 18.75%
Train Epoch: 23 [
Train Epoch: 23 [ 3200/ 8390 ( 38%)] Loss: 1.934952 Accuracy: 28.22%
Train Epoch: 23 [ 6400/ 8390 ( 76\%)] Loss: 2.093279 Accuracy: 27.61%
Epoch 23 - Time: 224.18s - Train Loss: 1.999862 - Train Accuracy: 27.32%
Test Loss: 2.041623 - Test Accuracy: 25.56%
Train Epoch: 24 [
                      0/ 8390 ( 0%)] Loss: 1.804892 Accuracy: 37.50%
Train Epoch: 24 [ 3200/ 8390 ( 38%)] Loss: 2.206030 Accuracy: 27.78%
Train Epoch: 24 [ 6400/ 8390 ( 76%)] Loss: 1.932141 Accuracy: 27.08%
Epoch 24 - Time: 224.50s - Train Loss: 1.996928 - Train Accuracy: 27.57%
Test Loss: 2.081249 - Test Accuracy: 24.62%
                      0/ 8390 ( 0%)] Loss: 1.818998 Accuracy: 37.50%
Train Epoch:
             25 [
             25 [ 3200/ 8390 ( 38%)] Loss: 2.048907 Accuracy: 28.50%
Train Epoch:
             25 [ 6400/ 8390 ( 76%)] Loss: 2.009765 Accuracy: 27.57%
Train Epoch:
Epoch 25 - Time: 224.85s - Train Loss: 1.990574 - Train Accuracy: 27.56%
Test Loss: 2.069043 - Test Accuracy: 24.44%
                      0/ 8390 ( 0%)] Loss: 1.843599 Accuracy: 37.50%
Train Epoch: 26 [
Train Epoch: 26 [ 3200/ 8390 ( 38%)] Loss: 2.136900 Accuracy: 27.44%
            26 [ 6400/ 8390 ( 76%)] Loss: 1.867156 Accuracy: 27.89%
Train Epoch:
Epoch 26 - Time: 227.72s - Train Loss: 1.986620 - Train Accuracy: 28.12%
Test Loss: 2.048724 - Test Accuracy: 24.69%
Train Epoch: 27 [
                      0/ 8390 ( 0%)] Loss: 1.889203 Accuracy: 31.25%
Train Epoch: 27 [ 3200/ 8390 ( 38%)] Loss: 1.977899 Accuracy: 28.34%
Train Epoch: 27 [ 6400/ 8390 (76%)] Loss: 2.176792 Accuracy: 27.83%
Epoch 27 - Time: 226.10s - Train Loss: 1.995100 - Train Accuracy: 27.88%
Test Loss: 2.056802 - Test Accuracy: 25.62%
Train Epoch: 28 [
                      0/ 8390 ( 0%)] Loss: 1.990392 Accuracy: 31.25%
Train Epoch: 28 [ 3200/ 8390 ( 38%)] Loss: 1.947343 Accuracy: 27.88%
Train Epoch: 28 [ 6400/ 8390 (76%)] Loss: 2.123044 Accuracy: 28.00%
Epoch 28 - Time: 223.05s - Train Loss: 1.985914 - Train Accuracy: 27.91%
Test Loss: 2.034711 - Test Accuracy: 25.69%
Train Epoch: 29 [
                      0/ 8390 ( 0%)] Loss: 1.824628 Accuracy: 43.75%
Train Epoch: 29 [ 3200/ 8390 ( 38%)] Loss: 1.940703 Accuracy: 29.21%
Train Epoch: 29 [ 6400/ 8390 ( 76%)] Loss: 2.051470 Accuracy: 28.28%
Epoch 29 - Time: 223.30s - Train Loss: 1.970584 - Train Accuracy: 28.46%
Test Loss: 2.062386 - Test Accuracy: 26.69%
```

```
Train Epoch: 30 [
                      0/ 8390 ( 0%)] Loss: 1.932767 Accuracy: 31.25%
Train Epoch: 30 [ 3200/ 8390 ( 38%)] Loss: 2.009117 Accuracy: 29.02%
Train Epoch: 30 [ 6400/ 8390 ( 76%)] Loss: 1.938020 Accuracy: 28.51%
Epoch 30 - Time: 221.56s - Train Loss: 1.964117 - Train Accuracy: 28.62%
Test Loss: 2.015479 - Test Accuracy: 28.25%
                      0/ 8390 ( 0%)] Loss: 1.612053 Accuracy: 43.75%
Train Epoch: 31 [
Train Epoch: 31 [ 3200/ 8390 ( 38%)] Loss: 1.733670 Accuracy: 29.73%
Train Epoch: 31 [ 6400/ 8390 ( 76%)] Loss: 1.920024 Accuracy: 29.20%
Epoch 31 - Time: 223.11s - Train Loss: 1.956306 - Train Accuracy: 29.24%
Test Loss: 2.053814 - Test Accuracy: 27.62%
Train Epoch: 32 [
                      0/ 8390 ( 0%)] Loss: 1.901363 Accuracy: 25.00%
Train Epoch: 32 [ 3200/ 8390 ( 38%)] Loss: 1.922382 Accuracy: 30.14%
Train Epoch: 32 [ 6400/ 8390 ( 76%)] Loss: 2.035112 Accuracy: 29.73%
Epoch 32 - Time: 220.86s - Train Loss: 1.951182 - Train Accuracy: 29.58%
Test Loss: 2.034440 - Test Accuracy: 25.69%
                      0/ 8390 ( 0%)] Loss: 1.991580 Accuracy: 25.00%
Train Epoch: 33 [
Train Epoch: 33 [ 3200/ 8390 ( 38%)] Loss: 1.911169 Accuracy: 30.82%
Train Epoch: 33 [ 6400/ 8390 ( 76\%)] Loss: 1.893150 Accuracy: 30.53%
Epoch 33 - Time: 225.68s - Train Loss: 1.944604 - Train Accuracy: 29.99%
Test Loss: 2.033751 - Test Accuracy: 25.94%
Train Epoch: 34 [
                      0/ 8390 ( 0%)] Loss: 1.752453 Accuracy: 31.25%
Train Epoch: 34 [ 3200/ 8390 ( 38%)] Loss: 1.883572 Accuracy: 30.17%
Train Epoch: 34 [ 6400/ 8390 ( 76%)] Loss: 1.837702 Accuracy: 29.49%
Epoch 34 - Time: 223.98s - Train Loss: 1.946527 - Train Accuracy: 29.62%
Test Loss: 2.073126 - Test Accuracy: 26.44%
             35 [
                      0/ 8390 ( 0%)] Loss: 2.025464 Accuracy: 25.00%
Train Epoch:
                  3200/ 8390 ( 38%)] Loss: 1.954219 Accuracy: 29.95%
Train Epoch:
             35 [
             35 [ 6400/ 8390 ( 76%)] Loss: 1.886833 Accuracy: 29.94%
Train Epoch:
Epoch 35 - Time: 223.24s - Train Loss: 1.936648 - Train Accuracy: 29.68%
Test Loss: 2.020539 - Test Accuracy: 27.81%
                      0/ 8390 ( 0%)] Loss: 1.900638 Accuracy: 25.00%
Train Epoch: 36 [
Train Epoch: 36 [ 3200/ 8390 ( 38%)] Loss: 1.862369 Accuracy: 30.14%
Train Epoch: 36 [ 6400/ 8390 ( 76%)] Loss: 1.809317 Accuracy: 30.36%
Epoch 36 - Time: 227.75s - Train Loss: 1.942515 - Train Accuracy: 30.13%
Test Loss: 2.031603 - Test Accuracy: 25.81%
Train Epoch: 37 [
                      0/ 8390 ( 0%)] Loss: 2.025652 Accuracy: 21.88%
Train Epoch: 37 [ 3200/ 8390 ( 38%)] Loss: 1.811957 Accuracy: 30.32%
Train Epoch: 37 [ 6400/ 8390 ( 76%)] Loss: 2.013695 Accuracy: 30.66%
Epoch 37 - Time: 222.05s - Train Loss: 1.927433 - Train Accuracy: 30.36%
Test Loss: 2.051604 - Test Accuracy: 26.31%
                      0/ 8390 ( 0%)] Loss: 1.649459 Accuracy: 43.75%
Train Epoch: 38 [
Train Epoch: 38 [ 3200/ 8390 ( 38%)] Loss: 2.124419 Accuracy: 31.37%
Train Epoch: 38 [ 6400/ 8390 (76%)] Loss: 1.922676 Accuracy: 30.77%
Epoch 38 - Time: 230.87s - Train Loss: 1.921546 - Train Accuracy: 31.20%
Test Loss: 2.057478 - Test Accuracy: 28.44%
Train Epoch: 39 [
                      0/ 8390 ( 0%)] Loss: 2.099957 Accuracy: 18.75%
Train Epoch: 39 [ 3200/ 8390 ( 38%)] Loss: 2.118045 Accuracy: 31.87%
Train Epoch: 39 [ 6400/ 8390 ( 76%)] Loss: 1.844247 Accuracy: 31.67%
Epoch 39 - Time: 227.03s - Train Loss: 1.904664 - Train Accuracy: 31.55%
Test Loss: 2.079740 - Test Accuracy: 24.88%
```

```
Train Epoch: 40 [
                      0/ 8390 ( 0%)] Loss: 2.131852 Accuracy: 25.00%
Train Epoch: 40 [ 3200/ 8390 ( 38%)] Loss: 1.620973 Accuracy: 31.68%
Train Epoch: 40 [ 6400/ 8390 ( 76%)] Loss: 2.101529 Accuracy: 31.31%
Epoch 40 - Time: 226.69s - Train Loss: 1.911417 - Train Accuracy: 31.11%
Test Loss: 2.053170 - Test Accuracy: 26.00%
                      0/ 8390 ( 0%)] Loss: 1.750316 Accuracy: 34.38%
Train Epoch: 41 [
Train Epoch: 41 [ 3200/ 8390 ( 38%)] Loss: 1.904465 Accuracy: 30.69%
Train Epoch: 41 [ 6400/ 8390 ( 76%)] Loss: 1.963924 Accuracy: 31.19%
Epoch 41 - Time: 225.56s - Train Loss: 1.904321 - Train Accuracy: 31.17%
Test Loss: 2.053985 - Test Accuracy: 27.31%
Train Epoch: 42 [
                      0/ 8390 ( 0%)] Loss: 1.974954 Accuracy: 28.12%
Train Epoch: 42 [ 3200/ 8390 ( 38%)] Loss: 1.891893 Accuracy: 31.96%
Train Epoch: 42 [ 6400/ 8390 ( 76%)] Loss: 1.921841 Accuracy: 32.59%
Epoch 42 - Time: 225.97s - Train Loss: 1.895247 - Train Accuracy: 32.32%
Test Loss: 1.997389 - Test Accuracy: 28.06%
                      0/ 8390 ( 0%)] Loss: 1.914194 Accuracy: 31.25%
Train Epoch: 43 [
Train Epoch: 43 [ 3200/ 8390 ( 38%)] Loss: 1.982564 Accuracy: 32.67%
Train Epoch: 43 [ 6400/ 8390 ( 76\%)] Loss: 2.258419 Accuracy: 32.65%
Epoch 43 - Time: 223.78s - Train Loss: 1.899233 - Train Accuracy: 32.44%
Test Loss: 2.024002 - Test Accuracy: 27.38%
Train Epoch: 44 [
                      0/ 8390 ( 0%)] Loss: 1.560061 Accuracy: 50.00%
Train Epoch: 44 [ 3200/ 8390 ( 38%)] Loss: 1.845327 Accuracy: 32.92%
Train Epoch: 44 [ 6400/ 8390 ( 76%)] Loss: 2.210847 Accuracy: 32.40%
Epoch 44 - Time: 226.01s - Train Loss: 1.893218 - Train Accuracy: 32.04%
Test Loss: 2.061902 - Test Accuracy: 24.31%
Train Epoch: 45 [
                      0/ 8390 ( 0%)] Loss: 1.775600 Accuracy: 43.75%
             45 [ 3200/ 8390 ( 38%)] Loss: 1.951963 Accuracy: 32.24%
Train Epoch:
Train Epoch: 45 [ 6400/ 8390 (76%)] Loss: 1.674304 Accuracy: 31.95%
Epoch 45 - Time: 225.07s - Train Loss: 1.889554 - Train Accuracy: 32.03%
Test Loss: 2.012643 - Test Accuracy: 28.81%
                      0/ 8390 ( 0%)] Loss: 1.857784 Accuracy: 34.38%
Train Epoch: 46 [
Train Epoch: 46 [ 3200/ 8390 ( 38%)] Loss: 1.889494 Accuracy: 33.79%
Train Epoch: 46 [ 6400/ 8390 ( 76%)] Loss: 1.861357 Accuracy: 32.76%
Epoch 46 - Time: 225.23s - Train Loss: 1.875798 - Train Accuracy: 32.97%
Test Loss: 2.018404 - Test Accuracy: 28.50%
Train Epoch: 47 [
                      0/ 8390 ( 0%)] Loss: 2.024217 Accuracy: 31.25%
Train Epoch: 47 [ 3200/ 8390 ( 38%)] Loss: 1.554365 Accuracy: 32.58%
Train Epoch: 47 [ 6400/ 8390 ( 76%)] Loss: 1.847797 Accuracy: 31.98%
Epoch 47 - Time: 224.48s - Train Loss: 1.879617 - Train Accuracy: 32.55%
Test Loss: 2.083142 - Test Accuracy: 27.81%
Train Epoch: 48 [
                      0/ 8390 ( 0%)] Loss: 1.864645 Accuracy: 37.50%
Train Epoch: 48 [ 3200/ 8390 ( 38%)] Loss: 2.004141 Accuracy: 32.12%
Train Epoch: 48 [ 6400/ 8390 (76%)] Loss: 1.954044 Accuracy: 32.56%
Epoch 48 - Time: 222.04s - Train Loss: 1.873967 - Train Accuracy: 32.67%
Test Loss: 2.052414 - Test Accuracy: 26.94%
Train Epoch: 49 [
                      0/ 8390 ( 0%)] Loss: 1.916777 Accuracy: 40.62%
Train Epoch: 49 [ 3200/ 8390 ( 38%)] Loss: 1.728014 Accuracy: 33.48%
Train Epoch: 49 [ 6400/ 8390 ( 76%)] Loss: 1.615704 Accuracy: 33.26%
Epoch 49 - Time: 1162.20s - Train Loss: 1.856905 - Train Accuracy: 33.05%
Test Loss: 2.021979 - Test Accuracy: 28.06%
```

FINAL RESULTS:

epoch times: [233.97046875953674, 226.14852595329285, 236.52325081825256, 238.92535185813904, 239.38257002830505, 236.6788511276245, 237.02662801742 554, 239.32301020622253, 242.27710700035095, 240.29133009910583, 241.49365 496635437, 237.19384503364563, 233.34383893013, 231.7748110294342, 228.695 59788703918, 228.27052807807922, 228.22335124015808, 226.9341676235199, 22 7.17398810386658, 228.38212084770203, 234.2978479862213, 225.821125984191 9, 225.02131295204163, 224.1751549243927, 224.49942111968994, 224.85096287 727356, 227.71697902679443, 226.1047580242157, 223.05186772346497, 223.297 59693145752, 221.56133818626404, 223.107741355896, 220.85710501670837, 22 5.68304800987244, 223.97671675682068, 223.2411026954651, 227.7453482151031 5, 222.0526521205902, 230.87250208854675, 227.02583384513855, 226.69209814 071655, 225.56455397605896, 225.97482013702393, 223.7847821712494, 226.007 67278671265, 225.06873416900635, 225.23424696922302, 224.47550320625305, 2 22.03592991828918, 1162.1967041492462] train_losses: [2.234476645029228, 2.1828049061862567, 2.171332196879933, 2.166512229515396, 2.1437400169954954, 2.138811717051586, 2.13067216045073 86, 2.1220557052670546, 2.1193076758894303, 2.099406872996847, 2.108154222 2554446, 2.0959825861545007, 2.0781302060789733, 2.0908009400804533, 2.073 023048066001, 2.051294315862292, 2.0596924214872696, 2.0341545625497366, 2.0367706076789447, 2.0306985701313454, 2.0323631217461506, 2.027406216577 7194, 2.0014411761560513, 1.9998621972462602, 1.9969276835900227, 1.990574 1105552848, 1.9866200831100231, 1.9950999772275677, 1.985913817664139, 1.9 705841104492887, 1.9641166929980272, 1.9563061344714565, 1.951182177958597 6, 1.9446035810099302, 1.9465266179492455, 1.9366483128707828, 1.942514810 853332, 1.9274329051716637, 1.9215455496584186, 1.9046635550397042, 1.9114 173896440112, 1.9043212164449328, 1.8952473711421471, 1.899233222917746, 1.8932179776766829, 1.8895541998266263, 1.8757984788363216, 1.879616890699 8088, 1.873966821732412, 1.8569049575856624] train_accuracies: [17.36591179976162, 19.189511323003575, 19.4755661501787 86, 19.833134684147794, 20.858164481525627, 21.489868891537544, 21.2038140 64362337, 21.799761620977353, 21.442193087008345, 22.240762812872468, 22.8 00953516090583, 22.824791418355186, 24.183551847437425, 23.70679380214541 3, 24.37425506555423, 24.35041716328963, 25.399284862932063, 26.5196662693 68294, 25.68533969010727, 26.221692491060786, 25.852205005959476, 26.23361 1442193087, 26.96066746126341, 27.31823599523242, 27.568533969010726, 27.5 5661501787843, 28.116805721096544, 27.878426698450536, 27.914183551847437, 28.462455303933254, 28.61740166865316, 29.237187127532778, 29.582836710369 488, 29.9880810488677, 29.61859356376639, 29.67818831942789, 30.1311084624 55305, 30.357568533969012, 31.203814064362337, 31.549463647199048, 31.1084 62455303933, 31.168057210965436, 32.32419547079857, 32.44338498212157, 32. 038140643623365, 32.02622169249106, 32.967818831942786, 32.55065554231228, 32.66984505363528, 33.05125148986889] test losses: [2.1866367852687834, 2.154017615318298, 2.1912943744659423, 2.1815134119987487, 2.1333746206760407, 2.176407445669174, 2.1457816970348 36, 2.176116580963135, 2.1135067558288574, 2.145893280506134, 2.1452674436 569215, 2.0977504682540893, 2.2395331597328187, 2.1073072028160094, 2.1131 2224149704, 2.088547270298004, 2.077507041692734, 2.0735635244846344, 2.06 90382504463196, 2.080795907974243, 2.0997307825088503, 2.0479457080364227, 2.0538084936141967, 2.041623057126999, 2.0812490618228914, 2.0690434098243 715, 2.0487236738204957, 2.0568019306659697, 2.0347112727165224, 2.0623856 341838835, 2.015479021072388, 2.0538138830661774, 2.0344402396678927, 2.03 37510764598847, 2.0731262707710267, 2.0205389261245728, 2.031603275537490

6, 2.0516035866737368, 2.057477984428406, 2.079739997386932, 2.05316980123

5199, 2.0539849162101746, 1.9973892450332642, 2.0240018010139464, 2.061902 1534919737, 2.0126427090168, 2.018404322862625, 2.0831423473358153, 2.0524 144637584687, 2.02197856426239] test_accuracies: [20.4375, 20.75, 17.3125, 18.6875, 22.375, 18.3125, 21.5, 19.6875, 22.3125, 19.1875, 22.25, 23.875, 18.8125, 25.0, 21.6875, 26.125, 25.625, 24.375, 25.8125, 24.9375, 25.1875, 25.3125, 25.6875, 25.5625, 24.6 25, 24.4375, 24.6875, 25.625, 25.6875, 26.6875, 26.25, 27.625, 25.6875, 25.9375, 26.4375, 27.8125, 25.8125, 26.3125, 28.4375, 24.875, 26.0, 27.312 5, 28.0625, 27.375, 24.3125, 28.8125, 28.5, 27.8125, 26.9375, 28.0625]

2. Simple Graph Net (Magniude + phase wieghts)

```
In [36]: def train(model, device, train_loader, test_loader, optimizer, epoch, met
             model.train()
             total loss = 0
             correct = 0
             total_samples = len(train_loader.dataset)
             start_time = time.time()
             for batch_idx, (data, data2, target) in enumerate(train_loader):
                 data, data2, target = data.to(device), data2.to(device), target.t
                 optimizer.zero_grad()
                 output = model([data, data2])
                 loss = F.nll_loss(output, target)
                 loss.backward()
                 optimizer.step()
                 total_loss += loss.item()
                 pred = output.argmax(dim=1, keepdim=True)
                 correct += pred.eq(target.view_as(pred)).sum().item()
                 if batch_idx % 100 == 0:
                      batch_accuracy = 100. * correct / ((batch_idx + 1) * len(data
                      print('Train Epoch: {:3} [{:6}/{:6} ({:3.0f}%)]\tLoss: {:.6f}
                          epoch,
                          batch_idx * len(data),
                          total_samples,
                          100. * batch_idx / len(train_loader),
                          loss.item(),
                         batch accuracy)
                      )
             end_time = time.time()
             epoch_times = metrics_dict['epoch_times']
             epoch_times.append(end_time - start_time)
             epoch_loss = total_loss / len(train_loader)
             epoch_accuracy = 100. * correct / total_samples
             train_losses = metrics_dict['train_losses']
             train_accuracies = metrics_dict['train_accuracies']
             train_losses.append(epoch_loss)
             train accuracies.append(epoch accuracy)
             print('Epoch {} - Time: {:.2f}s - Train Loss: {:.6f} - Train Accuracy
             # Evaluate on test data
             model.eval()
             test_loss = 0
             correct = 0
             with torch.no grad():
                 for data, data2, target in test_loader:
```

```
data, data2, target = data.to(device), data2.to(device), targ
                     output = model([data, data2])
                     test_loss += F.nll_loss(output, target, reduction='sum').item
                     pred = output.argmax(dim=1, keepdim=True)
                     correct += pred.eq(target.view_as(pred)).sum().item()
             test_loss /= len(test_loader.dataset)
             test accuracy = 100. * correct / len(test loader.dataset)
             test_losses = metrics_dict['test_losses']
             test_accuracies = metrics_dict['test_accuracies']
             test_losses.append(test_loss)
             test accuracies.append(test accuracy)
             print('Test Loss: {:.6f} - Test Accuracy: {:.2f}%\n'.format(test_loss
In [37]: class ComplexGraphNet(nn.Module):
             def __init__(self):
                 super(ComplexGraphNet, self).__init__()
                 self.gnn_layer = GCNConv(in_channels=126, out_channels=126, node_
                 self.conv1 = ComplexConv2d(1, 10, 2, 1)
                 self.bn = ComplexBatchNorm2d(10)
                 self.conv2 = ComplexConv2d(10, 20, 2, 1)
                 self.fc1 = ComplexLinear(30*2*20, 500)
                 self.fc2 = ComplexLinear(500, 10)
             def forward(self, x): # Pass edge_index for GNN
                 x, phase_data = x[0], x[1]
                 batch_size, _, num_nodes, node_size = x.size()
                 edge_index = torch.tensor([[i, j] for i in range(num_nodes) for j
                 phase_data = torch.mean(phase_data.view(-1, num_nodes, node_size)
                 edge_weight = torch.tensor([torch.mean(np.abs(phase_data[edge_ind
                                                                phase_data[edge_ind
                                              for i in range(len(edge_index[0]))])
                 x = x.view(-1, num_nodes, node_size) # Reshape for batch process
                 x = self.gnn_layer(x, edge_index, edge_weight)
                 x = x.unsqueeze(1)
                 x = x.type(torch.complex64)
                 x = self.conv1(x)
                 x = complex_relu(x)
                 x = complex_max_pool2d(x, 2, 2)
                 x = self.bn(x)
                 x = self.conv2(x)
                 x = complex_relu(x)
                 x = complex_max_pool2d(x, 2, 2)
                 x = x.view(batch_size, -1) # Reshape back to batched form
                 x = self.fc1(x)
                 x = complex_relu(x)
                 x = self.fc2(x)
                 x = x.abs()
                 x = F.\log_softmax(x, dim=1)
                 return x
         device = torch.device('cuda' if torch.cuda.is available() else 'cpu')
         model = ComplexGraphNet().to(device)
         optimizer = torch.optim.SGD(model.parameters(), lr=0.01, momentum=0.9)
         metrics dict e2 = {
              'epoch times': [],
              'train_losses': [],
             'train_accuracies': [],
```

```
'test_losses': [],
    'test_accuracies': []
for epoch in range(NUM_EPOCHS):
    train(model,
          device,
          train_loader,
          test_loader,
          optimizer,
          epoch,
          metrics_dict_e2)
print("-"*100)
print("-"*100)
print("FINAL RESULTS:")
print("-"*100)
for key, value in metrics_dict_e2.items():
    print(f'{key}: {value}')
```

```
0 [
Train Epoch:
                      0/ 8390 ( 0%)] Loss: 2.479136 Accuracy: 6.25%
              0 [ 3200/ 8390 ( 38%)] Loss: 2.111964 Accuracy: 16.49%
Train Epoch:
              0 [ 6400/ 8390 ( 76%)] Loss: 2.072670 Accuracy: 18.86%
Train Epoch:
Epoch 0 - Time: 1216.79s - Train Loss: 2.162852 - Train Accuracy: 19.68%
Test Loss: 2.109093 - Test Accuracy: 22.25%
                      0/ 8390 ( 0%)] Loss: 1.894730 Accuracy: 25.00%
Train Epoch:
              1 [
Train Epoch:
              1 [ 3200/ 8390 ( 38%)] Loss: 2.064820 Accuracy: 22.62%
              1 [ 6400/ 8390 ( 76%)] Loss: 2.095362 Accuracy: 23.46%
Train Epoch:
Epoch 1 - Time: 237.43s - Train Loss: 2.037587 - Train Accuracy: 24.28%
Test Loss: 2.066230 - Test Accuracy: 23.56%
Train Epoch:
              2 [
                      0/ 8390 ( 0%)] Loss: 2.163065 Accuracy: 21.88%
              2 [ 3200/ 8390 ( 38%)] Loss: 2.177595 Accuracy: 26.21%
Train Epoch:
Train Epoch:
              2 [ 6400/ 8390 ( 76%)] Loss: 1.961488 Accuracy: 26.90%
Epoch 2 - Time: 3536.20s - Train Loss: 1.987517 - Train Accuracy: 26.82%
Test Loss: 2.096034 - Test Accuracy: 21.19%
                      0/ 8390 ( 0%)] Loss: 2.063694 Accuracy: 25.00%
Train Epoch:
              3 [
Train Epoch:
              3 [ 3200/ 8390 ( 38%)] Loss: 1.783233 Accuracy: 26.98%
              3 [ 6400/ 8390 ( 76%)] Loss: 2.109796 Accuracy: 27.33%
Train Epoch:
Epoch 3 - Time: 255.05s - Train Loss: 1.977226 - Train Accuracy: 27.37%
Test Loss: 1.984386 - Test Accuracy: 26.75%
Train Epoch:
              4 [
                      0/ 8390 ( 0%)] Loss: 1.770829 Accuracy: 46.88%
              4 [ 3200/ 8390 ( 38%)] Loss: 1.907099 Accuracy: 26.30%
Train Epoch:
              4 [ 6400/ 8390 (76%)] Loss: 2.030431 Accuracy: 26.40%
Train Epoch:
Epoch 4 - Time: 338.99s - Train Loss: 1.973808 - Train Accuracy: 26.90%
Test Loss: 1.946919 - Test Accuracy: 28.12%
              5 [
                      0/ 8390 ( 0%)] Loss: 1.673114 Accuracy: 53.12%
Train Epoch:
                  3200/ 8390 ( 38%)] Loss: 1.919456 Accuracy: 28.34%
              5 [
Train Epoch:
              5 [ 6400/ 8390 ( 76%)] Loss: 2.014733 Accuracy: 29.12%
Train Epoch:
Epoch 5 - Time: 249.76s - Train Loss: 1.922926 - Train Accuracy: 29.37%
Test Loss: 1.960438 - Test Accuracy: 29.12%
                      0/ 8390 ( 0%)] Loss: 1.968090 Accuracy: 25.00%
Train Epoch:
              6 [
              6 [ 3200/ 8390 ( 38%)] Loss: 1.901110 Accuracy: 29.86%
Train Epoch:
              6 [ 6400/ 8390 ( 76%)] Loss: 2.166843 Accuracy: 30.22%
Train Epoch:
Epoch 6 - Time: 260.97s - Train Loss: 1.913745 - Train Accuracy: 30.00%
Test Loss: 2.020193 - Test Accuracy: 25.06%
              7 [
                      0/ 8390 ( 0%)] Loss: 1.990562 Accuracy: 28.12%
Train Epoch:
Train Epoch:
              7 [ 3200/ 8390 ( 38%)] Loss: 1.973588 Accuracy: 31.13%
Train Epoch:
              7 [ 6400/ 8390 ( 76%)] Loss: 1.772776 Accuracy: 30.99%
Epoch 7 - Time: 290.29s - Train Loss: 1.895390 - Train Accuracy: 31.13%
Test Loss: 2.053939 - Test Accuracy: 31.88%
              8 [
                      0/ 8390 ( 0%)] Loss: 1.993796 Accuracy: 25.00%
Train Epoch:
              8 [ 3200/ 8390 ( 38%)] Loss: 1.942533 Accuracy: 31.50%
Train Epoch:
Train Epoch:
              8 [ 6400/ 8390 ( 76%)] Loss: 1.756390 Accuracy: 30.89%
Epoch 8 - Time: 2350.99s - Train Loss: 1.899573 - Train Accuracy: 30.83%
Test Loss: 2.063662 - Test Accuracy: 28.69%
Train Epoch:
              9 [
                      0/ 8390 ( 0%)] Loss: 1.870236 Accuracy: 43.75%
Train Epoch:
              9 [ 3200/ 8390 ( 38%)] Loss: 1.853202 Accuracy: 31.96%
              9 [ 6400/ 8390 ( 76%)] Loss: 1.817463 Accuracy: 32.51%
Train Epoch:
Epoch 9 - Time: 1119.26s - Train Loss: 1.858082 - Train Accuracy: 32.37%
Test Loss: 1.877559 - Test Accuracy: 30.88%
```

```
Train Epoch: 10 [
                      0/ 8390 ( 0%)] Loss: 1.855305 Accuracy: 28.12%
Train Epoch: 10 [ 3200/ 8390 ( 38%)] Loss: 1.746241 Accuracy: 32.09%
Train Epoch: 10 [ 6400/ 8390 ( 76%)] Loss: 1.742811 Accuracy: 32.70%
Epoch 10 - Time: 1714.28s - Train Loss: 1.838106 - Train Accuracy: 32.60%
Test Loss: 1.843091 - Test Accuracy: 33.31%
                      0/ 8390 ( 0%)] Loss: 1.638626 Accuracy: 46.88%
Train Epoch: 11 [
Train Epoch: 11 [ 3200/ 8390 ( 38%)] Loss: 1.710752 Accuracy: 34.38%
Train Epoch: 11 [ 6400/ 8390 ( 76%)] Loss: 1.678067 Accuracy: 33.78%
Epoch 11 - Time: 685.16s - Train Loss: 1.824078 - Train Accuracy: 33.58%
Test Loss: 1.925280 - Test Accuracy: 30.50%
Train Epoch: 12 [
                      0/ 8390 ( 0%)] Loss: 1.972635 Accuracy: 21.88%
Train Epoch: 12 [ 3200/ 8390 ( 38%)] Loss: 1.832804 Accuracy: 33.35%
Train Epoch: 12 [ 6400/ 8390 ( 76%)] Loss: 1.663738 Accuracy: 34.67%
Epoch 12 - Time: 229.54s - Train Loss: 1.800104 - Train Accuracy: 34.56%
Test Loss: 1.895443 - Test Accuracy: 29.94%
                      0/ 8390 ( 0%)] Loss: 1.694533 Accuracy: 46.88%
Train Epoch: 13 [
Train Epoch: 13 [ 3200/ 8390 ( 38%)] Loss: 2.048083 Accuracy: 34.31%
Train Epoch: 13 [ 6400/ 8390 ( 76\%)] Loss: 1.721056 Accuracy: 35.49%
Epoch 13 - Time: 247.96s - Train Loss: 1.801329 - Train Accuracy: 35.18%
Test Loss: 2.059045 - Test Accuracy: 28.69%
Train Epoch: 14 [
                      0/ 8390 ( 0%)] Loss: 1.800010 Accuracy: 31.25%
Train Epoch: 14 [ 3200/ 8390 ( 38%)] Loss: 1.848253 Accuracy: 35.61%
Train Epoch: 14 [ 6400/ 8390 ( 76%)] Loss: 1.741197 Accuracy: 35.54%
Epoch 14 - Time: 228.88s - Train Loss: 1.772695 - Train Accuracy: 35.88%
Test Loss: 1.796405 - Test Accuracy: 36.19%
Train Epoch: 15 [
                      0/ 8390 ( 0%)] Loss: 1.862352 Accuracy: 34.38%
             15 [ 3200/ 8390 ( 38%)] Loss: 1.758721 Accuracy: 36.26%
Train Epoch:
            15 [ 6400/ 8390 ( 76%)] Loss: 1.585711 Accuracy: 36.72%
Train Epoch:
Epoch 15 - Time: 225.72s - Train Loss: 1.766506 - Train Accuracy: 36.84%
Test Loss: 1.717395 - Test Accuracy: 36.69%
                      0/ 8390 ( 0%)] Loss: 1.405506 Accuracy: 56.25%
Train Epoch: 16 [
Train Epoch: 16 [ 3200/ 8390 ( 38%)] Loss: 1.843312 Accuracy: 37.53%
             16 [ 6400/ 8390 ( 76%)] Loss: 1.662048 Accuracy: 36.63%
Train Epoch:
Epoch 16 - Time: 227.74s - Train Loss: 1.762409 - Train Accuracy: 36.71%
Test Loss: 1.860578 - Test Accuracy: 30.94%
Train Epoch: 17 [
                      0/ 8390 ( 0%)] Loss: 1.506352 Accuracy: 46.88%
Train Epoch: 17 [ 3200/ 8390 ( 38%)] Loss: 1.742810 Accuracy: 37.41%
Train Epoch: 17 [ 6400/ 8390 ( 76%)] Loss: 1.585670 Accuracy: 37.00%
Epoch 17 - Time: 229.74s - Train Loss: 1.733406 - Train Accuracy: 37.16%
Test Loss: 1.890041 - Test Accuracy: 33.00%
Train Epoch: 18 [
                      0/ 8390 ( 0%)] Loss: 1.732439 Accuracy: 31.25%
Train Epoch: 18 [ 3200/ 8390 ( 38%)] Loss: 1.549548 Accuracy: 38.18%
Train Epoch: 18 [ 6400/ 8390 (76%)] Loss: 1.562699 Accuracy: 38.03%
Epoch 18 - Time: 236.13s - Train Loss: 1.706303 - Train Accuracy: 38.25%
Test Loss: 1.805835 - Test Accuracy: 31.38%
Train Epoch: 19 [
                      0/ 8390 ( 0%)] Loss: 1.522326 Accuracy: 53.12%
Train Epoch: 19 [ 3200/ 8390 ( 38%)] Loss: 1.878907 Accuracy: 39.14%
Train Epoch: 19 [ 6400/ 8390 ( 76%)] Loss: 1.591529 Accuracy: 38.68%
Epoch 19 - Time: 231.99s - Train Loss: 1.693270 - Train Accuracy: 39.06%
Test Loss: 1.893017 - Test Accuracy: 31.00%
```

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Train Epoch: 20 [
                      0/ 8390 ( 0%)] Loss: 1.637941 Accuracy: 34.38%
Train Epoch: 20 [ 3200/ 8390 ( 38%)] Loss: 1.428763 Accuracy: 38.27%
Train Epoch: 20 [ 6400/ 8390 (76%)] Loss: 1.534950 Accuracy: 38.63%
Epoch 20 - Time: 230.55s - Train Loss: 1.689023 - Train Accuracy: 39.01%
Test Loss: 1.742904 - Test Accuracy: 35.69%
                      0/ 8390 ( 0%)] Loss: 1.540716 Accuracy: 46.88%
Train Epoch: 21 [
Train Epoch: 21 [ 3200/ 8390 ( 38%)] Loss: 1.768099 Accuracy: 39.29%
Train Epoch: 21 [ 6400/ 8390 ( 76%)] Loss: 1.482714 Accuracy: 39.23%
Epoch 21 - Time: 234.37s - Train Loss: 1.677518 - Train Accuracy: 39.01%
Test Loss: 1.751613 - Test Accuracy: 38.19%
Train Epoch: 22 [
                      0/ 8390 ( 0%)] Loss: 1.777973 Accuracy: 43.75%
Train Epoch: 22 [ 3200/ 8390 ( 38%)] Loss: 1.748068 Accuracy: 39.88%
Train Epoch: 22 [ 6400/ 8390 ( 76%)] Loss: 1.431685 Accuracy: 40.66%
Epoch 22 - Time: 234.67s - Train Loss: 1.657473 - Train Accuracy: 40.64%
Test Loss: 1.876027 - Test Accuracy: 32.38%
                      0/ 8390 ( 0%)] Loss: 2.058917 Accuracy: 25.00%
Train Epoch: 23 [
Train Epoch: 23 [ 3200/ 8390 ( 38%)] Loss: 1.625033 Accuracy: 38.83%
Train Epoch: 23 [ 6400/ 8390 ( 76\%)] Loss: 1.697508 Accuracy: 39.80%
Epoch 23 - Time: 224.09s - Train Loss: 1.652329 - Train Accuracy: 40.42%
Test Loss: 1.726458 - Test Accuracy: 38.56%
Train Epoch: 24 [
                      0/ 8390 ( 0%)] Loss: 1.661963 Accuracy: 37.50%
Train Epoch: 24 [ 3200/ 8390 ( 38%)] Loss: 1.884388 Accuracy: 41.43%
Train Epoch: 24 [ 6400/ 8390 (76%)] Loss: 1.717796 Accuracy: 41.00%
Epoch 24 - Time: 226.88s - Train Loss: 1.633753 - Train Accuracy: 41.20%
Test Loss: 1.755266 - Test Accuracy: 39.50%
             25 [
                      0/ 8390 ( 0%)] Loss: 2.029453 Accuracy: 21.88%
Train Epoch:
             25 [ 3200/ 8390 ( 38%)] Loss: 1.803970 Accuracy: 41.62%
Train Epoch:
            25 [ 6400/ 8390 ( 76%)] Loss: 1.742526 Accuracy: 41.48%
Train Epoch:
Epoch 25 - Time: 241.10s - Train Loss: 1.638339 - Train Accuracy: 41.25%
Test Loss: 1.831373 - Test Accuracy: 35.31%
                      0/ 8390 ( 0%)] Loss: 1.667392 Accuracy: 43.75%
Train Epoch: 26 [
Train Epoch: 26 [ 3200/ 8390 ( 38%)] Loss: 1.706036 Accuracy: 43.75%
             26 [ 6400/ 8390 ( 76%)] Loss: 1.283091 Accuracy: 41.93%
Train Epoch:
Epoch 26 - Time: 242.64s - Train Loss: 1.636386 - Train Accuracy: 41.80%
Test Loss: 1.872317 - Test Accuracy: 37.25%
Train Epoch: 27 [
                      0/ 8390 ( 0%)] Loss: 1.798654 Accuracy: 37.50%
Train Epoch: 27 [ 3200/ 8390 ( 38%)] Loss: 1.548966 Accuracy: 40.69%
Train Epoch: 27 [ 6400/ 8390 (76%)] Loss: 1.751830 Accuracy: 42.37%
Epoch 27 - Time: 227.35s - Train Loss: 1.597866 - Train Accuracy: 42.66%
Test Loss: 1.769318 - Test Accuracy: 35.69%
Train Epoch: 28 [
                      0/ 8390 ( 0%)] Loss: 1.510158 Accuracy: 40.62%
Train Epoch: 28 [ 3200/ 8390 ( 38%)] Loss: 1.709183 Accuracy: 43.53%
Train Epoch: 28 [ 6400/ 8390 (76%)] Loss: 1.747401 Accuracy: 42.75%
Epoch 28 - Time: 226.97s - Train Loss: 1.610359 - Train Accuracy: 42.72%
Test Loss: 1.805375 - Test Accuracy: 37.50%
Train Epoch: 29 [
                      0/ 8390 ( 0%)] Loss: 1.620673 Accuracy: 43.75%
Train Epoch: 29 [ 3200/ 8390 ( 38%)] Loss: 1.735744 Accuracy: 43.16%
Train Epoch: 29 [ 6400/ 8390 ( 76%)] Loss: 1.518578 Accuracy: 43.52%
Epoch 29 - Time: 222.71s - Train Loss: 1.580171 - Train Accuracy: 43.17%
Test Loss: 1.713054 - Test Accuracy: 37.12%
```

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Train Epoch: 30 [
                      0/ 8390 ( 0%)] Loss: 1.523651 Accuracy: 43.75%
Train Epoch: 30 [ 3200/ 8390 ( 38%)] Loss: 1.402524 Accuracy: 42.82%
Train Epoch: 30 [ 6400/ 8390 ( 76%)] Loss: 1.423656 Accuracy: 43.17%
Epoch 30 - Time: 221.71s - Train Loss: 1.588955 - Train Accuracy: 43.31%
Test Loss: 1.720405 - Test Accuracy: 40.56%
                      0/ 8390 ( 0%)] Loss: 1.578195 Accuracy: 53.12%
Train Epoch: 31 [
Train Epoch: 31 [ 3200/ 8390 ( 38%)] Loss: 1.480698 Accuracy: 45.45%
Train Epoch: 31 [ 6400/ 8390 ( 76%)] Loss: 1.441470 Accuracy: 45.94%
Epoch 31 - Time: 224.97s - Train Loss: 1.546672 - Train Accuracy: 45.16%
Test Loss: 1.775559 - Test Accuracy: 38.19%
Train Epoch: 32 [
                      0/ 8390 ( 0%)] Loss: 1.695147 Accuracy: 37.50%
Train Epoch: 32 [ 3200/ 8390 ( 38%)] Loss: 1.325187 Accuracy: 44.86%
Train Epoch: 32 [ 6400/ 8390 ( 76%)] Loss: 1.499307 Accuracy: 44.71%
Epoch 32 - Time: 232.97s - Train Loss: 1.528269 - Train Accuracy: 45.01%
Test Loss: 1.851925 - Test Accuracy: 35.56%
                      0/ 8390 ( 0%)] Loss: 1.566870 Accuracy: 37.50%
Train Epoch: 33 [
Train Epoch: 33 [ 3200/ 8390 ( 38%)] Loss: 1.623017 Accuracy: 46.81%
Train Epoch: 33 [ 6400/ 8390 ( 76\%)] Loss: 1.333343 Accuracy: 46.13\%
Epoch 33 - Time: 222.50s - Train Loss: 1.519943 - Train Accuracy: 45.77%
Test Loss: 1.797330 - Test Accuracy: 38.19%
Train Epoch: 34 [
                      0/ 8390 ( 0%)] Loss: 1.530742 Accuracy: 53.12%
Train Epoch: 34 [ 3200/ 8390 ( 38%)] Loss: 1.340442 Accuracy: 46.26%
Train Epoch: 34 [ 6400/ 8390 ( 76%)] Loss: 1.714650 Accuracy: 46.25%
Epoch 34 - Time: 371.90s - Train Loss: 1.506658 - Train Accuracy: 46.63%
Test Loss: 1.941669 - Test Accuracy: 35.25%
                      0/ 8390 ( 0%)] Loss: 1.191646 Accuracy: 65.62%
Train Epoch:
             35 [
                  3200/ 8390 ( 38%)] Loss: 1.346883 Accuracy: 46.75%
Train Epoch:
             35 [
             35 [ 6400/ 8390 ( 76%)] Loss: 1.417341 Accuracy: 46.50%
Train Epoch:
Epoch 35 - Time: 839.33s - Train Loss: 1.492409 - Train Accuracy: 46.16%
Test Loss: 1.755629 - Test Accuracy: 39.75%
                      0/ 8390 ( 0%)] Loss: 1.476019 Accuracy: 46.88%
Train Epoch: 36 [
Train Epoch: 36 [ 3200/ 8390 ( 38%)] Loss: 1.865099 Accuracy: 46.26%
            36 [ 6400/ 8390 ( 76%)] Loss: 1.578250 Accuracy: 47.51%
Train Epoch:
Epoch 36 - Time: 260.74s - Train Loss: 1.480662 - Train Accuracy: 47.54%
Test Loss: 1.746769 - Test Accuracy: 41.62%
Train Epoch: 37 [
                      0/ 8390 ( 0%)] Loss: 1.372396 Accuracy: 65.62%
Train Epoch: 37 [ 3200/ 8390 ( 38%)] Loss: 1.404371 Accuracy: 48.58%
Train Epoch: 37 [ 6400/ 8390 ( 76%)] Loss: 1.312795 Accuracy: 47.89%
Epoch 37 - Time: 238.93s - Train Loss: 1.456575 - Train Accuracy: 47.79%
Test Loss: 1.713381 - Test Accuracy: 40.44%
Train Epoch: 38 [
                      0/ 8390 ( 0%)] Loss: 1.285304 Accuracy: 46.88%
Train Epoch: 38 [ 3200/ 8390 ( 38%)] Loss: 1.466446 Accuracy: 47.06%
Train Epoch: 38 [ 6400/ 8390 (76%)] Loss: 1.480421 Accuracy: 47.50%
Epoch 38 - Time: 225.90s - Train Loss: 1.466263 - Train Accuracy: 47.52%
Test Loss: 1.734649 - Test Accuracy: 39.38%
Train Epoch: 39 [
                      0/ 8390 ( 0%)] Loss: 1.281939 Accuracy: 56.25%
Train Epoch: 39 [ 3200/ 8390 ( 38%)] Loss: 1.203103 Accuracy: 49.04%
Train Epoch: 39 [ 6400/ 8390 ( 76%)] Loss: 1.221993 Accuracy: 48.69%
Epoch 39 - Time: 233.83s - Train Loss: 1.438474 - Train Accuracy: 48.75%
Test Loss: 1.698388 - Test Accuracy: 41.25%
```

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Train Epoch: 40 [
                      0/ 8390 ( 0%)] Loss: 1.390738 Accuracy: 50.00%
Train Epoch: 40 [ 3200/ 8390 ( 38%)] Loss: 1.468864 Accuracy: 48.05%
Train Epoch: 40 [ 6400/ 8390 ( 76%)] Loss: 1.655652 Accuracy: 49.02%
Epoch 40 - Time: 234.83s - Train Loss: 1.442420 - Train Accuracy: 48.86%
Test Loss: 1.713381 - Test Accuracy: 40.88%
                      0/ 8390 ( 0%)] Loss: 1.223912 Accuracy: 46.88%
Train Epoch: 41 [
Train Epoch: 41 [ 3200/ 8390 ( 38%)] Loss: 1.173113 Accuracy: 48.42%
Train Epoch: 41 [ 6400/ 8390 ( 76%)] Loss: 1.541021 Accuracy: 48.74%
Epoch 41 - Time: 240.24s - Train Loss: 1.412495 - Train Accuracy: 48.99%
Test Loss: 1.804260 - Test Accuracy: 40.00%
Train Epoch: 42 [
                      0/ 8390 ( 0%)] Loss: 1.315914 Accuracy: 56.25%
Train Epoch: 42 [ 3200/ 8390 ( 38%)] Loss: 1.457621 Accuracy: 50.93%
Train Epoch: 42 [ 6400/ 8390 ( 76%)] Loss: 1.301119 Accuracy: 49.56%
Epoch 42 - Time: 228.13s - Train Loss: 1.408532 - Train Accuracy: 49.81%
Test Loss: 1.848636 - Test Accuracy: 36.69%
                      0/ 8390 ( 0%)] Loss: 1.095912 Accuracy: 68.75%
Train Epoch: 43 [
Train Epoch: 43 [ 3200/ 8390 ( 38%)] Loss: 1.502681 Accuracy: 52.04%
Train Epoch: 43 [ 6400/ 8390 ( 76\%)] Loss: 1.337117 Accuracy: 50.92%
Epoch 43 - Time: 231.53s - Train Loss: 1.396336 - Train Accuracy: 50.35%
Test Loss: 1.700084 - Test Accuracy: 42.94%
Train Epoch: 44 [
                      0/ 8390 ( 0%)] Loss: 1.331070 Accuracy: 53.12%
Train Epoch: 44 [ 3200/ 8390 ( 38%)] Loss: 1.648317 Accuracy: 51.79%
Train Epoch: 44 [ 6400/ 8390 ( 76%)] Loss: 1.354382 Accuracy: 51.85%
Epoch 44 - Time: 234.37s - Train Loss: 1.361948 - Train Accuracy: 51.42%
Test Loss: 1.661956 - Test Accuracy: 42.50%
Train Epoch: 45 [
                      0/ 8390 ( 0%)] Loss: 1.314737 Accuracy: 62.50%
                  3200/ 8390 ( 38%)] Loss: 1.620541 Accuracy: 53.00%
Train Epoch:
             45 [
Train Epoch: 45 [ 6400/ 8390 (76%)] Loss: 1.276034 Accuracy: 51.38%
Epoch 45 - Time: 237.77s - Train Loss: 1.358715 - Train Accuracy: 51.16%
Test Loss: 1.723875 - Test Accuracy: 39.81%
                      0/ 8390 ( 0%)] Loss: 1.273015 Accuracy: 53.12%
Train Epoch: 46 [
Train Epoch: 46 [ 3200/ 8390 ( 38%)] Loss: 1.205081 Accuracy: 51.89%
Train Epoch: 46 [ 6400/ 8390 ( 76%)] Loss: 1.084803 Accuracy: 51.94%
Epoch 46 - Time: 230.29s - Train Loss: 1.345437 - Train Accuracy: 52.11%
Test Loss: 1.786524 - Test Accuracy: 40.50%
Train Epoch: 47 [
                      0/ 8390 ( 0%)] Loss: 1.356501 Accuracy: 46.88%
Train Epoch: 47 [ 3200/ 8390 ( 38%)] Loss: 1.344147 Accuracy: 52.26%
Train Epoch: 47 [ 6400/ 8390 ( 76%)] Loss: 1.232960 Accuracy: 52.39%
Epoch 47 - Time: 235.62s - Train Loss: 1.351638 - Train Accuracy: 52.31%
Test Loss: 1.924757 - Test Accuracy: 37.25%
Train Epoch: 48 [
                      0/ 8390 ( 0%)] Loss: 1.029061 Accuracy: 65.62%
Train Epoch: 48 [ 3200/ 8390 ( 38%)] Loss: 1.407160 Accuracy: 52.13%
Train Epoch: 48 [ 6400/ 8390 (76%)] Loss: 1.230066 Accuracy: 52.91%
Epoch 48 - Time: 237.75s - Train Loss: 1.333594 - Train Accuracy: 53.11%
Test Loss: 1.675849 - Test Accuracy: 42.44%
Train Epoch: 49 [
                      0/ 8390 ( 0%)] Loss: 1.518033 Accuracy: 46.88%
Train Epoch: 49 [ 3200/ 8390 ( 38%)] Loss: 1.227060 Accuracy: 52.78%
Train Epoch: 49 [ 6400/ 8390 ( 76%)] Loss: 1.245394 Accuracy: 53.25%
Epoch 49 - Time: 228.26s - Train Loss: 1.321129 - Train Accuracy: 53.13%
Test Loss: 1.728029 - Test Accuracy: 41.00%
```

FINAL RESULTS:

epoch_times: [1216.786159992218, 237.43125772476196, 3536.2034180164337, 2 55.0527946949005, 338.98512411117554, 249.76298189163208, 260.968131065368 65, 290.2906048297882, 2350.9871430397034, 1119.262617111206, 1714.2808780 670166, 685.1609690189362, 229.54470205307007, 247.95893597602844, 228.884 4177722931, 225.72268295288086, 227.74287104606628, 229.74079060554504, 23 6.1341609954834, 231.98818516731262, 230.55307173728943, 234.3666918277740 5, 234.67452025413513, 224.09229612350464, 226.87726593017578, 241.1005702 0187378, 242.64449501037598, 227.35298085212708, 226.97432398796082, 222.7 1014785766602, 221.70982909202576, 224.96943998336792, 232.96854400634766, 222.49809098243713, 371.89834690093994, 839.3271780014038, 260.74057102203 37, 238.9295699596405, 225.8984100818634, 233.8280041217804, 234.825166702 2705, 240.2430510520935, 228.12757992744446, 231.5294008255005, 234.373477 22053528, 237.76521015167236, 230.28806805610657, 235.62296104431152, 237.7456498146057, 228.25890517234802]

train_losses: [2.162851532906976, 2.0375869633587262, 1.9875167171463712, 1.9772260184506423, 1.973807847226849, 1.9229257152280734, 1.9137453100153 508, 1.8953898330681196, 1.899573454420075, 1.8580818735916196, 1.83810602 11713078, 1.824077689920673, 1.8001040738957528, 1.8013294184480915, 1.772 6950404298214, 1.7665060276293572, 1.7624088416572745, 1.7334060755394798, 1.706302819816211, 1.6932695644502422, 1.6890230351731976, 1.6775176966463 337, 1.657472894846938, 1.6523291555069786, 1.6337526204021833, 1.63833934 61467655, 1.6363864782202335, 1.5978663550078414, 1.6103589298160932, 1.58 0170889392154, 1.588955131650881, 1.546672313267948, 1.5282688573116565, 1.5199425070340398, 1.506657939375812, 1.492409292978185, 1.48066221894198 7, 1.4565749753067512, 1.4662629063347823, 1.4384736666697582, 1.442420180 5172985, 1.4124947722631556, 1.408531955407776, 1.3963362629177005, 1.3619 47868844025, 1.358714550961065, 1.3454369156415227, 1.3516383494129618, 1. 3335936713309688, 1.3211287958476379]

train_accuracies: [19.67818831942789, 24.27890345649583, 26.81764004767580 5, 27.36591179976162, 26.90107270560191, 29.36829558998808, 30.0, 31.13230 0357568536, 30.834326579261024, 32.37187127532777, 32.598331346841476, 33. 57568533969011, 34.56495828367104, 35.18474374255066, 35.87604290822408, 3 6.841477949940405, 36.7103694874851, 37.163289630512516, 38.2479141835518 5, 39.05840286054827, 39.01072705601907, 39.01072705601907, 40.64362336114 422, 40.417163289630516, 41.203814064362334, 41.25148986889154, 41.7997616 2097736, 42.65792610250298, 42.717520858164484, 43.1704410011919, 43.31346 84147795, 45.160905840286055, 45.00595947556615, 45.76877234803337, 46.626 936829559, 46.162097735399286, 47.54469606674613, 47.794994040524436, 47.5 20858164481524, 48.74851013110846, 48.85578069129917, 48.98688915375447, 4 9.80929678188319, 50.345649582836714, 51.418355184743746, 51.1561382598331 35, 52.109654350417166, 52.31227651966627, 53.1108462455304, 53.1346841477 94991

test_losses: [2.109093050956726, 2.066229785680771, 2.0960341399908065, 1.9843857073783875, 1.9469191420078278, 1.9604377828538417, 2.02019314527511 6, 2.0539393174648284, 2.0636624544113875, 1.877559413909912, 1.8430911654 233932, 1.92527961820364, 1.8954430627822876, 2.059045124053955, 1.7964048 707485198, 1.7173949246108533, 1.8605775427818299, 1.890041069984436, 1.80 5834757089615, 1.893017338514328, 1.7429044938087463, 1.751613089442253, 1.8760265758633614, 1.7264579290151596, 1.7552662622928619, 1.831373276114 4639, 1.87231743901968, 1.7693175518512725, 1.805375024974346, 1.713054386 973381, 1.7204049178957939, 1.7755592098832131, 1.8519245845079422, 1.7973 303461819887, 1.9416690100729466, 1.755628821849823, 1.7467694664001465, 1.7133814676105976, 1.734649378284812, 1.698387702703476, 1.71338147729635

25, 1.8042599228024483, 1.8486363255977631, 1.7000837564468383, 1.66195631 92129134, 1.7238749971985816, 1.7865237033367156, 1.9247570157051086, 1.67 58494615554809, 1.7280293914675713] test_accuracies: [22.25, 23.5625, 21.1875, 26.75, 28.125, 29.125, 25.0625, 31.875, 28.6875, 30.875, 33.3125, 30.5, 29.9375, 28.6875, 36.1875, 36.687 5, 30.9375, 33.0, 31.375, 31.0, 35.6875, 38.1875, 32.375, 38.5625, 39.5, 3 5.3125, 37.25, 35.6875, 37.5, 37.125, 40.5625, 38.1875, 35.5625, 38.1875, 35.25, 39.75, 41.625, 40.4375, 39.375, 41.25, 40.875, 40.0, 36.6875, 42.93 75, 42.5, 39.8125, 40.5, 37.25, 42.4375, 41.0]

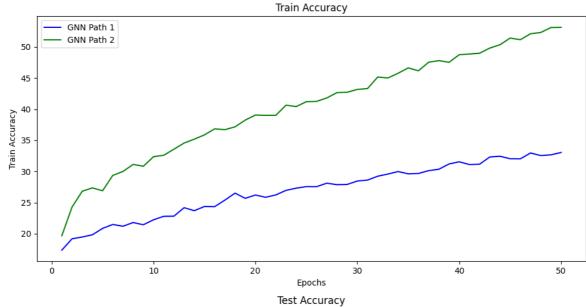
Plots

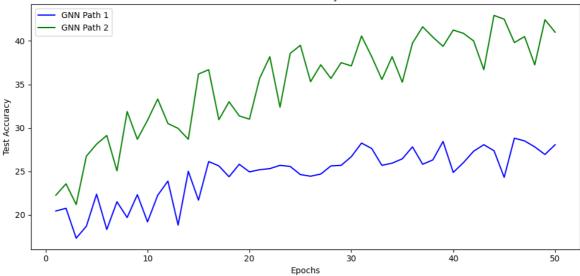
```
In [40]: # Data for the four scenarios
         data = {
             "GNN Path 1": metrics_dict_e1,
             "GNN Path 2": metrics_dict_e2,
         # Data for plotting
         epochs = range(1, 51)
         colors = ['b', 'g', 'r', 'm', 'y', 'c', 'k', '#FF5733', '#7E4DFF']
         scenarios = list(data.keys())
         fig, axes = plt.subplots(2, 1, figsize=(10, 10))
         for i, scenario in enumerate(scenarios):
             axes[0].plot(epochs, data[scenario]["train_accuracies"], label=scenar
         axes[0].set_title("Train Accuracy")
         axes[0].set_xlabel("Epochs")
         axes[0].set_ylabel("Train Accuracy")
         axes[0].legend()
         for i, scenario in enumerate(scenarios):
             axes[1].plot(epochs, data[scenario]["test_accuracies"], label=scenari
         axes[1].set_title("Test Accuracy")
         axes[1].set_xlabel("Epochs")
         axes[1].set_ylabel("Test Accuracy")
         axes[1].legend()
         plt.tight_layout()
         plt.show()
         fig, axes = plt.subplots(2, 1, figsize=(10, 10))
         for i, scenario in enumerate(scenarios):
             axes[0].plot(epochs, data[scenario]["train_losses"], label=scenario,
         axes[0].set title("Train Loss")
         axes[0].set_xlabel("Epochs")
         axes[0].set ylabel("Train Loss")
         axes[0].legend()
         for i, scenario in enumerate(scenarios):
             axes[1].plot(epochs, data[scenario]["test_losses"], label=scenario, c
         axes[1].set_title("Test Loss")
```

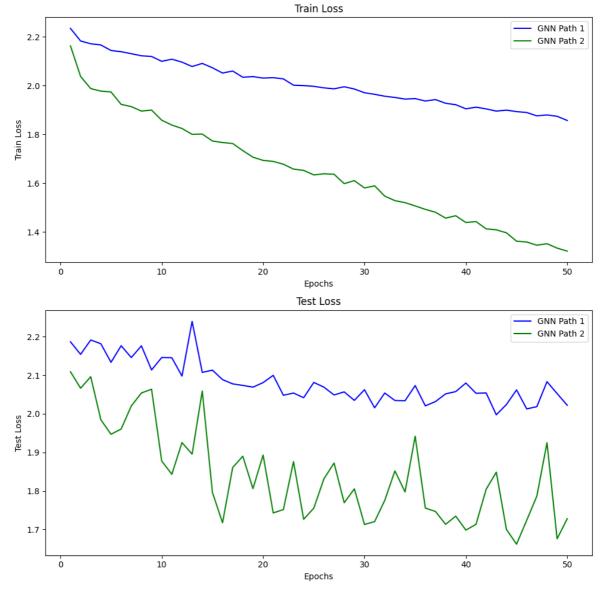
```
axes[1].set_xlabel("Epochs")
axes[1].set_ylabel("Test Loss")
axes[1].legend()

plt.tight_layout()
plt.show()

fig, axes = plt.subplots(1, 1, figsize=(10, 5))
for i, scenario in enumerate(scenarios):
    axes.plot(epochs, data[scenario]["epoch_times"], label=scenario, colo
axes.set_title("Time")
axes.set_xlabel("Epochs")
axes.set_ylabel("Time (secs)")
axes.legend()
```







Out[40]: <matplotlib.legend.Legend at 0x2af840c50>

